

**BEFORE THE PUBLIC SERVICE COMMISSION  
OF SOUTH CAROLINA**

**DIRECT TESTIMONY OF  
JAMES H. VANDER WEIDE, PH.D.**

**ON BEHALF OF  
DOMINION ENERGY SOUTH CAROLINA, INC.  
DOCKET NO. 2020-125-E**

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**I. INTRODUCTION**

**Q. PLEASE STATE YOUR NAME, BUSINESS ADDRESS, AND OCCUPATION.**

A. My name is James H. Vander Weide. I am President of Financial Strategy Associates, a firm that provides strategic and financial consulting services to business clients. My business address is 3606 Stoneybrook Drive, Durham, North Carolina 27705.

**Q. PLEASE DESCRIBE YOUR EDUCATIONAL BACKGROUND AND PRIOR ACADEMIC EXPERIENCE.**

A. I graduated from Cornell University with a Bachelor of Arts in Economics and from Northwestern University with a Ph.D. in Finance. After joining the faculty of the School of Business at Duke University, I was named Assistant Professor, Associate Professor, Professor, and then Research Professor. I have published research in the areas of finance and economics and taught courses in these fields at Duke for more than thirty-five years. I am now retired from my teaching duties at Duke. A summary of my research, teaching, and other professional experience is presented in Exhibit No. \_\_\_\_ (JWV-1).

**Q. HAVE YOU PREVIOUSLY TESTIFIED ON FINANCIAL OR ECONOMIC ISSUES?**

A. Yes. As an expert on financial and economic theory and practice, I have participated in more than five hundred regulatory and legal proceedings before the public service commissions of forty-five states and four Canadian provinces, the United States Congress, the Federal Energy Regulatory Commission, the National Energy Board (Canada), the Federal Communications Commission, the Canadian Radio-Television and Telecommunications Commission, the National Telecommunications and Information Administration, the insurance commissions of five states, the Iowa State Board of Tax Review, the National Association of Securities Dealers, and the North Carolina Property Tax Commission. In addition, I have prepared expert testimony in proceedings before the United States District Court for the District of Nebraska; the United States District Court for the District of New Hampshire; the United States District Court for the District of Northern Illinois; the United States District Court for the Eastern District of North Carolina; the United States District Court for the Northern District of California; the United

1 States District Court for the Eastern District of Michigan; the United States Bankruptcy  
2 Court for the Southern District of West Virginia; the Montana Second Judicial District  
3 Court, Silver Bow County; the Superior Court, North Carolina; and the Supreme Court of  
4 the State of New York.

5 **Q. WHAT IS THE PURPOSE OF YOUR TESTIMONY?**

6 A. I have been asked by Dominion Energy South Carolina, Inc. (“DESC” or “the Company”)  
7 to prepare an independent appraisal of DESC’s cost of equity and to recommend to the  
8 South Carolina Public Service Commission (“the Commission”) a rate of return on equity  
9 that is fair, that allows DESC to attract capital on reasonable terms, and that allows DESC  
10 to maintain its financial integrity.

11 **II. SUMMARY OF TESTIMONY**

12 **Q. HOW DO YOU ESTIMATE DESC’S COST OF EQUITY?**

13 A. I estimate DESC’s cost of equity by applying several standard cost of equity methods to  
14 market data for a large group of utility companies of comparable risk.

15 **Q. WHY DO YOU ESTIMATE DESC’S COST OF EQUITY BY APPLYING**  
16 **SEVERAL COST OF EQUITY METHODS TO MARKET DATA FOR A LARGE**  
17 **GROUP OF COMPARABLE RISK COMPANIES?**

18 A. I estimate DESC’S cost of equity by applying several cost of equity methods to a large  
19 group of comparable risk companies because standard cost of equity methods such as the  
20 discounted cash flow (“DCF”), risk premium, and capital asset pricing model (“CAPM”)  
21 require inputs of quantities that are not easily measured. Because these inputs can only be  
22 estimated, there is naturally some degree of uncertainty surrounding the estimate of the  
23 cost of equity for each company. However, the uncertainty in the estimate of the cost of  
24 equity for an individual company can be greatly reduced by applying several cost of equity  
25 methods to a relatively large sample of comparable companies. Intuitively, unusually high  
26 model estimates for some individual companies are offset by unusually low model  
27 estimates for other individual companies. Thus, financial economists generally apply  
28 several cost of equity methods to a relatively large group of comparable companies. In  
29 utility regulation, the practice of using a group of comparable companies, called the

comparable company approach, is further supported by the United States Supreme Court standard that the utility should be allowed to earn a return on its investment that is commensurate with returns being earned on other investments of the same risk. (See *Bluefield Waterworks and Imp. Co. v. Public Service Comm'n of W. Va.*, 262 U.S. 679, 692 (1923) and *Federal Power Comm'n v. Hope Natural Gas Co.*, 320 U.S. 591, 603 (1944).)

**Q. WHAT FAIR RATE OF RETURN ON EQUITY DO YOU RECOMMEND FOR DESC?**

A. I recommend a fair rate of return on equity for DESC equal to 10.4 percent.

**Q. HOW DO YOU ARRIVE AT YOUR RECOMMENDED 10.4 PERCENT FAIR RATE OF RETURN ON EQUITY FOR DESC?**

A. I arrive at my recommended 10.4 percent fair rate of return on equity for DESC by first applying standard cost of equity estimation techniques, including the DCF model, the ex ante risk premium approach, the ex post risk premium approach, the CAPM, and the comparable earnings method to a broad group of companies of comparable *business* risk. From my application of these methods, I obtain an average cost of equity result equal to 9.8 percent. I then adjust this cost of equity to reflect the higher *financial* risk associated with DESC's ratemaking capital structure compared to the lower financial risk associated with the average market-value capital structure of my proxy company group. (The calculation that produces the adjusted cost of equity, which is required to have the same overall return on capital as the proxy group in the marketplace, is described below and shown in Exhibit No. \_\_\_\_ (JVW-2).

**Q. YOU NOTE THAT YOUR COMPARABLE COMPANY GROUP HAS SIMILAR BUSINESS RISK TO DESC, BUT LESS FINANCIAL RISK THAN DESC. WHAT IS THE DIFFERENCE BETWEEN BUSINESS RISK AND FINANCIAL RISK?**

A. Business risk is the underlying risk that investors will earn less than their required return on investment when the investment is financed entirely with equity. Financial risk is the additional risk of earning less than the required return when the investment is financed with both fixed-cost debt and equity.

1 **Q. YOU ADJUST THE COST OF EQUITY OF YOUR PROXY COMPANIES TO**  
2 **REFLECT THE HIGHER FINANCIAL RISK IN DESC'S RATEMAKING**  
3 **CAPITAL STRUCTURE COMPARED TO THE LOWER FINANCIAL RISK IN**  
4 **THE PROXY GROUP'S MARKET VALUE CAPITAL STRUCTURE. WHY IS**  
5 **THAT ADJUSTMENT NEEDED?**

6 A. This adjustment is needed because the cost of equity for my proxy companies measures the  
7 return investors require in the capital markets on other investments of comparable risk,  
8 including both business risk and financial risk. Although my proxy company group has  
9 comparable business risk to DESC, the proxy group has less financial risk than DESC  
10 because DESC's recommended ratemaking capital structure contains a higher percentage  
11 of debt and a lower percentage of equity than the average market value capital structure  
12 investors use to measure the financial risk of investing in the proxy companies. It is both  
13 logically and economically inconsistent to apply a cost of equity developed for a sample of  
14 companies with a specific degree of financial risk to a capital structure with a different  
15 degree of financial risk. To be consistent, one must adjust the cost of equity for my proxy  
16 companies upward in order for investors in DESC to have an opportunity to earn a return  
17 on their investment in DESC that is commensurate with returns investors could earn in the  
18 capital markets on other investments of comparable risk.

19 **Q. WHAT IS THE DIFFERENCE BETWEEN DESC'S RECOMMENDED RATE**  
20 **MAKING CAPITAL STRUCTURE AND THE AVERAGE MARKET VALUE**  
21 **CAPITAL STRUCTURE OF YOUR PROXY UTILITY COMPANY GROUP?**

22 A. DESC's recommended rate making capital structure in this proceeding contains  
23 46.65 percent debt and 53.35 percent common equity, whereas the average market value  
24 capital structure for my proxy group of utilities contains approximately 40 percent debt and  
25 60 percent common equity. (I note that I have also examined the average market value  
26 capital structure for the Value Line electric utilities over the last five years, and I find that  
27 the average market value capital structure for the Value Line electric utilities over this  
28 period contains approximately 37 percent debt and 63 percent equity.) Thus, the financial  
29 risk of DESC as reflected in its recommended rate making capital structure is greater than  
30 the financial risk embedded in the cost of equity estimates for my proxy companies.

1 **Q. DO YOU HAVE EXHIBITS ACCOMPANYING YOUR TESTIMONY?**

2 A. Yes. I have prepared or supervised the preparation of 16 exhibits that accompany my  
3 testimony. The 16 exhibits are attached as Exhibit No. \_\_\_\_ (JWV-1) through  
4 Exhibit No. \_\_\_\_ (JWV-16).

5 **III. ECONOMIC AND LEGAL PRINCIPLES**

6 **Q. HOW DO ECONOMISTS DEFINE THE REQUIRED RATE OF RETURN, OR**  
7 **COST OF CAPITAL, ASSOCIATED WITH PARTICULAR INVESTMENT**  
8 **DECISIONS SUCH AS THE DECISION TO INVEST IN ELECTRIC UTILITY**  
9 **PLANT AND EQUIPMENT?**

10 A. Economists define the cost of capital as the return investors expect to receive on alternative  
11 investments of comparable risk.

12 **Q. HOW DOES THE COST OF CAPITAL AFFECT A FIRM'S INVESTMENT**  
13 **DECISIONS?**

14 A. The goal of a firm is to maximize the value of the firm. This goal can be accomplished by  
15 investing only in plant and equipment with an expected rate of return that is equal to or  
16 greater than the cost of capital. Thus, a firm should continue to invest in plant and  
17 equipment only as long as the return on its investment is equal to or greater than its cost of  
18 capital.

19 **Q. HOW DOES THE COST OF CAPITAL AFFECT INVESTORS' WILLINGNESS**  
20 **TO INVEST IN A COMPANY?**

21 A. The cost of capital measures the return investors can expect on investments of comparable  
22 risk. The cost of capital also measures the investor's required rate of return on investment  
23 because rational investors will not invest in a particular investment opportunity if the  
24 expected return on that opportunity is less than the cost of capital. Thus, the cost of capital  
25 is a hurdle rate for both investors and the firm.

26 **Q. DO ALL INVESTORS HAVE THE SAME POSITION IN THE FIRM?**

27 A. No. Debt investors have a fixed claim on a firm's assets and income that must be paid prior  
28 to any payment to the firm's equity investors. Because the firm's equity investors have a

1 residual claim on the firm's assets and income, equity investments are riskier than debt  
2 investments. Thus, the cost of equity exceeds the cost of debt.

3 **Q. WHAT IS THE OVERALL OR WEIGHTED AVERAGE COST OF CAPITAL?**

4 A. The overall or average cost of capital is a weighted average of the cost of debt and cost of  
5 equity, where the weights are the percentages of debt and equity in a firm's capital  
6 structure.

7 **Q. CAN YOU ILLUSTRATE THE CALCULATION OF THE OVERALL OR**  
8 **WEIGHTED AVERAGE COST OF CAPITAL?**

9 A. Yes. Assume that the cost of debt is 7 percent, the cost of equity is 11 percent, and the  
10 percentages of debt and equity in the firm's capital structure are 50 percent and 50 percent,  
11 respectively. Then the weighted average cost of capital is expressed by 0.50 times 7 percent  
12 plus 0.50 times 11 percent, or 9.0 percent.

13 **Q. HOW DO ECONOMISTS DEFINE THE COST OF EQUITY?**

14 A. Economists define the cost of equity as the return investors expect to receive on alternative  
15 equity investments of comparable risk. Because the return on an equity investment of  
16 comparable risk is not a contractual return, the cost of equity is more difficult to measure  
17 than the cost of debt. However, as I have already noted, there is agreement among  
18 economists that the cost of equity is greater than the cost of debt. There is also agreement  
19 among economists that the cost of equity is both forward looking and market based.

20 **Q. HOW DO ECONOMISTS MEASURE THE PERCENTAGES OF DEBT AND**  
21 **EQUITY IN A FIRM'S CAPITAL STRUCTURE?**

22 A. Economists measure the percentages of debt and equity in a firm's capital structure by first  
23 calculating the market value of the firm's debt and the market value of its equity.  
24 Economists then calculate the percentage of debt by the ratio of the market value of debt  
25 to the combined market values of debt and equity, and the percentage of equity by the ratio  
26 of the market value of equity to the combined market values of debt and equity. For  
27 example, if a firm's debt has a market value of \$25 million and its equity has a market



1 value of \$75 million, then its total market capitalization is \$100 million, and its capital  
2 structure contains 25 percent debt and 75 percent equity.

3 **Q. WHY DO ECONOMISTS MEASURE A FIRM'S CAPITAL STRUCTURE IN**  
4 **TERMS OF THE MARKET VALUES OF ITS DEBT AND EQUITY?**

5 A. Economists measure a firm's capital structure in terms of the market values of its debt and  
6 equity because: (1) the weighted average cost of capital is defined as the return investors  
7 expect to earn on a portfolio of the company's debt and equity securities; (2) investors  
8 measure the expected return and risk on their portfolios using market value weights, not  
9 book value weights; and (3) market values are the best measures of the amounts of debt  
10 and equity investors have invested in the company on a going forward basis.

11 **Q. WHY DO INVESTORS MEASURE THE EXPECTED RETURN AND RISK ON**  
12 **THEIR INVESTMENT PORTFOLIOS USING MARKET VALUE WEIGHTS**  
13 **RATHER THAN BOOK VALUE WEIGHTS?**

14 A. Investors measure the expected return and risk on their investment portfolios using market  
15 value weights because: (1) the expected return on a portfolio is calculated by comparing  
16 the expected value of the portfolio at the end of the investment period to its current value;  
17 (2) the risk of a portfolio is calculated by examining the variability of the return on the  
18 portfolio about the expected value; and (3) market values are the best measure of the  
19 current value of the portfolio. From the investor's point of view, the historical cost, or book  
20 value of their investment, is generally a poor indicator of the portfolio's current value.

21 **Q. IS THE ECONOMIC DEFINITION OF THE WEIGHTED AVERAGE COST OF**  
22 **CAPITAL CONSISTENT WITH REGULATORS' TRADITIONAL DEFINITION**  
23 **OF THE WEIGHTED AVERAGE COST OF CAPITAL?**

24 A. No. The economic definition of the weighted average cost of capital is based on the market  
25 costs of debt and equity, the market value percentages of debt and equity in a company's  
26 capital structure, and the future expected risk of investing in the company. In contrast,  
27 regulators have traditionally defined the weighted average cost of capital using the  
28 embedded cost of debt and the book or accounting values of debt and equity shown on a  
29 company's balance sheet. A company's market value capital structure generally differs

1 from its book value capital structure because the market value capital structure reflects the  
2 current values of the company's debt and equity in the capital markets, whereas the  
3 company's book value capital structure reflects the values of the company's debt and equity  
4 based on historical accounting costs.

5 **Q. WILL INVESTORS HAVE AN OPPORTUNITY TO EARN A FAIR RETURN ON**  
6 **THE VALUE OF THEIR EQUITY INVESTMENT IN THE COMPANY IF**  
7 **REGULATORS CALCULATE THE WEIGHTED AVERAGE COST OF CAPITAL**  
8 **USING THE BOOK VALUE OF EQUITY IN THE COMPANY'S CAPITAL**  
9 **STRUCTURE?**

10 A. No. Investors will only have an opportunity to earn a fair return on the value of their equity  
11 investment if regulators either: (1) calculate the weighted average cost of capital using the  
12 market value of equity in the company's capital structure; or (2) adjust the cost of equity  
13 for the difference between the financial risk reflected in the market value capital structures  
14 of the proxy companies and the financial risk reflected in the company's ratemaking capital  
15 structure.

16 **Q. ARE THE ECONOMIC PRINCIPLES REGARDING THE FAIR RETURN FOR**  
17 **CAPITAL RECOGNIZED IN ANY UNITED STATES SUPREME COURT**  
18 **CASES?**

19 A. Yes. These economic principles, relating to the supply of and demand for capital, are  
20 recognized in two United States Supreme Court cases: (1) *Bluefield Waterworks and*  
21 *Improvement Co. v. Public Service Comm'n. of W. Va.*; and (2) *Federal Power Comm'n v.*  
22 *Hope Natural Gas Co.* In the *Bluefield Waterworks* case, the Court stated:

23 A public utility is entitled to such rates as will permit it to earn a return upon  
24 the value of the property which it employs for the convenience of the public  
25 equal to that generally being made at the same time and in the same general  
26 part of the country on investments in other business undertakings which are  
27 attended by corresponding risks and uncertainties; but it has no  
28 constitutional right to profits such as are realized or anticipated in highly  
29 profitable enterprises or speculative ventures. The return should be

1 reasonably sufficient to assure confidence in the financial soundness of the  
2 utility, and should be adequate, under efficient and economical  
3 management, to maintain and support its credit, and enable it to raise the  
4 money necessary for the proper discharge of its public duties. [*Bluefield*  
5 *Waterworks and Improvement Co. v. Public Service Comm'n.* 262 U.S. 679,  
6 692 (1923).]

7 The Court clearly recognizes here that: (1) a regulated firm cannot remain financially sound  
8 unless the return it is allowed to earn on the value of its property is at least equal to the cost  
9 of capital (the principle relating to the demand for capital); and (2) a regulated firm will  
10 not be able to attract capital if it does not offer investors an opportunity to earn a return on  
11 their investment equal to the return they expect to earn on other investments of the same  
12 risk (the principle relating to the supply of capital).

13 In the *Hope Natural Gas* case, the Court reiterates the financial soundness and capital  
14 attraction principles of the *Bluefield* case:

15 From the investor or company point of view it is important that there be  
16 enough revenue not only for operating expenses but also for the capital costs  
17 of the business. These include service on the debt and dividends on the  
18 stock... By that standard the return to the equity owner should be  
19 commensurate with returns on investments in other enterprises having  
20 corresponding risks. That return, moreover, should be sufficient to assure  
21 confidence in the financial integrity of the enterprise, so as to maintain its  
22 credit and to attract capital. [*Federal Power Comm'n v. Hope Natural Gas*  
23 *Co.*, 320 U.S. 591, 603 (1944).]

24 The Court clearly recognizes in these decisions that the fair rate of return on equity should  
25 be: (1) comparable to returns investors expect to earn on other investments of similar risk;  
26 (2) sufficient to assure confidence in the company's financial integrity; and (3) adequate to  
27 maintain and support the company's credit and to attract capital.

1 **Q. ARE THESE PRINCIPLES APPLIED IN SOUTH CAROLINA?**

2 A. Yes. The Commission previously recognized and applied the *Hope* and *Bluefield* standards  
3 in Order No. 2010-471, dated July 15, 2010, and issued in Docket No. 2009-489-E. The  
4 South Carolina Supreme Court also recognized and applied these standards in *S. Bell Tel.*  
5 *& Tel. Co. v. Public Service Comm'n of South Carolina*, 244 S.E.2d 278 (1978).

6 **IV. BUSINESS AND FINANCIAL RISKS**

7 **Q. HOW DO INVESTORS ESTIMATE THE EXPECTED RATE OF RETURN ON**  
8 **SPECIFIC INVESTMENTS, SUCH AS AN INVESTMENT IN DESC?**

9 A. Investors estimate the expected rate of return in several steps. First, they estimate the  
10 amount of their investment in the company. Second, they estimate the timing and amounts  
11 of the cash flows they expect to receive from their investment over the life of the  
12 investment. Third, they determine the return, or discount rate, that equates the present value  
13 of the expected cash receipts from their investment in the company to the current value of  
14 their investment in the company.

15 **Q. ARE THE RETURNS ON INVESTMENT OPPORTUNITIES, SUCH AS AN**  
16 **INVESTMENT IN DESC, KNOWN WITH CERTAINTY AT THE TIME THE**  
17 **INVESTMENT IS MADE?**

18 A. No. The return on an investment in DESC depends on the Company's expected future cash  
19 flows over the life of the investment, as discussed above. Because the Company's expected  
20 future cash flows are uncertain at the time the investment is made, the return on the  
21 investment is also uncertain.

22 **Q. YOU MENTION THAT INVESTORS REQUIRE A RETURN ON INVESTMENT**  
23 **THAT IS EQUAL TO THE RETURN THEY EXPECT TO RECEIVE ON OTHER**  
24 **INVESTMENTS OF SIMILAR RISK. DOES THE REQUIRED RETURN ON AN**  
25 **INVESTMENT DEPEND ON THE INVESTOR'S ESTIMATE OF THE RISK OF**  
26 **THAT INVESTMENT?**

27 A. Yes. Because investors are averse to risk, they require a higher rate of return on investments  
28 with greater risk.

1 **Q. WHAT FUNDAMENTAL RISK DO INVESTORS FACE WHEN THEY INVEST**  
2 **IN A COMPANY SUCH AS DESC?**

3 A. Investors face the fundamental risk that their realized, or actual, return on investment, will  
4 be less than their required return on investment.

5 **Q. HOW DO INVESTORS MEASURE INVESTMENT RISK?**

6 A. Investors generally measure investment risk by estimating the probability, or likelihood, of  
7 earning less than the required return on investment. For investments with potential returns  
8 distributed symmetrically about the expected, or mean return, investors can also measure  
9 investment risk by estimating the variance, or volatility, of the potential return on  
10 investment.

11 **Q. DO INVESTORS DISTINGUISH BETWEEN BUSINESS AND FINANCIAL RISK?**

12 A. Yes. Business risk is the underlying risk that investors will earn less than their required  
13 return on investment when the investment is financed entirely with equity. Financial risk  
14 is the additional risk of earning less than the required return when the investment is  
15 financed with both fixed-cost debt and equity.

16 **Q. WHAT ARE THE PRIMARY DETERMINANTS OF AN ELECTRIC UTILITY'S**  
17 **BUSINESS RISK?**

18 A. The business risk of investing in electric utility companies such as DESC is caused by:  
19 (1) demand uncertainty; (2) operating expense uncertainty; (3) investment cost  
20 uncertainty; (4) high operating leverage; and (5) regulatory uncertainty.

21 **Q. WHAT CAUSES THE DEMAND FOR ELECTRICITY TO BE UNCERTAIN?**

22 A. Electric utilities experience demand uncertainty in both the short run and the long run.  
23 Short-run demand uncertainty is caused by the strong dependence of electric demand on  
24 the state of the economy, the average temperature during the peak heating and cooling  
25 seasons, and the possibility of service interruptions due to accidents and/or natural  
26 disasters. Long-run demand uncertainty is caused by: (a) the sensitivity of demand to  
27 changes in rates; (b) the efforts of customers to conserve energy; (c) the potential  
28 development of new energy efficient technologies and appliances; (d) the improved

1 economics of distributed generation; (e) the ability of some customers to co-generate their  
2 own electricity or purchase electricity from competitors; (f) the uncertain impact of  
3 changing governmental regulations and subsidies on the price of electricity; and (g) the  
4 uncertain impact of unprecedented events such as the Coronavirus pandemic on economic  
5 conditions and the demand for electricity.

6 **Q. HOW DOES SHORT-RUN DEMAND UNCERTAINTY AFFECT AN ELECTRIC**  
7 **UTILITY'S BUSINESS RISK?**

8 A. Short-run demand uncertainty affects an electric utility's business risk through its impact  
9 on the variability of the company's revenues and its return on investment. The greater the  
10 short-run uncertainty in demand, the greater is the uncertainty in the company's yearly  
11 revenues and return on investment.

12 **Q. HOW DOES LONG-RUN DEMAND UNCERTAINTY AFFECT AN ELECTRIC**  
13 **UTILITY'S BUSINESS RISK?**

14 A. Long-run demand uncertainty affects an electric utility's business risk through its impact  
15 on the utility's revenues over the life of its plant investments. Long-run demand uncertainty  
16 creates greater risk for electric utilities because investments in electric utility infrastructure  
17 are long-lived and irreversible. If demand turns out to be less than expected over the life of  
18 the investment, or the economic life of the investment turns out to be less than expected at  
19 the time the investment was made, the utility may not be able to generate sufficient  
20 revenues over the life of the investment to cover its operating expenses and earn a fair  
21 return on its investment.

22 **Q. DOES DESC EXPERIENCE DEMAND UNCERTAINTY?**

23 A. Yes. DESC experiences demand uncertainty in both the short run and the long run. The  
24 Company experiences short-run demand uncertainty as a result of economic cycles, such  
25 as in recessions, when fewer homes are built, fewer new businesses are started, and  
26 factories run at less than full capacity; and as a result of weather patterns, such as unusually  
27 warm winters and cool summers. DESC experiences long-run demand uncertainty when it  
28 invests in major long-lived plant additions or replacements that are expected to remain in  
29 service for at least thirty or forty years. If future actual demand turns out to be less than

1 forecast demand, or if the life of the investment turns out to be less than the expected life  
2 due to technological, competitive, or regulatory changes (such as changes in environmental  
3 regulations), the Company may not generate sufficient revenues to recover its investment  
4 and earn a fair return on its investment.

5 **Q. DO INVESTORS RECOGNIZE THAT DESC'S FINANCIAL RESULTS MAY BE**  
6 **ADVERSELY AFFECTED BY DEMAND UNCERTAINTY?**

7 A. Yes. As the Company explains in its most recent Form 10-K filing:

8 DESC's financial results can be adversely affected by various factors  
9 driving supply and demand for electricity and gas and related services.  
10 Technological advances required by federal laws mandate new levels of  
11 energy efficiency in end-use devices, including lighting, furnaces and  
12 electric heat pumps and could lead to declines in per capita energy  
13 consumption. Additionally, certain regulatory and legislative bodies have  
14 introduced or are considering requirements and/or incentives to reduce  
15 energy consumption by a fixed date. Further, DESC's business model is  
16 premised upon the cost efficiency of the production, transmission and  
17 distribution of large-scale centralized utility generation. However, advances  
18 in distributed generation technologies, such as solar cells, gas  
19 microturbines, battery storage and fuel cells, may make these alternative  
20 generation methods competitive with large-scale utility generation, and  
21 change how customers acquire or use our services. DESC has an exclusive  
22 franchise to serve retail electric customers in its South Carolina service  
23 territory. If regulatory conditions change, DESC's exclusive franchise may  
24 erode.

25 Reduced energy demand or significantly slowed growth in demand due to  
26 customer adoption of energy efficient technology, conservation, distributed  
27 generation, regional economic conditions, or the impact of additional  
28 compliance obligations, unless substantially offset through regulatory cost

1 allocations, could adversely impact the value of DESC's business activities.

2 [DESC 2019 Form 10-K at page 8]

3 **Q. WHY ARE AN ELECTRIC UTILITY'S OPERATING EXPENSES UNCERTAIN?**

4 A. Operating expense uncertainty arises as a result of: (a) high volatility in fuel prices or  
5 interruptions in fuel supply; (b) variability in maintenance costs and the costs of materials;  
6 (c) uncertainty over outages of the company's generation, transmission, and distribution  
7 systems, as well as storm-related expenses; (d) uncertainty regarding the cost of purchased  
8 power and the revenues achieved from off-system sales; (e) the prospect of increasing  
9 employee health care and pension expenses; and (f) the prospect of increased expenses for  
10 security, both physical and cyber.

11 **Q. DOES DESC EXPERIENCE OPERATING EXPENSE UNCERTAINTY?**

12 A. Yes. DESC experiences both the typical operating expense uncertainty associated with its  
13 existing operations and the operating expense uncertainty associated with the future  
14 operations of major plant additions.

15 **Q. WHY ARE UTILITY INVESTMENT COSTS UNCERTAIN?**

16 A. The electric utility business requires large investments in the plant and equipment required  
17 to deliver electricity to customers. The future amounts of required investments in plant and  
18 equipment are uncertain as a result of: (a) demand uncertainty; (b) the changing economics  
19 of alternative generation technologies; (c) uncertainty in environmental regulations and  
20 clean air requirements; (d) uncertainty in the costs of construction materials and labor; and  
21 (e) uncertainty in the amount of additional investments to ensure the reliability of the  
22 company's transmission and distribution networks. Furthermore, the risk of investing in  
23 electric utility facilities is increased by the irreversible nature of the company's investments  
24 in utility plant and equipment. For example, if an electric utility decides to invest in new  
25 distribution plant to serve a new neighborhood, and, as a result of a changing economy,  
26 fewer housing units are built in the neighborhood, the company may not be able to recover  
27 its investment.



1 **Q. YOU NOTE ABOVE THAT HIGH OPERATING LEVERAGE CONTRIBUTES**  
2 **TO THE BUSINESS RISK OF ELECTRIC UTILITIES. WHAT IS OPERATING**  
3 **LEVERAGE?**

4 A. Operating leverage is the increased sensitivity of a company's earnings to sales variability  
5 that occurs when a significant percentage of the company's costs are fixed.

6 **Q. HOW DO ECONOMISTS MEASURE OPERATING LEVERAGE?**

7 A. Economists typically measure operating leverage by the ratio of a company's fixed  
8 expenses to its operating margin (revenues minus variable expenses).

9 **Q. WHAT IS THE DIFFERENCE BETWEEN FIXED AND VARIABLE EXPENSES?**

10 A. Fixed expenses are expenses that do not vary with output (that is, kWh sold), and variable  
11 expenses are expenses that vary directly with output. For electric utilities, fixed expenses  
12 include the capacity component of purchased power costs, the fixed component of  
13 operating and maintenance costs, depreciation and amortization, and taxes. Fuel expenses  
14 are the primary variable cost for electric utilities.

15 **Q. DO ELECTRIC UTILITIES EXPERIENCE HIGH OPERATING LEVERAGE?**

16 A. Yes. As noted above, operating leverage increases when a firm's commitment to fixed  
17 costs rises in relation to its operating margin on sales. The relatively high degree of fixed  
18 costs in the electric utility business arises primarily from: (1) the average electric utility's  
19 large investment in fixed plant and equipment that is depreciated over a long service life;  
20 and (2) the relatively fixed nature of an electric utility's operating and maintenance costs.  
21 High operating leverage causes the average electric utility's operating income to be highly  
22 sensitive to demand and revenue fluctuations.

23 **Q. CAN AN ELECTRIC UTILITY REDUCE ITS OPERATING LEVERAGE BY**  
24 **PURCHASING, RATHER THAN GENERATING, ELECTRICITY?**

25 A. No. Electric utilities generally purchase power under long-term contracts that include both  
26 a fixed capacity charge and a variable charge that depends on the amount of electricity  
27 purchased. Because the fixed capacity charge is designed to recover the seller's fixed costs

1 of generating electricity, electric utilities generally experience the same degree of operating  
2 leverage when they purchase power as when they generate power.

3 **Q. HOW DOES OPERATING LEVERAGE AFFECT A COMPANY'S BUSINESS**  
4 **RISK?**

5 A. Operating leverage affects a company's business risk through its impact on the variability  
6 of the company's profits or income. In general, the higher a company's operating leverage,  
7 the higher is the variability of the company's operating profits.

8 **Q. DOES REGULATION CREATE UNCERTAINTY FOR ELECTRIC UTILITIES?**

9 A. Yes. Rates for electric utility services are generally set by state regulatory authorities in a  
10 manner that provides electric utilities an opportunity to recover prudently-incurred  
11 operating expenses and earn a fair rate of return on their prudently-incurred investment in  
12 property, plant, and equipment. Investors' perceptions of the business and financial risks  
13 of electric utilities are strongly influenced by their views of the quality of regulation.  
14 Investors are aware that regulators in some jurisdictions may be unwilling at times to set  
15 rates that allow companies an opportunity to recover their cost of service in a timely manner  
16 and earn a fair and reasonable return on investment. Investors are also aware that, even if  
17 a company presently has an opportunity to earn a fair return on its investment in property,  
18 plant, and equipment, there is no assurance that they will continue to have such an  
19 opportunity in the future. If investors perceive that regulators may not provide an  
20 opportunity to earn a fair rate of return on investment, investors may demand a higher rate  
21 of return for utilities operating in such jurisdictions. If investors perceive that regulators  
22 are likely to continue to provide an opportunity for a company to earn a fair rate of return  
23 on investment, investors will view the risk of earning a less than fair return as minimal.

24 **Q. YOU NOTE THAT UNCERTAINTY ASSOCIATED WITH THE COSTS OF**  
25 **COMPLYING WITH ENVIRONMENTAL, HEALTH, AND SAFETY LAWS AND**  
26 **REGULATIONS IS A CAUSE OF AN ELECTRIC UTILITY'S INVESTMENT**  
27 **COST UNCERTAINTY. ARE INVESTORS AWARE OF THE RISK THAT DESC**  
28 **MAY FACE INCREASING COSTS OF COMPLYING WITH**  
29 **ENVIRONMENTAL, HEALTH, AND SAFETY LAWS AND REGULATIONS?**

1 A. Yes. The risks to DESC of compliance with current and future environmental laws and  
2 regulations are described in numerous sources, including DESC's 2019 Form 10-K:

3 DESC's operations and construction activities are subject to a number of  
4 environmental laws and regulations which impose significant compliance  
5 costs on DESC. DESC's operations and construction activities are subject  
6 to extensive federal, state and local environmental statutes, rules and  
7 regulations relating to air quality, water quality, waste management, natural  
8 resources, and health and safety. Compliance with these legal requirements  
9 requires DESC to commit significant capital toward permitting, emission  
10 fees, environmental monitoring, installation and operation of environmental  
11 control equipment and purchase of allowances and/or offsets. Additionally,  
12 DESC could be responsible for expenses relating to remediation and  
13 containment obligations, including at sites where it has been identified by a  
14 regulatory agency as a potentially responsible party. Expenditures relating  
15 to environmental compliance have been significant in the past, and DESC  
16 expects that they will remain significant in the future. As a result of these  
17 requirements, certain facilities may become uneconomical to operate and  
18 may need to be shut down, converted to new fuel types or sold.

19 We expect that existing environmental laws and regulations may be revised  
20 and/or new laws may be adopted including regulation of GHG emissions  
21 which could have an impact on DESC's business (risks relating to  
22 regulation of GHG emissions from existing fossil fuel-fired electric  
23 generating units are discussed in more detail below). In addition, further  
24 regulation of air quality and GHG emissions under the CAA have been  
25 imposed on the natural gas sector, including rules to limit methane leakage.  
26 DESC is also subject to federal water and waste regulations, including  
27 regulations concerning cooling water intake structures, coal combustion by-  
28 product handling and disposal practices, wastewater discharges from steam  
29 electric generating stations, management and disposal of hydraulic

1 fracturing fluids and the potential further regulation of polychlorinated  
2 biphenyls.

3 Compliance costs cannot be estimated with certainty due to the inability to  
4 predict the requirements and timing of implementation of any new  
5 environmental rules or regulations. Other factors which affect the ability to  
6 predict future environmental expenditures with certainty include the  
7 difficulty in estimating clean-up costs and quantifying liabilities under  
8 environmental laws that impose joint and several liabilities on all  
9 responsible parties. However, such expenditures, if material, could make  
10 DESC's facilities uneconomical to operate, result in the impairment of  
11 assets, or otherwise adversely affect DESC's results of operations, financial  
12 performance or liquidity. [DESC 2019 Form 10-K at 7]

13 **Q. YOU MENTION THAT DESC'S FINANCIAL PERFORMANCE MAY BE**  
14 **AFFECTED BY THE UNCERTAIN IMPACT OF THE CORONAVIRUS**  
15 **PANDEMIC ON ECONOMIC CONDITIONS AND THE DEMAND FOR**  
16 **ELECTRICITY. ARE DOMINION ENERGY'S INVESTORS ALSO AWARE OF**  
17 **THE UNCERTAINTY ASSOCIATED WITH THE IMPACT OF THE PANDEMIC**  
18 **ON DOMINION ENERGY'S AND THE COMPANY'S FINANCIAL**  
19 **PERFORMANCE?**

20 **A.** Yes. Dominion Energy discusses the potential impact of the pandemic on its consolidated  
21 financial performance in its Form Q-1 2020 filing:

22 Dominion Energy is monitoring the global outbreak of COVID-19 and  
23 taking steps to mitigate the potential risks to Dominion Energy posed by the  
24 spread of the virus. ... This is a rapidly evolving situation, and Dominion  
25 Energy will continue to monitor developments affecting its workforce,  
26 suppliers and other aspects of its business, such as construction projects,  
27 and will take additional precautions as Dominion Energy believes are  
28 warranted. In addition, Dominion Energy continues to monitor both  
29 customer demand and its ability to collect customer receivables. While

1 Dominion Energy currently does not expect a material impact to its results  
2 of operations from the impacts of the COVID-19 pandemic on its  
3 operations, the ultimate impacts on its results of operations, financial  
4 position and/or cash flows could be material based on the ultimate duration  
5 of the pandemic and the related economic recovery. [Dominion Energy  
6 Form 10-Q, March 31, 2020, at 105]

7 **Q. YOU DISCUSS ABOVE THAT A COMPANY INCURS ADDITIONAL RISK**  
8 **WHEN IT FINANCES ITS OPERATIONS WITH FIXED-COST DEBT. IS**  
9 **FINANCING WITH FIXED-COST DEBT REFERRED TO AS FINANCIAL**  
10 **LEVERAGE?**

11 A. Yes.

12 **Q. YOU NOTE THAT FINANCIAL LEVERAGE INCREASES THE RISK OF**  
13 **INVESTING IN ELECTRIC UTILITIES SUCH AS DESC. HOW DO**  
14 **ECONOMISTS MEASURE FINANCIAL LEVERAGE?**

15 A. Economists generally measure financial leverage by the percentages of debt and equity in  
16 a company's market value capital structure. Companies with a high percentage of debt  
17 compared to equity are considered to have high financial leverage.

18 **Q. WHY DOES FINANCIAL LEVERAGE AFFECT THE RISK OF INVESTING IN**  
19 **AN ELECTRIC UTILITY'S STOCK?**

20 A. High financial leverage is a source of additional risk to utility stock investors because it  
21 increases the percentage of the firm's costs that are fixed, and the presence of higher fixed  
22 costs increases the variability of the equity investors' return on investment.

23 **Q. HAS THE RISK ASSOCIATED WITH HIGH FINANCIAL LEVERAGE**  
24 **INCREASED IN RECENT YEARS?**

25 A. Yes. The risk associated with high financial leverage has increased due to the passage of  
26 the 2017 Tax Cuts and Jobs Act ("The Act").

1 **Q. HOW HAS THE ACT AFFECTED THE RISK OF HIGH FINANCIAL**  
2 **LEVERAGE FOR UTILITIES SUCH AS DESC?**

3 A. The Act has increased the risk of high financial leverage for utilities such as DESC because  
4 the lowering of the federal tax rate from 35 percent to 21 percent and the elimination of  
5 bonus depreciation reduce the cash flows available to cover interest and principal payments  
6 on the companies' debt obligations. These changes have a material negative impact on the  
7 companies' projected cash flows in the test year and beyond.

8 **Q. HAVE UTILITIES SUCH AS DESC BEEN TAKING ACTION TO MITIGATE**  
9 **THE NEGATIVE IMPACTS OF THE ACT ON THEIR FINANCIAL RISK?**

10 A. Yes. To mitigate the negative impacts of the Act and to protect customers and the utilities  
11 from the effects of declining cash flows, utilities such as DESC have generally increased  
12 the percentage of equity in their capital structures.

13 **Q. IN YOUR OPINION, IS INCREASING THE PERCENTAGE OF EQUITY IN THE**  
14 **CAPITAL STRUCTURE A REASONABLE OPTION FOR MITIGATING THE**  
15 **IMPACT OF THE ACT ON DESC'S FINANCIAL RISK?**

16 A. Yes. Increasing the percentage of equity in the capital structure is a reasonable option for  
17 DESC to offset the impact of the Act on its financial risk.

18 **Q. WHY IS IT IMPORTANT FOR A UTILITY SUCH AS DESC TO OFFSET THE**  
19 **NEGATIVE IMPACT OF THE ACT ON ITS FINANCIAL RISK?**

20 A. Utilities such as DESC make short-term and long-term investments to serve customers'  
21 needs for safe, reliable, and affordable energy. To best serve customers and have stable and  
22 assured access to capital markets at reasonable costs and terms in all market conditions,  
23 utilities such as DESC must take steps to offset the negative impacts of the Act.

24 **Q. CAN THE RISKS FACING ELECTRIC UTILITIES SUCH AS DESC BE**  
25 **DISTINGUISHED FROM THE RISKS OF INVESTING IN COMPANIES IN**  
26 **OTHER INDUSTRIES?**

27 A. Yes. The risks of investing in electric utilities such as DESC can be distinguished from the  
28 risks of investing in companies in many other industries in several ways. First, the risks of

investing in electric utilities are increased because of the greater capital intensity of the electric energy business and the fact that most investments in electric energy facilities are largely irreversible once they are made. Second, unlike returns in competitive industries, the returns from investment in electric utilities such as DESC are largely asymmetric. That is, it is more likely that the utility will earn less than its required return than that the utility will earn greater than its required return.

## V. COST OF EQUITY ESTIMATION METHODS

### Q. WHAT METHODS DO YOU USE TO ESTIMATE DESC'S COST OF EQUITY?

A. I use several generally accepted methods for estimating the cost of equity for DESC. These are the DCF, the ex ante risk premium, the ex post risk premium, the CAPM, and comparable earnings. The DCF method assumes that the current market price of a firm's stock is equal to the discounted value of all future cash flows equity investors expect to receive from their investment in the company. The ex ante risk premium method assumes that an investor's expectations regarding the equity risk premium can be estimated from data on the DCF expected rate of return on equity compared to the interest rate on long-term bonds. The ex post risk premium method assumes that an investor's expectations regarding the equity-debt return differential are influenced by the historical record of comparable returns on stock and bond investments. The cost of equity under both risk premium methods is then equal to the expected interest rate on bond investments plus the expected risk premium on equity investments such as an ownership interest in DESC. The CAPM assumes that the investor's required rate of return on equity is equal to an expected risk-free rate of interest plus the product of a company-specific risk factor, beta, and the expected risk premium on the market portfolio. The comparable earnings approach estimates investors' required return on equity by calculating the average expected rate of return on book equity for a group of comparable-risk companies.

### A. DISCOUNTED CASH FLOW METHOD

#### Q. PLEASE DESCRIBE THE DCF MODEL.

A. The DCF model is based on the assumption that investors value an asset because they expect to receive a sequence of cash flows from owning the asset. Thus, investors value an

investment in a bond because they expect to receive a sequence of semi-annual coupon payments over the life of the bond and a terminal payment equal to the bond's face value at the time the bond matures. Likewise, investors value an investment in a firm's stock because they expect to receive a sequence of dividend payments and, perhaps, expect to sell the stock at a higher price sometime in the future.

A second fundamental principle of the DCF method is that investors value a dollar received in the future less than a dollar received today. A future dollar is valued less than a current dollar because investors could invest a current dollar in an interest earning account and increase their wealth. This principle is called the time value of money.

Applying the two fundamental DCF principles noted above to an investment in a bond leads to the conclusion that investors value their investment in the bond based on the present value of the bond's future cash flows. Thus, the price of the bond should be equal to:

#### EQUATION 1

$$P_B = \frac{C}{(1+i)} + \frac{C}{(1+i)^2} + \dots + \frac{C+F}{(1+i)^n}$$

Where:

$P_B$  = Bond price;

$C$  = Cash value of the coupon payment (assumed for notational convenience to occur annually rather than semi-annually);

$F$  = Face value of the bond;

$i$  = The rate of interest investors could earn by investing their money in an alternative bond of equal risk; and

$n$  = The number of periods before the bond matures.

Applying these same principles to an investment in a firm's stock suggests that the price of the stock should be equal to:



## EQUATION 2

$$P_s = \frac{D_1}{(1+k)} + \frac{D_2}{(1+k)^2} + \dots + \frac{D_n + P_n}{(1+k)^n}$$

Where:

$P_s$  = Current price of the firm's stock;

$D_1, D_2, \dots, D_n$  = Expected annual dividend per share on the firm's stock;

$P_n$  = Price per share of stock at the time the investor expects to sell the stock; and

$k$  = Return the investor expects to earn on alternative investments of the same risk, i.e., the investor's required rate of return.

Equation (2) is frequently called the annual discounted cash flow model of stock valuation.

Assuming that dividends grow at a constant annual rate,  $g$ , this equation can be solved for  $k$ , the cost of equity. The resulting cost of equity equation is  $k = D_1/P_s + g$ , where  $k$  is the cost of equity,  $D_1$  is the expected next period annual dividend,  $P_s$  is the current price of the stock, and  $g$  is the constant annual growth rate in earnings, dividends, and book value per share. The term  $D_1/P_s$  is called the expected dividend yield component of the annual DCF model, and the term  $g$  is called the expected growth component of the annual DCF model.

**Q. ARE YOU RECOMMENDING THAT THE ANNUAL DCF MODEL BE USED TO ESTIMATE DESC'S COST OF EQUITY?**

A. No. The DCF model assumes that a company's stock price is equal to the present discounted value of all expected future dividends. The annual DCF model is only a correct expression of the present value of future dividends if dividends are paid annually at the end of each year. Because the companies in my comparable group all pay dividends quarterly, the current market price that investors are willing to pay reflects the expected quarterly receipt of dividends. Therefore, a quarterly DCF model should be used to estimate the cost of equity for these firms. The quarterly DCF model differs from the annual DCF model in that it expresses a company's stock price as the present value of a quarterly stream of

dividend payments. A complete analysis of the implications of the quarterly payment of dividends on the DCF model is provided in Exhibit No. \_\_\_\_ (JWV-3). For the reasons cited there, I employed the quarterly DCF model throughout my calculations.

**Q. PLEASE DESCRIBE THE QUARTERLY DCF MODEL YOU USE.**

A. The quarterly DCF model I use is described on Exhibit No. \_\_\_\_ (JWV-3) and in Exhibit No. \_\_\_\_ (JWV-4). The quarterly DCF equation shows that the cost of equity is: the sum of the future expected dividend yield and the growth rate, where the dividend in the dividend yield is the equivalent future value of the four quarterly dividends at the end of the year, and the growth rate is the expected growth in dividends or earnings per share.

**Q. HOW DO YOU ESTIMATE THE QUARTERLY DIVIDEND PAYMENTS IN YOUR QUARTERLY DCF MODEL?**

A. The quarterly DCF model requires an estimate of the dividends,  $d_1$ ,  $d_2$ ,  $d_3$ , and  $d_4$ , investors expect to receive over the next four quarters. I estimate the next four quarterly dividends by multiplying the previous four quarterly dividends by the factor,  $(1 + \text{the growth rate}, g)$ .

**Q. CAN YOU ILLUSTRATE HOW YOU ESTIMATE THE NEXT FOUR QUARTERLY DIVIDENDS WITH DATA FOR A SPECIFIC COMPANY?**

A. Yes. In the case of Alliant Energy, for example, an electric utility company shown in Exhibit No. \_\_\_\_ (JWV-4), the last four quarterly dividends are equal to 0.355, 0.355, 0.38, and 0.38, and the expected growth rate is 5.3 percent. Thus dividends,  $d_1$ ,  $d_2$ ,  $d_3$ , and  $d_4$  are equal to 0.37 and 0.40 [ $0.355 \times (1 + 0.053) = 0.37$ , and  $0.38 \times (1 + 0.053) = 0.40$ ]. (As noted previously, the logic underlying this procedure is described in Exhibit No. \_\_\_\_ (JWV-3).)

**Q. HOW DO YOU ESTIMATE THE GROWTH COMPONENT OF THE QUARTERLY DCF MODEL?**

A. I use the I/B/E/S analysts' estimates of future earnings per share ("EPS") growth reported by Refinitiv (formerly Thomson Reuters).

1 **Q. WHAT ARE THE ANALYSTS' ESTIMATES OF FUTURE EPS GROWTH?**

2 A. As part of their research, financial analysts working at Wall Street firms periodically  
3 estimate EPS growth for each firm they follow. The EPS forecasts for each firm are then  
4 published. Investors who are contemplating purchasing or selling shares in individual  
5 companies review the forecasts. These estimates represent three- to five-year forecasts of  
6 EPS growth.

7 **Q. WHAT IS I/B/E/S?**

8 A. I/B/E/S is a database that reports analysts' EPS growth forecasts for a broad group of  
9 companies. The forecasts are expressed in terms of a mean forecast and a standard  
10 deviation of forecast for each company. Investors use the mean forecast as an estimate of  
11 future company performance.

12 **Q. WHY DO YOU USE THE I/B/E/S GROWTH ESTIMATES?**

13 A. The I/B/E/S growth rates: (1) are widely circulated in the financial community, (2) include  
14 the projections of reputable financial analysts who develop estimates of future EPS growth,  
15 (3) are reported on a timely basis to investors, and (4) are widely used by institutional and  
16 other investors.

17 **Q. WHY DO YOU RELY ON ANALYSTS' PROJECTIONS OF FUTURE EPS**  
18 **GROWTH IN ESTIMATING THE INVESTORS' EXPECTED GROWTH RATE**  
19 **RATHER THAN LOOKING AT PAST HISTORICAL GROWTH RATES?**

20 A. I rely on analysts' projections of future EPS growth because there is considerable empirical  
21 evidence that investors use analysts' forecasts to estimate future earnings growth.

22 **Q. HAVE YOU PERFORMED ANY STUDIES CONCERNING THE USE OF**  
23 **ANALYSTS' FORECASTS AS AN ESTIMATE OF INVESTORS' EXPECTED**  
24 **GROWTH RATE, G?**

25 A. Yes. I prepared a study with Willard T. Carleton, Professor Emeritus of Finance at the  
26 University of Arizona, which is described in a paper entitled "Investor Growth  
27 Expectations: Analysts vs. History," published in *The Journal of Portfolio Management*.

1 **Q. PLEASE SUMMARIZE THE RESULTS OF YOUR STUDY.**

2 A. We performed a correlation analysis to identify the historically-oriented growth rates which  
3 best described a firm's stock price. We then performed a regression study comparing the  
4 historical growth rates and retention growth rates with the average I/B/E/S analysts'  
5 forecasts. In every case, the regression equations containing the average of analysts'  
6 forecasts statistically outperformed the regression equations containing the historical  
7 growth and retention growth estimates. These results are consistent with those found by  
8 Cragg and Malkiel, the early major research in this area (John G. Cragg and Burton G.  
9 Malkiel, Expectations and the Structure of Share Prices, University of Chicago Press).  
10 These results are also consistent with the hypothesis that investors use analysts' forecasts,  
11 rather than historically-oriented growth calculations, in making decisions to buy and sell  
12 stock. The results provide overwhelming evidence that the analysts' forecasts of future  
13 growth are superior to historically-oriented growth measures in predicting a firm's stock  
14 price. I note that researchers at State Street Financial Advisors updated my study, and their  
15 results confirmed that analysts' growth forecasts are superior to historically-oriented  
16 growth measures in predicting a company's stock price.

17 **Q. WHAT PRICE DO YOU USE IN YOUR DCF MODEL?**

18 A. I use a simple average of the monthly high and low stock prices for each firm for the three-  
19 month period ending May 2020. These high and low stock prices were obtained from  
20 Refinitiv.

21 **Q. WHY DO YOU USE THE THREE-MONTH AVERAGE STOCK PRICE IN**  
22 **APPLYING THE DCF METHOD?**

23 A. I use the three-month average stock price in applying the DCF method because stock prices  
24 fluctuate daily, while financial analysts' forecasts for a given company are generally  
25 changed less frequently, often on a quarterly basis. Thus, to match the stock price with an  
26 earnings forecast, it is appropriate to average stock prices over a three-month period.

1 **Q. DO YOU INCLUDE AN ALLOWANCE FOR FLOTATION COSTS IN YOUR DCF**  
2 **ANALYSIS?**

3 A. Yes. I include a 5 percent allowance for flotation costs in my DCF calculations. A complete  
4 explanation of the need for flotation costs is contained in Exhibit No. \_\_\_\_ (JVV-5).

5 **Q. PLEASE EXPLAIN YOUR INCLUSION OF FLOTATION COSTS.**

6 A. All firms that have sold securities in the capital markets have incurred some level of  
7 flotation costs, including the costs of underwriters' commissions, legal fees, and printing  
8 expense, for example. These costs are withheld from the proceeds of the stock sale or are  
9 paid separately and must be recovered over the life of the equity issue. Costs vary  
10 depending upon the size of the issue, the type of registration method used and other factors,  
11 but in general these costs range between three and 5 percent of the proceeds from the issue  
12 [see Inmoo Lee, Scott Lochhead, Jay Ritter, and Quanshui Zhao, "The Costs of Raising  
13 Capital," *The Journal of Financial Research*, Vol. XIX No 1 (Spring 1996), 59-74, and  
14 Clifford W. Smith, "Alternative Methods for Raising Capital," *Journal of Financial*  
15 *Economics* 5 (1977) 273-307]. In addition to these costs, for large equity issues (in relation  
16 to outstanding equity shares), there is likely to be a decline in price associated with the sale  
17 of shares to the public. On average, the decline in price associated with new stock issuances  
18 has been estimated at 2 to 3 percent [see Richard H. Pettway, "The Effects of New Equity  
19 Sales Upon Utility Share Prices," *Public Utilities Fortnightly*, May 10, 1984, 35—39].  
20 Thus, the total flotation cost, including both issuance expense and stock price decline,  
21 generally ranges from 5 to 8 percent of the proceeds of an equity issue. I believe a combined  
22 5 percent allowance for flotation costs is a conservative estimate that should be used in  
23 applying the DCF model in this proceeding.

24 **Q. HOW DO YOU APPLY THE DCF APPROACH TO ESTIMATE THE REQUIRED**  
25 **RETURN ON EQUITY FOR DESC?**

26 A. I apply the DCF approach to the Value Line electric utilities shown in  
27 Exhibit No. \_\_\_\_ (JVV-4).

1 **Q. HOW DO YOU SELECT YOUR ELECTRIC UTILITY COMPANY GROUP?**

2 A. I select all the electric utilities followed by Value Line that: (1) have an investment-grade  
3 bond rating; (2) paid dividends during every quarter of the last two years; (3) did not  
4 decrease dividends during any quarter of the past two years; (4) have a positive I/B/E/S  
5 long-term growth forecast; and (5) are not the subject of a merger offer that has not been  
6 completed. I also note that each of the utilities included in my comparable group has a  
7 Value Line Safety Rank of 1, 2, or 3.

8 **Q. WHY DO YOU ELIMINATE COMPANIES THAT HAVE EITHER DECREASED**  
9 **OR ELIMINATED THEIR DIVIDEND IN THE PAST TWO YEARS?**

10 A. The DCF model requires the assumption that dividends will grow at a constant rate into  
11 the indefinite future. If a company has either decreased or eliminated its dividend in recent  
12 years, the DCF model cannot be used to estimate the cost of equity because the company's  
13 recent dividend experience is inconsistent with this fundamental DCF model assumption.  
14 For example, if the company has eliminated its dividend, there is no dividend input for the  
15 model.

16 **Q. WHY DO YOU ELIMINATE COMPANIES THAT ARE THE SUBJECT OF A**  
17 **MERGER OFFER THAT HAS NOT BEEN COMPLETED?**

18 A. A merger announcement can sometimes have a significant impact on a company's stock  
19 price because of anticipated merger-related cost savings and new market opportunities.  
20 Analysts' growth forecasts, on the other hand, are necessarily related to companies as they  
21 currently exist, and do not reflect investors' views of the potential cost savings and new  
22 market opportunities associated with mergers that have not yet been completed. The use of  
23 a stock price that includes the value of potential mergers in conjunction with growth  
24 forecasts that do not include the growth enhancing prospects of potential mergers may  
25 distort the DCF model result.

26 **Q. PLEASE SUMMARIZE THE RESULTS OF YOUR APPLICATION OF THE DCF**  
27 **MODEL TO YOUR COMPANY GROUP.**

28 A. As shown on Exhibit No. \_\_\_\_ (JVW-4), I obtain an average DCF result of 9.3 percent for  
29 my electric utility group.

**B. RISK PREMIUM METHOD**

**Q. PLEASE DESCRIBE THE RISK PREMIUM METHOD OF ESTIMATING THE COST OF EQUITY.**

A. The risk premium method is based on the principle that investors expect to earn a return on an equity investment that reflects a “premium” over and above the interest rate they expect to earn on an investment in bonds. This equity risk premium compensates equity investors for the additional risk they bear in making equity investments versus bond investments.

**Q. DOES THE RISK PREMIUM APPROACH SPECIFY WHAT DEBT INSTRUMENT SHOULD BE USED TO ESTIMATE THE INTEREST RATE COMPONENT IN THE METHODOLOGY?**

A. No. The risk premium approach can be implemented using virtually any debt instrument. However, the risk premium approach does require that the debt instrument used to estimate the risk premium be the same as the debt instrument used to calculate the interest rate component of the risk premium approach. For example, if the risk premium on equity is calculated by comparing the returns on stocks to the interest rate on A-rated utility bonds, then the interest rate on A-rated utility bonds must be used to estimate the interest rate component of the risk premium approach.

**Q. DOES THE RISK PREMIUM APPROACH REQUIRE THAT THE SAME COMPANIES BE USED TO ESTIMATE THE STOCK RETURN AS ARE USED TO ESTIMATE THE BOND RETURN?**

A. No. For example, many analysts apply the risk premium approach by comparing the return on a portfolio of stocks to the income return on Treasury securities such as long-term Treasury bonds. Clearly, in this widely accepted application of the risk premium approach, the same companies are not used to estimate the stock return as are used to estimate the bond return, since the U.S. government is not a company.

**Q. HOW DO YOU MEASURE THE REQUIRED RISK PREMIUM ON AN EQUITY INVESTMENT IN YOUR GROUP OF PUBLICLY-TRADED ELECTRIC UTILITIES?**

A. I use two methods to estimate the required risk premium on an equity investment in electric utilities. The first is called the *ex ante* risk premium method and the second is called the *ex post* risk premium method.

**1. EX ANTE RISK PREMIUM METHOD**

**Q. PLEASE DESCRIBE YOUR EX ANTE RISK PREMIUM APPROACH FOR MEASURING THE REQUIRED RISK PREMIUM ON AN EQUITY INVESTMENT IN ELECTRIC UTILITIES.**

A. My *ex ante* risk premium method is based on studies of the DCF expected return on a group of electric utilities compared to the interest rate on Moody's A-rated utility bonds. Specifically, for each month in my study period, I calculate the risk premium using the equation,

$$RP_{\text{PROXY}} = DCF_{\text{PROXY}} - I_A$$

where:

$RP_{\text{PROXY}}$  = the required risk premium on an equity investment in the proxy group of companies;

$DCF_{\text{PROXY}}$  = average DCF estimated cost of equity on a portfolio of proxy companies; and

$I_A$  = the yield to maturity on an investment in A-rated utility bonds.

I then perform a regression analysis to determine if there is a relationship between the calculated risk premium and interest rates. Finally, I use the results of the regression analysis to estimate the investors' required risk premium. To estimate the cost of equity, I then add the required risk premium to the forecasted interest rate on A-rated utility bonds. One could use the yield to maturity on other debt investments to measure the interest rate component of the risk premium approach as long as one uses the yield on the same debt investment to measure the expected risk premium component of the risk premium



1 approach. I use the yield on A-rated utility bonds because it is a frequently-used benchmark  
2 for utility bond yields. A detailed description of my *ex ante* risk premium studies is  
3 contained in Exhibit No. \_\_\_\_ (JWV-6), and the underlying DCF results and interest rates  
4 are displayed in Exhibit No. \_\_\_\_ (JWV-7).

5 **Q. WHAT COST OF EQUITY DO YOU OBTAIN FROM YOUR *EX ANTE* RISK**  
6 **PREMIUM METHOD?**

7 A. To estimate the cost of equity using the *ex ante* risk premium method, one may add the  
8 estimated risk premium over the yield on A-rated utility bonds to the forecasted or expected  
9 yield to maturity on A-rated utility bonds. I arrive at the expected yield to maturity on A-  
10 rated utility bonds, 4.43 percent, by averaging forecast data from Value Line and the U.S.  
11 Energy Information Administration (“EIA”). For my electric utility sample, my analyses  
12 produce an estimated risk premium over the expected yield on A-rated utility bonds equal  
13 to 5.64 percent. Adding an estimated risk premium of 5.64 percent to the expected  
14 4.43 percent yield to maturity on A-rated utility bonds produces a cost of equity estimate  
15 of 10.1 percent using the *ex ante* risk premium method.

16 **Q. HOW DO YOU ARRIVE AT THE EXPECTED YIELD ON A-RATED UTILITY**  
17 **BONDS?**

18 A. As noted above, I arrive at the expected yield to maturity on A-rated utility bonds,  
19 4.4 percent, by averaging forecast data from Value Line and the EIA. Value Line Selection  
20 & Opinion (May 29, 2020) projects a AAA-rated Corporate bond yield equal to 3.3 percent.  
21 The average spread between A-rated utility bonds and AAA-rated Corporate bonds is 65  
22 basis points (A-rated utility, 3.14 percent, less AAA-rated Corporate, 2.49 percent, equals  
23 65 basis points). Adding 65 basis points to the 3.3 percent Value Line AAA Corporate  
24 bond forecast equals a forecast yield of 3.95 percent for A-rated utility bonds. The EIA  
25 forecasts a AA-rated utility bond yield equal to 4.66 percent. The spread between AA-rated  
26 utility and A-rated utility bonds is 25 basis points (3.14 percent less 2.89 percent). Adding  
27 25 basis points to EIA’s 4.66 percent AA-utility bond yield forecast equals a forecast yield  
28 for A-rated utility bonds equal to 4.91 percent. The average of the forecasts (3.95 percent  
29 using Value Line data and 4.91 percent using EIA data) is 4.43 percent.

1 **Q. WHY DO YOU USE A FORECASTED YIELD TO MATURITY ON UTILITY**  
2 **BONDS RATHER THAN A CURRENT YIELD TO MATURITY?**

3 A. I use a forecasted yield to maturity on utility bonds rather than a current yield to maturity  
4 because: (1) the fair rate of return standard requires that a company have an opportunity to  
5 earn its required return on its investment during the forward-looking period during which  
6 rates will be in effect; and (2) current interest rates reflect the unprecedented efforts of the  
7 Federal Reserve to preserve liquidity and encourage investment in the face of the economic  
8 crisis caused by the global COVID-19 pandemic. Thus, the use of forecasted interest rates  
9 is consistent with the fair rate of return standard, whereas the use of current interest rates  
10 at this time is not.

11 **2. EX POST RISK PREMIUM METHOD**

12 **Q. PLEASE DESCRIBE YOUR EX POST RISK PREMIUM METHOD FOR**  
13 **MEASURING THE REQUIRED RISK PREMIUM ON AN EQUITY**  
14 **INVESTMENT IN ELECTRIC UTILITIES.**

15 A. I first perform a study of the comparable returns received by bond and stock investors over  
16 the 83 years of my study. I estimate the returns on stock and bond portfolios, using stock  
17 price and dividend yield data on the S&P 500 and bond yield data on Moody's A-rated  
18 utility bonds. My study consists of making an investment of one dollar in the S&P 500 and  
19 Moody's utility bonds at the beginning of 1937, and reinvesting the principal plus return  
20 each year to 2020. The return associated with each stock portfolio is the sum of the annual  
21 dividend yield and capital gain (or loss) which accrued to this portfolio during the year(s)  
22 in which it was held. The return associated with the bond portfolio, on the other hand, is  
23 the sum of the annual coupon yield and capital gain (or loss) which accrued to the bond  
24 portfolio during the year(s) in which it was held. (See Exhibit No. \_\_\_\_ (JWV-8), which  
25 further describes my ex post risk premium method.) The resulting annual returns on the  
26 stock and bond portfolios purchased in each year between 1937 and 2020 are shown on  
27 Exhibit No. \_\_\_\_ (JWV-9). The average annual return on an investment in the S&P 500  
28 stock portfolio is 11.41 percent, while the average annual return on an investment in the

1 Moody's A-rated utility bond portfolio is 6.76 percent. The risk premium on the S&P 500  
2 stock portfolio is, therefore, 4.7 percent.

3 I also conduct a second study using stock data on the S&P Utilities rather than the  
4 S&P 500. As shown on Exhibit No. \_\_\_\_ (JWV-10), the average annual return on the  
5 S&P Utility stock portfolio is 10.74 percent. Thus, the return on the S&P Utility stock  
6 portfolio exceeded the return on the Moody's A-rated utility bond portfolio by 4.0 percent.

7 **Q. WHY IS IT APPROPRIATE TO PERFORM YOUR EX POST RISK PREMIUM**  
8 **ANALYSIS USING BOTH THE S&P 500 AND THE S&P UTILITIES STOCK**  
9 **INDICES?**

10 A. I perform my ex post risk premium analysis on both the S&P 500 and the S&P Utilities  
11 because I believe electric energy companies today face risks that are somewhere in between  
12 the average risk of the S&P Utilities and the S&P 500 over the years 1937 to 2020. Thus,  
13 I use the average of the two historically-based risk premiums as my estimate of the required  
14 risk premium in my ex post risk premium method.

15 **Q. WHY DO YOU BELIEVE ELECTRIC ENERGY COMPANIES TODAY FACE**  
16 **RISKS THAT ARE SOMEWHERE IN BETWEEN THE AVERAGE RISK OF THE**  
17 **S&P UTILITIES AND THE S&P 500 OVER THE YEARS 1937 TO 2020?**

18 A. I believe electric energy companies today face risks that are at least as great as the average  
19 risk of the S&P Utilities and the S&P 500 over the years 1937 to 2020 because the structure  
20 of the electric utility industry is changing rapidly. The basic assumption over most of the  
21 years since 1937 was that electric utilities were natural monopolies that could produce  
22 clean and efficient energy at a lower cost than a competitive electric utility industry.  
23 However, dramatic changes in technologies, laws, and regulations have reduced and could  
24 further reduce the cost of producing electricity from alternative distributed resources. As  
25 these changes evolve, it is increasingly possible that the traditional electric operating  
26 companies will be unable to earn a market-required rate of return on their investments in  
27 generating, transmission, and distribution facilities.

1 **Q. WOULD YOUR STUDY PROVIDE A DIFFERENT RISK PREMIUM IF YOU**  
2 **STARTED WITH A DIFFERENT TIME PERIOD?**

3 A. Yes. The risk premium results vary somewhat depending on the historical time period  
4 chosen. My policy is to use the largest set of reliable historical data. I thought it would be  
5 most meaningful to begin after the passage and implementation of the Public Utility  
6 Holding Company Act of 1935. This Act significantly changed the structure of the public  
7 utility industry. Because the Public Utility Holding Company Act of 1935 was not  
8 implemented until the beginning of 1937, I concluded that data prior to 1937 should not be  
9 used in my study. (The repeal of the 1935 Act has not materially impacted the structure of  
10 the public utility industry; thus, the Act's repeal does not have any impact on my choice of  
11 time period.)

12 **Q. WHY IS IT NECESSARY TO EXAMINE THE YIELD FROM DEBT**  
13 **INVESTMENTS IN ORDER TO DETERMINE THE INVESTORS' REQUIRED**  
14 **RATE OF RETURN ON EQUITY CAPITAL?**

15 A. As previously explained, investors expect to earn a return on their equity investment that  
16 exceeds currently available bond yields because the return on equity, as a residual return,  
17 is less certain than the yield on bonds; and investors must be compensated for this  
18 uncertainty. Investors' expectations concerning the amount by which the return on equity  
19 will exceed the bond yield may be influenced by historical differences in returns to bond  
20 and stock investors. Thus, we can estimate investors' expected returns from an equity  
21 investment from information about past differences between returns on stocks and bonds.  
22 In interpreting this information, investors would also recognize that risk premiums increase  
23 when interest rates are low.

24 **Q. WHAT CONCLUSIONS DO YOU DRAW FROM YOUR EX POST RISK**  
25 **PREMIUM ANALYSES ABOUT THE REQUIRED RETURN ON AN EQUITY**  
26 **INVESTMENT IN ELECTRIC UTILITIES?**

27 A. My studies provide evidence that investors today require an equity return of at least 4.0 to  
28 4.7 percentage points above the expected yield on A-rated utility bonds. As discussed  
29 above, the expected yield on A-rated utility bonds is 4.43 percent. Adding a 4.0 to 4.7

percentage point risk premium to the 4.43 percent yield on A-rated utility bonds, I obtain an expected return on equity in the range 8.4 percent to 9.1 percent with a midpoint estimate equal to 8.8 percent. Adding a 20-basis point allowance for flotation costs, I obtain an estimate of 9.0 percent as the ex post risk premium cost of equity. (I determine the flotation cost allowance by calculating the difference in my DCF results with and without a flotation cost allowance.)

### C. CAPITAL ASSET PRICING MODEL

#### Q. WHAT IS THE CAPM?

A. The CAPM is an equilibrium model of the security markets in which the expected or required return on a given security is equal to the risk-free rate of interest, plus the company equity “beta,” times the market risk premium:

$$\text{Cost of equity} = \text{Risk-free rate} + \text{Equity beta} \times \text{Market risk premium}$$

The risk-free rate in this equation is the expected rate of return on a risk-free government security, the equity beta is a measure of the company’s risk relative to the market as a whole, and the market risk premium is the premium investors require to invest in the market basket of all securities compared to the risk-free security.

#### Q. HOW DO YOU USE THE CAPM TO ESTIMATE THE COST OF EQUITY FOR YOUR PROXY COMPANIES?

A. The CAPM requires an estimate of the risk-free rate, the company-specific risk factor or beta, and the expected return on the market portfolio. For my estimate of the risk-free rate, I use a forecasted yield to maturity on 20-year Treasury bonds of 2.84 percent, obtained using data from Value Line and the United States Energy Information Administration (“EIA”). For my estimate of the company-specific risk, or beta, I use both the current average 0.87 Value Line beta for the Value Line electric utilities and the 0.89 beta estimated from the relationship between the historical risk premium on utilities and the historical risk premium on the market portfolio (see Exhibit No. \_\_\_\_ (JWV-11)). For my estimate of the expected risk premium on the market portfolio, I also use two approaches. First, I estimate the risk premium on the market portfolio using historical risk premium

1 data reported in the 2020 SBBI<sup>®</sup> Yearbook for the years 1926 through 2019. Second, I  
2 estimate the risk premium on the market portfolio from the difference between the DCF  
3 cost of equity for the S&P 500 and the forecasted yield to maturity on 20-year Treasury  
4 bonds.

5 **Q. HOW DO YOU ARRIVE AT THE FORECASTED YIELD TO MATURITY ON 20-**  
6 **YEAR TREASURY BONDS?**

7 A. As noted above, I use data from Value Line and EIA to arrive at a forecasted yield to  
8 maturity on 20-year Treasury bonds. Value Line forecasts a yield on 10-year Treasury  
9 notes equal to 1.5 percent. The spread between the average yield on 10-year Treasury notes  
10 (0.67 percent) and 20-year Treasury bonds (1.12 percent) is 45 basis points. Adding 45  
11 basis points to Value Line's 1.5 percent forecasted yield on 10-year Treasury notes  
12 produces a forecasted yield of 1.95 percent for 20-year Treasury bonds (see Value Line  
13 Investment Survey, Selection & Opinion, May 29, 2020). EIA forecasts a yield of  
14 3.28 percent on 10-year Treasury notes. Adding the 45-basis point spread between 10-year  
15 Treasury notes and 20-year Treasury bonds to the EIA forecast of 3.28 percent for 10-year  
16 Treasury notes produces an EIA forecast for 20-year Treasury bonds equal to 3.73 percent.  
17 The average of the forecasts is 2.84 percent (1.95 percent using Value Line data and  
18 3.73 percent using EIA data).

19 **1. HISTORICAL CAPM**

20 **Q. HOW DO YOU ESTIMATE THE EXPECTED RISK PREMIUM ON THE**  
21 **MARKET PORTFOLIO USING HISTORICAL RISK PREMIUM DATA**  
22 **DEVELOPED BY IBBOTSON<sup>®</sup> SBBI<sup>®</sup>?**

23 A. I estimate the expected risk premium on the market portfolio by calculating the difference  
24 between the arithmetic mean total return on the S&P 500 from 1926 to 2020 (12.1 percent)  
25 and the average income return on 20-year U.S. Treasury bonds over the same period  
26 (4.9 percent). Thus, my historical risk premium method produces a risk premium of  
27 7.2 percent ( $12.1 - 4.9 = 7.2$ ).

1 **Q. WHY DO YOU RECOMMEND THAT THE RISK PREMIUM ON THE MARKET**  
2 **PORTFOLIO BE ESTIMATED USING THE ARITHMETIC MEAN RETURN ON**  
3 **THE S&P 500?**

4 A. I recommend that the risk premium on the market portfolio be estimated using the  
5 arithmetic mean return on the S&P 500 because, for an investment which has an uncertain  
6 outcome, the arithmetic mean is the best historically-based measure of the return investors  
7 expect to receive in the future. A discussion of the importance of using arithmetic mean  
8 returns in the context of CAPM or risk premium studies is contained in Exhibit No. \_\_\_\_  
9 (JVW-12).

10 **Q. WHY DO YOU RECOMMEND THAT THE RISK PREMIUM ON THE MARKET**  
11 **PORTFOLIO BE MEASURED USING THE INCOME RETURN ON 20-YEAR**  
12 **TREASURY BONDS RATHER THAN THE TOTAL RETURN ON THESE**  
13 **BONDS?**

14 A. As discussed above, the CAPM requires an estimate of the risk-free rate of interest. When  
15 Treasury bonds are issued, the income return on the bond is risk free, but the total return,  
16 which includes both income and capital gains or losses, is not. Thus, the income return  
17 should be used in the CAPM because it is only the income return that is risk free.

18 **Q. IS THERE ANY EVIDENCE FROM THE FINANCE LITERATURE THAT THE**  
19 **APPLICATION OF THE HISTORICAL CAPM MAY UNDERESTIMATE THE**  
20 **COST OF EQUITY?**

21 A. Yes. There is substantial evidence that: (1) the historical CAPM tends to underestimate the  
22 cost of equity for companies whose equity beta is less than 1.0; and (2) the CAPM is less  
23 reliable the further the estimated beta is from 1.0.

24 **Q. WHAT IS THE EVIDENCE THAT THE CAPM TENDS TO UNDERESTIMATE**  
25 **THE COST OF EQUITY FOR COMPANIES WITH BETAS LESS THAN 1.0 AND**  
26 **IS LESS RELIABLE THE FURTHER THE ESTIMATED BETA IS FROM 1.0?**

27 A. The original evidence that the unadjusted CAPM tends to underestimate the cost of equity  
28 for companies whose equity beta is less than 1.0 and is less reliable the further the estimated  
29 beta is from 1.0 was presented in a paper by Black, Jensen, and Scholes, "The Capital Asset

Pricing Model: Some Empirical Tests.” Numerous subsequent papers have validated the Black, Jensen, and Scholes findings, including those by Litzenberger and Ramaswamy (1979), Banz (1981), Fama and French (1992), Fama and French (2004), Fama and MacBeth (1973), and Jegadeesh and Titman (1993).

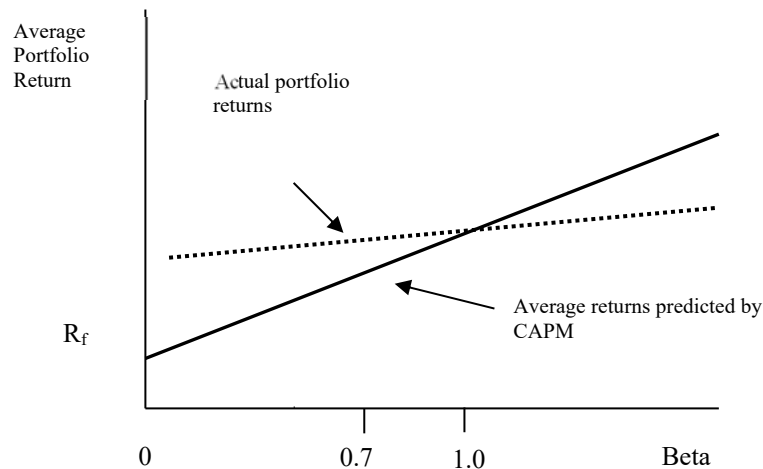
**Q. CAN YOU BRIEFLY SUMMARIZE THESE ARTICLES?**

A. Yes. The CAPM conjectures that security returns increase with increases in security betas in line with the equation:

$$ER_i = R_f + \beta_i [ER_m - R_f]$$

where  $ER_i$  is the expected return on security or portfolio  $i$ ,  $R_f$  is the risk-free rate,  $ER_m - R_f$  is the expected risk premium on the market portfolio, and  $\beta_i$  is a measure of the risk of investing in security or portfolio  $i$  (see **Figure 1** below).

**FIGURE 1  
AVERAGE RETURNS COMPARED TO BETA  
FOR PORTFOLIOS FORMED ON PRIOR BETA**



Financial scholars have studied the relationship between estimated portfolio betas and the achieved returns on the underlying portfolio of securities to test whether the CAPM correctly predicts achieved returns in the marketplace. They find that the relationship between returns and betas is inconsistent with the relationship posited by the CAPM. As described in Fama and French (1992) and Fama and French (2004), the actual relationship



1 between portfolio betas and returns is shown by the dotted line in Figure 1 above. Although  
2 financial scholars disagree on the reasons why the return/beta relationship looks more like  
3 the dotted line in Figure 1 than the solid line, they generally agree that the dotted line lies  
4 above the solid line for portfolios with betas less than 1.0 and below the solid line for  
5 portfolios with betas greater than 1.0. Thus, in practice, scholars generally agree that the  
6 CAPM underestimates portfolio returns for companies with betas less than 1.0, and  
7 overestimates portfolio returns for portfolios with betas greater than 1.0.

8 **Q. WHAT HISTORICAL CAPM RESULT DO YOU OBTAIN WHEN YOU**  
9 **ESTIMATE THE EXPECTED RISK PREMIUM ON THE MARKET PORTFOLIO**  
10 **FROM THE ARITHMETIC MEAN DIFFERENCE BETWEEN THE RETURN ON**  
11 **THE MARKET AND THE YIELD ON 20-YEAR TREASURY BONDS?**

12 A. Using a risk-free rate equal to 2.84 percent, an electric utility beta equal to 0.87, a risk  
13 premium on the market portfolio equal to 7.2 percent, and a flotation cost allowance equal  
14 to 20 basis points, I obtain an historical CAPM estimate of the cost of equity equal to  
15 9.3 percent for my electric utility group  $[2.84 + (0.87 \times 7.2) + 0.20 = 9.3]$  (see  
16 Exhibit No. \_\_\_\_ (J VW-13).

17 **Q. WHAT HISTORICAL CAPM RESULT DO YOU OBTAIN WHEN YOU USE AN**  
18 **ELECTRIC UTILITY BETA EQUAL TO 0.89?**

19 A. I obtain an historical CAPM result equal to 9.5 percent using a risk free rate equal to  
20 2.84 percent, a beta equal to 0.89, the historical market risk premium equal to 7.2 percent,  
21 and a flotation cost allowance of 20 basis points  $(2.84 + 0.89 \times 7.2 + 0.20 = 9.5)$ . (See  
22 Exhibit No. \_\_\_\_ (J VW-13).

23 **Q. WHAT IS THE AVERAGE OF YOUR TWO HISTORICAL CAPM RESULTS?**

24 A. The average of my two historical CAPM results is 9.4 percent  $((9.3 \text{ percent} + 9.5 \text{ percent})$   
25  $\div 2 = 9.4 \text{ percent})$ . I use 9.4 percent as my estimate of the historical CAPM cost of equity.

1           **2.       FORWARD-LOOKING CAPM**

2   **Q.       HOW DOES YOUR FORWARD-LOOKING CAPM DIFFER FROM YOUR**  
3   **HISTORICAL CAPM?**

4   A.       As noted above, my forward-looking CAPM differs from my historical CAPM only in the  
5           method I use to estimate the risk premium on the market portfolio. In the historical CAPM,  
6           I use historical risk premium data to estimate the risk premium on the market portfolio. In  
7           the forward-looking CAPM, I estimate the risk premium on the market portfolio from the  
8           difference between the DCF cost of equity for the S&P 500 and the forecasted yield to  
9           maturity on 20-year Treasury bonds.

10 **Q.       WHAT RISK PREMIUM DO YOU OBTAIN WHEN YOU CALCULATE THE**  
11 **DIFFERENCE BETWEEN THE DCF-RETURN ON THE S&P 500 AND THE**  
12 **RISK-FREE RATE?**

13 A.       Using this method, I obtain a risk premium on the market portfolio equal to 8.7 percent  
14           ((11.5 percent DCF for the S&P 500) – (2.8 percent (risk-free rate) = 8.7)). (See  
15           Exhibit No. \_\_\_\_ (JWV-14).

16 **Q.       WHAT CAPM RESULT DO YOU OBTAIN WHEN YOU ESTIMATE THE**  
17 **EXPECTED RETURN ON THE MARKET PORTFOLIO BY APPLYING THE**  
18 **DCF MODEL TO THE S&P 500?**

19 A.       Using a risk-free rate of 2.8 percent, an electric utility beta of 0.87, a risk premium on the  
20           market portfolio of 8.7 percent, and a flotation cost allowance of 20 basis points, I obtain  
21           a forward-looking CAPM result of 10.6 percent for my electric utility group. (See  
22           Exhibit No. \_\_\_\_ (JWV-14). Using a risk-free rate of 2.8 percent, an electric utility beta of  
23           0.89, a risk premium on the market portfolio of 8.7 percent, and a flotation cost allowance  
24           of 20 basis points, I obtain a forward-looking CAPM result of 10.8 percent for my electric  
25           utility group. (See Exhibit No. \_\_\_\_ (JWV-14). The average of my two forward-looking  
26           CAPM results is 10.7 percent  $((10.6 \text{ percent} + 10.8 \text{ percent}) \div 2 = 10.7 \text{ percent})$ ). I use  
27           10.7 percent as my estimate of the forward-looking CAPM cost of equity.

**D. COMPARABLE EARNINGS METHOD**

**Q. WHAT IS THE COMPARABLE EARNINGS METHOD FOR ESTIMATING THE REQUIRED RATE OF RETURN ON EQUITY?**

A. The comparable earnings method estimates the required rate of return on equity by calculating the expected rate of return on book equity for a group of comparable risk companies. The United States Supreme Court states in the *Hope Natural Gas* case that the “return to the equity owner should be commensurate with returns on investments in other enterprises having corresponding risks.” [*Federal Power Comm’n v. Hope Natural Gas Co.*, 320 U.S. 591, 603 (1944).] The comparable earnings approach implements the *Hope* standard by calculating the expected rate of return on equity for a group of comparable-risk companies.

**Q. WHAT COMPARABLE RISK COMPANIES DO YOU USE TO ESTIMATE DESC’S REQUIRED RATE OF RETURN ON EQUITY USING THE COMPARABLE EARNINGS METHOD?**

A. I use the Value Line electric utilities to estimate DESC’s cost of equity using the comparable earnings method.

**Q. HOW DO YOU CALCULATE THE EXPECTED RATE OF RETURN ON BOOK EQUITY FOR THESE COMPARABLE-RISK ELECTRIC UTILITIES?**

A. I estimate the expected rate of return on book equity for each company by calculating the average expected rate of return on book equity reported by the Value Line Investment Survey for the years 2020 and 2023 – 2025.

**Q. DO YOU MAKE ANY ADJUSTMENTS TO VALUE LINE’S REPORTED EXPECTED RATES OF RETURN ON BOOK EQUITY?**

A. Yes. Value Line calculates its expected rates of return on book equity by dividing each company’s expected earnings by its estimate of the company’s year-end equity. Because a rate of return based on year-end equity understates the rate of return on the average equity investment during the year, I adjust Value Line’s estimates to reflect expected rates of return on average equity for the year. My method for calculating the expected rate of return

1 on average book equity for the comparable companies is described in the notes  
2 accompanying my exhibit.

3 **Q. WHAT AVERAGE EXPECTED RATE OF RETURN ON BOOK EQUITY DO**  
4 **YOU OBTAIN FOR YOUR GROUP OF COMPARABLE-RISK UTILITIES?**

5 A. The average expected rate of return on book equity for this large group of comparable-risk  
6 utilities is 10.1 percent (see Exhibit No. \_\_\_\_ (JWV-15)).

7 **VI. RECOMMENDED RATE OF RETURN ON EQUITY**

8 **Q. WHAT IS THE FAIR RATE OF RETURN ON EQUITY?**

9 A. As discussed above, the fair rate of return on equity is a forward-looking return on equity  
10 that provides the regulated company with an opportunity to earn a return on its equity  
11 investment over the period in which rates are in effect that is commensurate with returns  
12 that investors expect to earn on other equity investments of similar risk. Because the fair  
13 rate of return on equity is a forward-looking return, the estimate of the fair rate of return  
14 on equity requires consideration of investors' expectations for a reasonably long period  
15 into the future.

16 **Q. BASED ON YOUR APPLICATION OF SEVERAL COST OF EQUITY METHODS**  
17 **TO YOUR PROXY ELECTRIC UTILITIES, WHAT IS YOUR CONCLUSION**  
18 **REGARDING THE MARKET COST OF EQUITY FOR YOUR COMPARABLE**  
19 **ELECTRIC UTILITY GROUP?**

20 A. Based on my application of several cost of equity methods, I conclude that the market cost  
21 of equity for my comparable electric utility group is in the range 9.0 percent to  
22 10.7 percent, with an average equal to 9.8 percent (see TABLE 1).

**TABLE 1**  
**COST OF EQUITY MODEL RESULTS**

COST OF EQUITY MODEL	MODEL RESULT
Discounted Cash Flow	9.3%
Ex Ante Risk Premium	10.1%
Ex Post Risk Premium	9.0%
CAPM – Historical	9.4%
CAPM – Forward looking	10.7%
Comparable Earnings	10.1%
Average	9.8%

**Q. DOES YOUR 9.8 PERCENT AVERAGE ESTIMATE OF THE MARKET COST OF EQUITY FOR YOUR COMPARABLE COMPANY GROUP DEPEND ON THE PERCENTAGES OF DEBT AND EQUITY IN THE COMPARABLE COMPANY GROUP'S AVERAGE MARKET VALUE CAPITAL STRUCTURE?**

A. Yes. My 9.8 percent cost of equity conclusion reflects the financial risk associated with the average market value capital structure of my proxy utility group, which has approximately 60 percent equity. I have also examined the average market value capital structure of the Value Line electric utilities over the last five years, and I find that the average market value capital structure of the Value Line electric utilities over this period contains approximately 63 percent equity. (See Exhibit No. \_\_\_\_ (JVW-16).

**Q. WHY DOES THE AVERAGE 9.8 PERCENT MARKET COST OF EQUITY RESULT FOR YOUR PROXY ELECTRIC UTILITY GROUP REFLECT THE FINANCIAL RISK ASSOCIATED WITH THE GROUP'S AVERAGE MARKET VALUE CAPITAL STRUCTURE RATHER THAN THE GROUP'S AVERAGE BOOK VALUE CAPITAL STRUCTURE?**

A. The average 9.8 percent market cost of equity for my proxy utility group reflects the financial risk associated with the group's average market value capital structure because the variability or variance of the equity investor's expected return on equity in the marketplace depends on the group's market value equity percentage, not the group's book value equity percentage.

1 **Q. WHY DOES THE VARIABILITY OF THE RETURN ON EQUITY DEPEND ON**  
2 **MARKET VALUES RATHER THAN BOOK VALUES?**

3 A. The variability of the return on equity depends on the market value of equity because the  
4 equity investor can only buy or sell stocks at market values.

5 **Q. DO FINANCIAL SCHOLARS GENERALLY RECOGNIZE THAT THE**  
6 **VARIABILITY OF THE EXPECTED MARKET RETURN ON AN EQUITY**  
7 **INVESTMENT DEPENDS ON THE MARKET VALUES OF EQUITY IN A**  
8 **COMPANY'S CAPITAL STRUCTURE, NOT THE BOOK VALUES?**

9 A. Yes. In the many years that I taught and performed research on financial economics, I have  
10 never seen a financial text that asserts that the financial risk of investing in a company's  
11 equity depends on the book value of equity in the company's capital structure.

12 **Q. WHAT CAPITAL STRUCTURE IS DESC RECOMMENDING IN THIS**  
13 **PROCEEDING FOR THE PURPOSE OF RATE MAKING?**

14 A. In accord with typical regulatory practice, DESC is recommending that its book value  
15 capital structure containing 46.65 percent debt and 53.35 percent common equity be used  
16 for rate making purposes in this proceeding.

17 **Q. HOW DOES THE FINANCIAL RISK REFLECTED IN DESC'S**  
18 **RECOMMENDED BOOK VALUE RATE MAKING CAPITAL STRUCTURE IN**  
19 **THIS PROCEEDING COMPARE TO THE FINANCIAL RISK REFLECTED IN**  
20 **THE MARKET COST OF EQUITY ESTIMATES FOR YOUR PROXY**  
21 **COMPANIES?**

22 A. Although DESC's recommended book value capital structure contains an appropriate mix  
23 of debt and equity and is a reasonable capital structure for rate making purposes in this  
24 proceeding, the Company's recommended book value rate making capital structure  
25 encompasses greater financial risk than is reflected in my market cost of equity estimates  
26 for my proxy companies.

1 **Q. YOU DISCUSS ABOVE THAT THE MARKET COST OF EQUITY DEPENDS ON**  
2 **A COMPANY'S MARKET VALUE CAPITAL STRUCTURE. IS THERE A WAY**  
3 **TO ADJUST THE 9.8 PERCENT MARKET COST OF EQUITY ESTIMATE FOR**  
4 **YOUR PROXY COMPANY GROUP TO REFLECT THE HIGHER FINANCIAL**  
5 **RISK OF DESC'S BOOK VALUE RATE MAKING CAPITAL STRUCTURE?**

6 A. Yes. Because my proxy group is similar in risk to DESC, DESC should have the same  
7 weighted average cost of capital as my proxy utility group. One may easily determine the  
8 cost of equity required to have the same weighted average cost of capital as my proxy  
9 utility group.

10 **Q. DO YOU PERFORM SUCH A CALCULATION?**

11 A. Yes. As I explained earlier in my testimony, I adjust the 9.8 percent average cost of equity  
12 for my proxy group by recognizing that to attract capital, DESC must have the same  
13 weighted average cost of capital as my proxy group. My analysis indicates that DESC  
14 requires an allowed rate of return on book equity equal to 10.4 percent to have an  
15 opportunity to earn the 9.8 percent required return on the market value of equity. (See  
16 Exhibit No. \_\_\_\_ (JWV-2), page 1).

17 **Q. YOUR ANALYSIS DEMONSTRATES THAT THE COMPANY REQUIRES A**  
18 **10.4 PERCENT ALLOWED RATE OF RETURN ON BOOK EQUITY IN ORDER**  
19 **TO HAVE AN OPPORTUNITY TO EARN ITS 9.8 PERCENT MARKET-**  
20 **REQUIRED RETURN ON EQUITY. UNDERSTANDING THAT MARKET**  
21 **VALUES OF EQUITY CHANGE AS MARKET CONDITIONS CHANGE, HAVE**  
22 **YOU ALSO CALCULATED THE REQUIRED RATES OF RETURN ON BOOK**  
23 **EQUITY IF MARKET VALUE CAPITAL STRUCTURES CONTAIN EITHER**  
24 **LOWER OR HIGHER EQUITY PERCENTAGES?**

25 A. Yes. I also calculate the required return on book equity based on market value capital  
26 structures containing 58 percent equity and 62 percent equity. To earn its 9.8 percent  
27 market-required rate of return on equity when the market equity ratio is 58 percent, the  
28 Company would need a 10.2 percent allowed return on its 53.35 percent book value equity  
29 ratio (see Exhibit No. \_\_\_\_ (JWV-2), page 2). To earn its 9.8 percent market-required rate

1 of return on equity when the market equity ratio is 62 percent, the Company would need a  
2 10.6 percent allowed return on its 53.35 percent book value equity ratio (see  
3 Exhibit No. \_\_\_\_ (JWV-2), page 3). Thus, for market equity ratios in the range 58 percent  
4 to 62 percent, the Company's required allowed return on book equity is in the range  
5 10.2 percent to 10.6 percent.

6 **Q. YOU NOTE ABOVE THAT THE 10.2 PERCENT TO 10.6 PERCENT EQUITY**  
7 **RANGE IS BASED ON MARKET VALUE EQUITY RATIOS IN THE RANGE**  
8 **58 PERCENT TO 62 PERCENT. IS THERE ANY REASON TO BELIEVE THAT**  
9 **YOUR USE OF MARKET VALUE EQUITY RATIOS IN THE RANGE**  
10 **58 PERCENT TO 62 PERCENT IS CONSERVATIVE?**

11 A. Yes. The average market value equity ratio for the years 2015 through 2019 is 63 percent  
12 (see Exhibit No. \_\_\_\_ (JWV-16), which is higher than my 58 percent to 62 percent range.

13 **Q. WHAT FAIR RATE OF RETURN ON COMMON EQUITY DO YOU**  
14 **RECOMMEND FOR DESC?**

15 A. I recommend a fair rate of return on common equity for DESC equal to 10.4 percent.

16 **Q. DOES THIS CONCLUDE YOUR PRE-FILED DIRECT TESTIMONY?**

A. Yes, it does.



**QUALIFICATIONS OF JAMES H. VANDER WEIDE, PH.D.**

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James H. Vander Weide is President of Financial Strategy Associates, a consulting firm that provides financial and economic consulting services, including cost of capital and valuation studies, to corporate clients. Dr. Vander Weide holds a Ph.D. in Finance from Northwestern University and a Bachelor of Arts in Economics from Cornell University. After receiving his Ph.D. in Finance, Dr. Vander Weide joined the faculty at Duke University, the Fuqua School of Business, and was named Assistant Professor, Associate Professor, Professor, and then Research Professor of Finance and Economics.

As a Professor at Duke University and the Fuqua School of Business, Dr. Vander Weide has published research in the areas of finance and economics and taught courses in corporate finance, investment management, management of financial institutions, statistics, economics, operations research, and the theory of public utility pricing. Dr. Vander Weide has been active in executive education at Duke and Duke Corporate Education, leading executive development seminars on topics including financial analysis, cost of capital, creating shareholder value, mergers and acquisitions, capital budgeting, measuring corporate performance, and valuation. In addition, Dr. Vander Weide designed and served as Program Director for several executive education programs, including the Advanced Management Program, Competitive Strategies in Telecommunications, and the Duke Program for Manager Development for managers from the former Soviet Union. He is now retired from his teaching responsibilities at Duke.

As an expert financial economist and industry expert, Dr. Vander Weide has participated in more than five hundred regulatory and legal proceedings, appearing in United States courts and federal and state or provincial proceedings in the United States and Canada. He has testified as an expert witness on the cost of capital, competition, risk, incentive regulation, forward-looking economic cost, economic pricing guidelines, valuation, and other financial and economic issues. His clients include investor-owned electric, gas, and water utilities, natural gas pipelines, oil pipelines, telecommunications companies, and insurance companies.

Publications

Dr. Vander Weide has written research papers on such topics as portfolio management, capital budgeting, investments, the effect of regulation on the performance of public utilities, and cash management. His articles have been published in *American Economic Review*, *Journal of Finance*, *Journal of Financial and Quantitative Analysis*, *Management Science*, *Financial Management*, *Journal of Portfolio Management*, *International Journal of Industrial Organization*, *Journal of Bank Research*, *Journal of Accounting Research*, *Journal of Cash Management*, *Atlantic Economic Journal*, *Journal of Economics and Business*, and *Computers and Operations Research*. He has written a book entitled *Managing Corporate Liquidity: An Introduction to Working Capital Management* published by John Wiley and Sons, Inc.; and he has written a chapter titled "Financial Management in the Short Run" for *The Handbook of Modern Finance*, and a chapter titled "Principles for Lifetime Portfolio Selection: Lessons from Portfolio Theory" for *The Handbook of Portfolio Construction: Contemporary Applications of Markowitz Techniques*. *The Handbook of Portfolio Construction* is a peer-reviewed collection of research papers by notable scholars on portfolio optimization, published in 2010 in honor of Nobel Prize winner Harry Markowitz.

Professional Consulting Experience

Dr. Vander Weide has provided financial and economic consulting services to firms in the electric, gas, insurance, oil and gas pipeline, telecommunications, and water industries for more than thirty years. He has testified on the cost of capital, competition, risk, incentive regulation, forward-looking economic cost, economic pricing guidelines, valuation, and other financial and economic issues in more than five hundred cases before the Federal Energy Regulatory Commission, the National Energy Board (Canada), the Federal Communications Commission, the Canadian Radio-Television and Telecommunications Commission, the National Telecommunications and Information Administration, the United States Tax Court, the public service commissions of forty-five states and the District of Columbia, four Canadian provinces, the insurance commissions of five states, the Iowa State Board of Tax Review, and the North Carolina Property Tax Commission. In addition, he has testified as an expert witness in proceedings before numerous federal district courts, including the United States District Court for the District of Nebraska; the United States District Court for the District of New Hampshire; the United States District Court for the District of Northern Illinois; the United States District Court for the Eastern District of North Carolina; the Montana Second Judicial District Court, Silver Bow County; the United States District Court for the Northern District of California; the Superior Court, North Carolina; the United States Bankruptcy Court for the Southern District of West Virginia; the United States District Court for the Eastern District of Michigan; and the Supreme Court of the State of New York. Dr. Vander Weide testified in thirty states on issues relating to the pricing of unbundled network elements and universal service cost studies and consulted with Bell Canada, Deutsche Telekom, and Telefónica on similar issues. Dr. Vander Weide has provided consulting and expert witness testimony to the following companies:

<b>ELECTRIC, GAS, PIPELINE, WATER COMPANIES</b>	
Alcoa Power Generating, Inc.	MidAmerican Energy and subsidiaries
Alliant Energy and subsidiaries	National Fuel Gas
AltaLink, L.P.	Nevada Power Company
Ameren	Newfoundland Power Inc.
American Water Works	NICOR
Atmos Energy and subsidiaries	North Carolina Natural Gas
BP p.l.c.	North Shore Gas
Buckeye Partners, L.P.	Northern Natural Gas Company
Central Illinois Public Service	NOVA Gas Transmission Ltd.
Citizens Utilities	PacifiCorp
Consolidated Edison and subsidiaries	Peoples Energy and its subsidiaries
Consolidated Natural Gas and subsidiaries	PG&E
Dominion Resources and subsidiaries	Plains All American Pipeline, L.P.
Duke Energy and subsidiaries	Progress Energy and subsidiaries
Empire District Electric and subsidiaries	PSE&G
EPCOR Distribution & Transmission Inc.	Public Service Company of North Carolina
EPCOR Energy Alberta Inc.	Sempra Energy/San Diego Gas and Electric
FortisAlberta Inc.	South Carolina Electric and Gas
FortisBC Utilities	Southern Company and subsidiaries
Hope Natural Gas	Spectra Energy
Iberdrola Renewables	Tennessee-American Water Company
Interstate Power Company	The Peoples Gas, Light and Coke Co.

ELECTRIC, GAS, PIPELINE, WATER COMPANIES	
Iowa Southern	Trans Québec & Maritimes Pipeline Inc.
Iowa-American Water Company	TransCanada
Iowa-Illinois Gas and Electric	Union Gas
Kentucky Power Company	United Cities Gas Company
Kentucky-American Water Company	Virginia-American Water Company
Kinder Morgan Energy Partners	West Virginia-American Water Company
Liberty Utilities	Westcoast Energy Inc.
Maritimes & Northeast Pipeline	Wisconsin Energy Corporation
	Xcel Energy

TELECOMMUNICATIONS COMPANIES	
ALLTEL and subsidiaries	Phillips County Cooperative Tel. Co.
Ameritech (now AT&T new)	Pine Drive Cooperative Telephone Co.
AT&T (old)	Roseville Telephone Company (SureWest)
Bell Canada/Nortel	SBC Communications (now AT&T new)
BellSouth and subsidiaries	Sherburne Telephone Company
Centel and subsidiaries	Siemens
Cincinnati Bell (Broadwing)	Southern New England Telephone
Cisco Systems	Sprint/United and subsidiaries
Citizens Telephone Company	Telefónica
Concord Telephone Company	Tellabs, Inc.
Contel and subsidiaries	The Stentor Companies
Deutsche Telekom	U S West (Qwest)
GTE and subsidiaries (now Verizon)	Union Telephone Company
Heins Telephone Company	United States Telephone Association
JDS Uniphase	Valor Telecommunications (Windstream)
Lucent Technologies	Verizon (Bell Atlantic) and subsidiaries
Minnesota Independent Equal Access Corp.	Woodbury Telephone Company
NYNEX and subsidiaries (Verizon)	
Pacific Telesis and subsidiaries	

INSURANCE COMPANIES
Allstate
North Carolina Rate Bureau
United Services Automobile Association (USAA)
The Travelers Indemnity Company
Gulf Insurance Company

Other Professional Experience

Dr. Vander Weide has conducted in-house seminars and training sessions on topics such as creating shareholder value, financial analysis, competitive strategy, cost of capital, real options, financial strategy, managing growth, mergers and acquisitions, valuation, measuring corporate performance, capital budgeting, cash management, and financial planning. Among the firms for whom he has designed and taught tailored programs and training sessions are ABB Asea Brown Boveri, Accenture, Allstate, Ameritech, AT&T, Bell Atlantic/Verizon, BellSouth, Progress Energy/Carolina Power & Light, Contel, Fisons, GlaxoSmithKline, GTE, Lafarge, MidAmerican Energy, New Century Energies, Norfolk Southern, Pacific Bell Telephone, The Rank Group, Siemens, Southern New England Telephone, TRW, and Wolseley Plc. Dr. Vander Weide has also hosted a nationally prominent conference/workshop on estimating the cost of capital. In 1989, at the request of Mr. Fuqua, Dr. Vander Weide designed the Duke Program for Manager Development for managers from the former Soviet Union, the first in the United States designed exclusively for managers from Russia and the former Soviet republics.

Early in his career, Dr. Vander Weide helped found University Analytics, Inc., one of the fastest growing small firms in the country at that time. As an officer at University Analytics, he designed cash management models, databases, and software used by most major U.S. banks in consulting with their corporate clients. Having sold his interest in University Analytics, Dr. Vander Weide now concentrates on strategic and financial consulting, academic research, and executive education.

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**JAMES H. VANDER WEIDE**

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**CALCULATION OF REQUIRED RETURN ON BOOK EQUITY  
MARKET VALUE EQUITY RATIO EQUAL TO 60 PERCENT**

<b>Market Weighted Average Cost of Capital</b>			
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Total Debt	40%	5.10%	2.04%
Common Equity	60%	9.8%	5.88%
Total	100%		7.92%
<b>Weighted Cost of Debt</b>			
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Long-term Debt	46.65%	5.10%	2.38%
<b>Cost of Equity Required to Achieve Equivalent WACC</b>			
(1) Market Weighted Cost of Capital	7.92%		
(2) Weighted Cost of Long-term Debt	2.38%		
(1) Less (2)	5.54%		
Cost of Equity ( $5.54 \div 53.35\% = 10.4\%$ )	10.4%		
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Long-term Debt	46.65%	5.10%	2.38%
Common Equity	53.35%	10.4%	5.54%
Total	100%		7.92%
Notes:			
	Before-tax Cost	After-tax Cost	Source
Tax rate	21%		
Long-term debt cost rate	6.46%	5.10%	Company
Cost of equity	9.8%		Cost of equity proxy group
Adjusted cost of equity:	10.4%		

**CALCULATION OF REQUIRED RETURN ON BOOK EQUITY  
MARKET VALUE EQUITY RATIO EQUAL TO 58 PERCENT**

<b>Market Weighted Average Cost of Capital</b>			
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Total Debt	42%	5.10%	2.14%
Common Equity	58%	9.8%	5.68%
Total	100%		7.83%
<b>Weighted Cost of Debt</b>			
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Long-term Debt	46.65%	5.10%	2.38%
<b>Cost of Equity Required to Achieve Equivalent WACC</b>			
(1) Market Weighted Cost of Capital	7.83%		
(2) Weighted Cost of Long-term Debt	2.38%		
(1) Less (2)	5.45%		
Cost of Equity ( $5.45 \div 53.35\% = 10.2\%$ )	10.2%		
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Long-term Debt	46.65%	5.10%	2.38%
Common Equity	53.35%	10.2%	5.45%
Total	100%		7.83%
Notes:			
	Before-tax Cost	After-tax Cost	Source
Tax rate	21%		
Long-term debt cost rate	6.46%	5.10%	Company
Cost of equity	9.8%		Cost of equity proxy group
Adjusted cost of equity:	10.2%		



**CALCULATION OF REQUIRED RETURN ON BOOK EQUITY  
MARKET VALUE EQUITY RATIO EQUAL TO 62 PERCENT**

<b>Market Weighted Average Cost of Capital</b>			
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Total Debt	38%	5.10%	1.94%
Common Equity	62%	9.8%	6.08%
Total	100%		8.02%
<b>Weighted Cost of Debt</b>			
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Long-term Debt	46.65%	5.10%	2.38%
<b>Cost of Equity Required to Achieve Equivalent WACC</b>			
(1) Market Weighted Cost of Capital	8.02%		
(2) Weighted Cost of Long-term Debt	2.38%		
(1) Less (2)	5.63%		
Cost of Equity ( $5.63 \div 53.35\% = 10.6\%$ )	10.6%		
Capital Source	% of Total	After-tax Cost Rate	Weighted Cost
Long-term Debt	46.65%	5.10%	2.38%
Common Equity	53.35%	10.6%	5.63%
Total	100%		8.02%
Notes:			
	Before-tax Cost	After-tax Cost	Source
Tax rate	21%		
Long-term debt cost rate	6.46%	5.10%	Company
Cost of equity	9.8%		Cost of equity proxy group
Adjusted cost of equity:	10.6%		

### DERIVATION OF THE QUARTERLY DCF MODEL

The simple DCF Model assumes that a firm pays dividends only at the end of each year. Since firms in fact pay dividends quarterly and investors appreciate the time value of money, the annual version of the DCF Model generally underestimates the value investors are willing to place on the firm's expected future dividend stream. In these workpapers, we review two alternative formulations of the DCF Model that allow for the quarterly payment of dividends.

When dividends are assumed to be paid annually, the DCF Model suggests that the current price of the firm's stock is given by the expression:

$$P_0 = \frac{D_1}{(1+k)} + \frac{D_2}{(1+k)^2} + \dots + \frac{D_n + P_n}{(1+k)^n} \quad (1)$$

where

$P_0$	=	current price per share of the firm's stock,
$D_1, D_2, \dots, D_n$	=	expected annual dividends per share on the firm's stock,
$P_n$	=	price per share of stock at the time investors expect to sell the stock, and
$k$	=	return investors expect to earn on alternative investments of the same risk, i.e., the investors' required rate of return.

Unfortunately, expression (1) is rather difficult to analyze, especially for the purpose of estimating  $k$ . Thus, most analysts make several simplifying assumptions. First, they assume that dividends are expected to grow at the constant rate  $g$  into the indefinite future. Second, they assume that the stock price at time  $n$  is simply the present value of all dividends expected in periods subsequent to  $n$ . Third, they assume that the investors' required rate of return,  $k$ , exceeds the expected dividend growth rate  $g$ . Under the above simplifying assumptions, a firm's stock price may be written as the following sum:

$$P_0 = \frac{D_0(1+g)}{(1+k)} + \frac{D_0(1+g)^2}{(1+k)^2} + \frac{D_0(1+g)^3}{(1+k)^3} + \dots, \quad (2)$$

where the three dots indicate that the sum continues indefinitely.

As we shall demonstrate shortly, this sum may be simplified to:

$$P_0 = \frac{D_0(1+g)}{(k-g)}$$

First, however, we need to review the very useful concept of a geometric progression.

### Geometric Progression

Consider the sequence of numbers 3, 6, 12, 24,..., where each number after the first is obtained by multiplying the preceding number by the factor 2. Obviously, this sequence of numbers may also be expressed as the sequence  $3, 3 \times 2, 3 \times 2^2, 3 \times 2^3$ , etc. This sequence is an example of a geometric progression.

Definition: A geometric progression is a sequence in which each term after the first is obtained by multiplying some fixed number, called the common ratio, by the preceding term.

A general notation for geometric progressions is:  $a$ , the first term,  $r$ , the common ratio, and  $n$ , the number of terms. Using this notation, any geometric progression may be represented by the sequence:

$$a, ar, ar^2, ar^3, \dots, ar^{n-1}.$$

In studying the DCF Model, we will find it useful to have an expression for the sum of  $n$  terms of a geometric progression. Call this sum  $S_n$ . Then

$$S_n = a + ar + \dots + ar^{n-1}. \quad (3)$$

However, this expression can be simplified by multiplying both sides of equation (3) by  $r$  and then subtracting the new equation from the old. Thus,

$$rS_n = ar + ar^2 + ar^3 + \dots + ar^n$$

and

$$S_n - rS_n = a - ar^n,$$

or

$$(1 - r) S_n = a (1 - r^n).$$

Solving for  $S_n$ , we obtain:

$$S_n = \frac{a(1 - r^n)}{(1 - r)} \quad (4)$$

as a simple expression for the sum of  $n$  terms of a geometric progression. Furthermore, if  $|r| < 1$ , then  $S_n$  is finite, and as  $n$  approaches infinity,  $S_n$  approaches  $a \div (1-r)$ . Thus, for a geometric progression with an infinite number of terms and  $|r| < 1$ , equation (4) becomes:

$$S = \frac{a}{1 - r} \quad (5)$$

#### Application to DCF Model

Comparing equation (2) with equation (3), we see that the firm's stock price (under the DCF assumption) is the sum of an infinite geometric progression with the first term

$$a = \frac{D_0(1 + g)}{(1 + k)}$$

and common factor

$$r = \frac{(1 + g)}{(1 + k)}$$

Applying equation (5) for the sum of such a geometric progression, we obtain

$$S = a \cdot \frac{1}{(1 - r)} = \frac{D_0(1 + g)}{(1 + k)} \cdot \frac{1}{1 - \frac{1 + g}{1 + k}} = \frac{D_0(1 + g)}{(1 + k)} \cdot \frac{1 + k}{k - g} = \frac{D_0(1 + g)}{k - g}$$

as we suggested earlier.

**Quarterly DCF Model**

The Annual DCF Model assumes that dividends grow at an annual rate of g% per year (see Figure 1).

Figure 1

Annual DCF Model

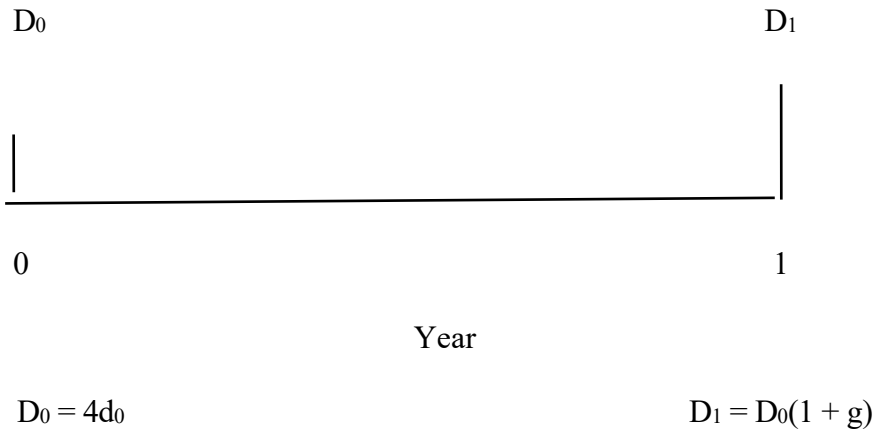
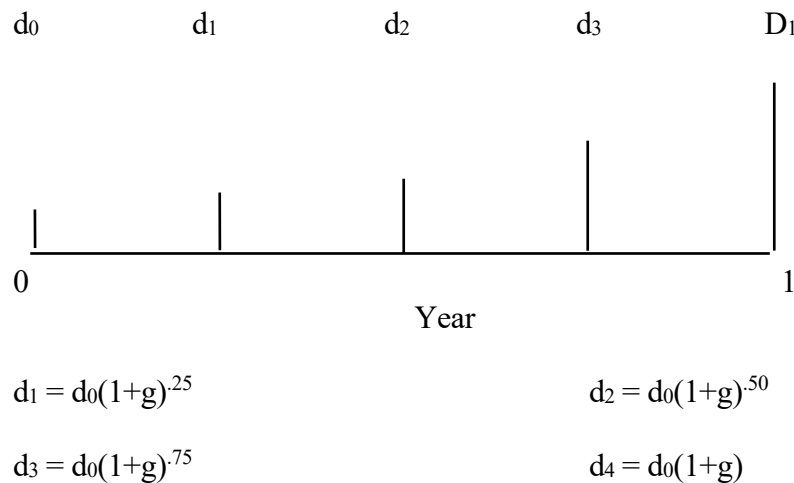


Figure 2

Quarterly DCF Model (Constant Growth Version)



In the Quarterly DCF Model, it is natural to assume that quarterly dividend payments differ from the preceding quarterly dividend by the factor  $(1 + g)^{.25}$ , where g is expressed in terms of percent per year and the decimal .25 indicates that the growth has only occurred for one quarter of

the year. (See Figure 2.) Using this assumption, along with the assumption of constant growth and  $k > g$ , we obtain a new expression for the firm's stock price, which takes account of the quarterly payment of dividends. This expression is:

$$P_0 = \frac{d_0(1+g)^{\frac{1}{4}}}{(1+k)^{\frac{1}{4}}} + \frac{d_0(1+g)^{\frac{2}{4}}}{(1+k)^{\frac{2}{4}}} + \frac{d_0(1+g)^{\frac{3}{4}}}{(1+k)^{\frac{3}{4}}} + \dots \quad (6)$$

where  $d_0$  is the last quarterly dividend payment, rather than the last annual dividend payment. (We use a lower case d to remind the reader that this is not the annual dividend.)

Although equation (6) looks formidable at first glance, it too can be greatly simplified using the formula [equation (4)] for the sum of an infinite geometric progression. As the reader can easily verify, equation (6) can be simplified to:

$$P_0 = \frac{d_0(1+g)^{\frac{1}{4}}}{(1+k)^{\frac{1}{4}} - (1+g)^{\frac{1}{4}}} \quad (7)$$

Solving equation (7) for  $k$ , we obtain a DCF formula for estimating the cost of equity under the quarterly dividend assumption:

$$k = \left[ \frac{d_0(1+g)^{\frac{1}{4}}}{P_0} + (1+g)^{\frac{1}{4}} \right]^4 - 1 \quad (8)$$

An Alternative Quarterly DCF Model

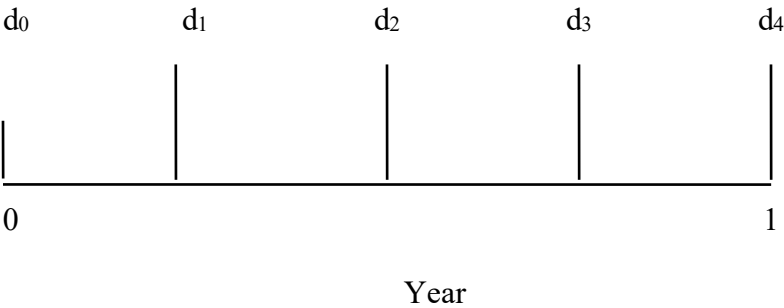
Although the constant growth Quarterly DCF Model [equation (8)] allows for the quarterly timing of dividend payments, it does require the assumption that the firm increases its dividend payments each quarter. Since this assumption is difficult for some analysts to accept, we now discuss a second Quarterly DCF Model that allows for constant quarterly dividend payments within each dividend year.

Assume then that the firm pays dividends quarterly and that each dividend payment is constant for four consecutive quarters. There are four cases to consider, with each case distinguished by varying assumptions about where we are evaluating the firm in relation to the time of its next dividend increase. (See Figure 3.)

**Figure 3**

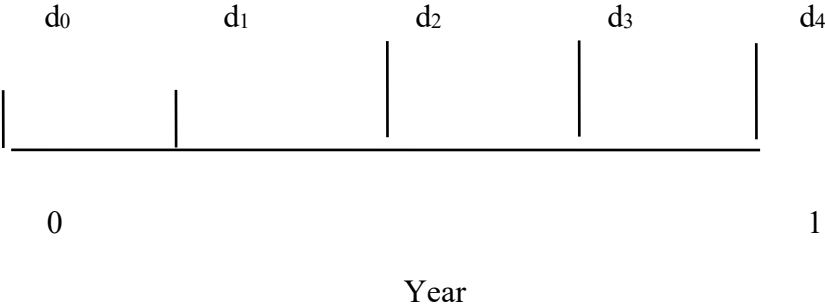
**Quarterly DCF Model (Constant Dividend Version)**

**Case 1**



$$d_1 = d_2 = d_3 = d_4 = d_0(1+g)$$

**Case 2**



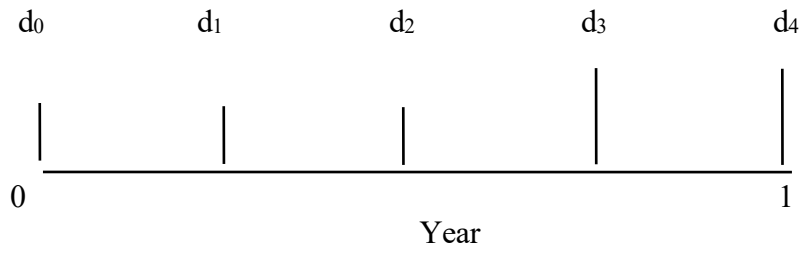
$$d_1 = d_0$$

$$d_2 = d_3 = d_4 = d_0(1+g)$$



**Figure 3 (continued)**

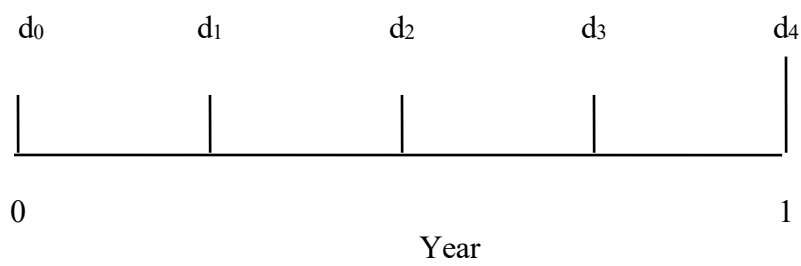
**Case 3**



$$d_1 = d_2 = d_0$$

$$d_3 = d_4 = d_0(1+g)$$

**Case 4**



$$d_1 = d_2 = d_3 = d_0$$

$$d_4 = d_0(1+g)$$

If we assume that the investor invests the quarterly dividend in an alternative investment of the same risk, then the amount accumulated by the end of the year will in all cases be given by:

$$D_1^* = d_1 (1+k)^{3/4} + d_2 (1+k)^{1/2} + d_3 (1+k)^{1/4} + d_4$$

where  $d_1$ ,  $d_2$ ,  $d_3$  and  $d_4$  are the four quarterly dividends. Under these new assumptions, the firm's stock price may be expressed by an Annual DCF Model of the form (2), with the exception that:

$$D_1^* = d_1 (1+k)^{3/4} + d_2 (1+k)^{1/2} + d_3 (1+k)^{1/4} + d_4 \quad (9)$$

is used in place of  $D_0(1+g)$ . But, we already know that the Annual DCF Model may be reduced to:

$$P_0 = \frac{D_0(1+g)}{k-g}$$

Thus, under the assumptions of the second Quarterly DCF Model, the firm's cost of equity is given by:

$$k = \frac{D_1^*}{P_0} + g \quad (10)$$

with  $D_1^*$  given by (9).

Although equation (10) looks like the Annual DCF Model, there are at least two very important practical differences. First, since  $D_1^*$  is always greater than  $D_0(1+g)$ , the estimates of the cost of equity are always larger (and more accurate) in the Quarterly Model (10) than in the Annual Model. Second, since  $D_1^*$  depends on  $k$  through equation (9), the unknown " $k$ " appears on both sides of (10), and an iterative procedure is required to solve for  $k$ .

**SUMMARY OF DISCOUNTED CASH FLOW ANALYSIS  
FOR ELECTRIC UTILITIES**

	COMPANY	MOST RECENT QUARTERLY DIVIDEND (d <sub>0</sub> )	STOCK PRICE (P <sub>0</sub> )	FORECAST OF FUTURE EARNINGS GROWTH	DCF MODEL RESULT
1	ALLETE	0.618	58.588	7.00%	11.8%
2	Alliant Energy	0.380	47.992	5.30%	8.8%
3	Amer. Elec. Power	0.700	81.226	6.20%	10.15%
4	Ameren Corp.	0.495	72.523	5.90%	9.0%
5	AVANGRID, Inc.	0.440	43.259	6.30%	11.0%
6	Avista Corp.	0.405	41.114	6.10%	10.6%
7	Black Hills	0.535	62.312	5.84%	9.75%
8	CMS Energy Corp.	0.408	57.395	7.29%	10.5%
9	Consol. Edison	0.765	78.273	2.65%	6.9%
10	Dominion Energy	0.940	76.167	4.89%	10.4%
11	DTE Energy	1.013	98.442	5.96%	10.6%
12	Duke Energy	0.945	83.082	4.12%	9.3%
13	Edison Int'l	0.638	56.522	3.00%	7.9%
14	Entergy Corp.	0.930	98.057	5.70%	10.1%
15	Evergy, Inc.	0.505	57.865	3.90%	7.8%
16	Eversource Energy	0.568	80.885	5.73%	8.9%
17	Fortis Inc.	0.478	51.957	4.85%	9.0%
18	Hawaiian Elec.	0.330	41.493	3.30%	6.8%
19	MGE Energy	0.353	63.998	4.00%	6.5%
20	NextEra Energy	1.400	233.401	8.01%	10.7%
21	NorthWestern Corp.	0.600	59.086	3.79%	8.2%
22	OGE Energy	0.388	30.728	2.40%	7.9%
23	Otter Tail Corp.	0.370	42.336	9.00%	13.1%
24	Pinnacle West Capital	0.783	76.832	4.86%	9.4%
25	PNM Resources	0.308	39.525	5.65%	9.1%
26	Portland General	0.385	47.108	4.15%	7.8%
27	PPL Corp.	0.415	25.295	2.90%	10.2%
28	Public Serv. Enterprise	0.490	47.010	3.70%	8.2%
29	Sempra Energy	1.045	118.862	4.20%	7.9%
30	Southern Co.	0.640	55.223	4.35%	9.5%
31	WEC Energy Group	0.633	88.758	5.90%	9.1%
32	Xcel Energy Inc.	0.430	60.506	6.00%	9.1%
33	Average				9.3%

Notes:

- $d_0$  = Most recent quarterly dividend.  
 $d_1, d_2, d_3, d_4$  = Next four quarterly dividends, calculated by multiplying the last four quarterly dividends by the factor  $(1 + g)$ .  
 $P_0$  = Average of the monthly high and low stock prices during the three months ending May 2020 per Refinitiv (formerly Thomson Reuters).  
 $FC$  = Flotation cost allowance (five percent) as a percent of stock price.  
 $g$  = I/B/E/S forecast of future earnings growth May 2020 from Refinitiv.  
 $k$  = Cost of equity using the quarterly version of the DCF model.

$$k = \frac{d_1(1+k)^{.75} + d_2(1+k)^{.50} + d_3(1+k)^{.25} + d_4}{P_0(1-FC)} + g$$

My analysis does not include results for companies that do not have an investment-grade bond rating, a positive I/B/E/S long-term growth forecast, or results that are less than one hundred basis points above the forecasted bond yield for a company's rating.

ADJUSTING FOR FLOTATION COSTS IN DETERMINING  
A PUBLIC UTILITY'S ALLOWED RATE OF RETURN ON EQUITY

1. INTRODUCTION

Regulation of public utilities is guided by the principle that utility revenues should be sufficient to allow recovery of all prudently incurred expenses, including the cost of capital. As set forth in the 1944 *Hope Natural Gas Case* [*Federal Power Comm'n v. Hope Natural Gas Co.* 320 U. S. 591 (1944) at 603], the U. S. Supreme Court states:

From the investor or company point of view it is important that there be enough revenue not only for operating expenses but also for the capital costs of the business. These include service on the debt and dividends on the stock....By that standard the return to the equity owner should be commensurate with returns on investments in other enterprises having corresponding risks.

Since the flotation costs arising from the issuance of debt and equity securities are an integral component of capital costs, this standard requires that the company's revenues be sufficient to fully recover flotation costs.

Despite the widespread agreement that flotation costs should be recovered in the regulatory process, several issues still need to be resolved. These include:

1. How is the term "flotation costs" defined? Does it include only the out-of-pocket costs associated with issuing securities (e. g., legal fees, printing costs, selling and underwriting expenses), or does it also include the reduction in a security's price that frequently accompanies flotation?
2. What should be the time pattern of cost recovery? Should a company be allowed to recover flotation costs immediately, or should flotation costs be recovered over the life of the issue?
3. For the purposes of regulatory accounting, should flotation costs be included as an expense? As an addition to rate base? Or as an additional element of a firm's allowed rate of return?
4. Do existing regulatory methods for flotation cost recovery allow a firm *full* recovery of flotation costs?

In this paper, I review the literature pertaining to the above issues and discuss my own views regarding how this literature applies to the cost of equity for a regulated firm.

## 2. DEFINITION OF FLOTATION COST

The value of a firm is related to the future stream of net cash flows (revenues minus expenses measured on a cash basis) that can be derived from its assets. In the process of acquiring assets, a firm incurs certain expenses which reduce its value. Some of these expenses or costs are directly associated with revenue production in one period (e. g., wages, cost of goods sold), others are more properly associated with revenue production in many periods (e. g., the acquisition cost of plant and equipment). In either case, the word “cost” refers to any item that reduces the value of a firm.

If this concept is applied to the act of issuing new securities to finance asset purchases, many items are properly included in issuance or flotation costs. These include: (1) compensation received by investment bankers for underwriting services, (2) legal fees, (3) accounting fees, (4) engineering fees, (5) trustee’s fees, (6) listing fees, (7) printing and engraving expenses, (8) SEC registration fees, (9) Federal Revenue Stamps, (10) state taxes, (11) warrants granted to underwriters as extra compensation, (12) postage expenses, (13) employees’ time, (14) market pressure, and (15) the offer discount. The finance literature generally divides these flotation cost items into three categories, namely, underwriting expenses, issuer expenses, and price effects.

## 3. MAGNITUDE OF FLOTATION COSTS

The finance literature contains several studies of the magnitude of the flotation costs associated with new debt and equity issues. These studies differ primarily regarding the time period studied, the sample of companies included, and the source of data. The flotation cost studies generally agree, however, that for large issues, underwriting expenses represent approximately one and one-half percent of the proceeds of debt issues and three to five percent of the proceeds of seasoned equity issues. They also agree that issuer expenses represent approximately 0.5 percent of both debt and equity issues, and that the announcement of an equity issue reduces the company’s stock price by at least two to three percent of the proceeds from the stock issue. Thus, total flotation costs represent approximately two percent<sup>1</sup> of the proceeds from debt issues, and five and one-half to eight and one-half percent of the proceeds of equity issues.

Lee *et. al.* [14] is an excellent example of the type of flotation cost studies found in the finance literature. The Lee study is a comprehensive recent study of the underwriting and issuer costs associated with debt and equity issues for both utilities and non-utilities. The results of the Lee *et. al.* study are reproduced in Tables 1 and 2. Table 1 demonstrates that the total underwriting and issuer expenses for the 1,092 debt issues in their study averaged 2.24 percent of the proceeds of the issues, while the total underwriting and issuer costs for the 1,593 seasoned equity issues in their study averaged 7.11 percent of the proceeds of the new issue. Table 1 also demonstrates that the total underwriting and issuer costs of seasoned equity offerings, as a percent of proceeds,

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[1] The two percent flotation cost on debt only recognizes the cost of newly-issued debt. When interest rates decline, many companies exercise the call provisions on higher cost debt and reissue debt at lower rates. This process involves reacquisition costs that are not included in the academic studies. If reacquisition costs were included in the academic studies, debt flotation costs could increase significantly.

decline with the size of the issue. For issues above \$60 million, total underwriting and issuer costs amount to from three to five percent of the amount of the proceeds.

Table 2 reports the total underwriting and issuer expenses for 135 utility debt issues and 136 seasoned utility equity issues. Total underwriting and issuer expenses for utility bond offerings averaged 1.47 percent of the amount of the proceeds and for seasoned utility equity offerings averaged 4.92 percent of the amount of the proceeds. Again, there are some economies of scale associated with larger equity offerings. Total underwriting and issuer expenses for equity offerings greater than 40 million dollars generally range from three to four percent of the proceeds.

The results of the Lee study for large equity issues are consistent with results of earlier studies by Bhagat and Frost [4], Mikkelsen and Partch [17], and Smith [24]. Bhagat and Frost found that total underwriting and issuer expenses average approximately four and one-half percent of the amount of proceeds from negotiated utility offerings during the period 1973 to 1980, and approximately three and one-half percent of the amount of the proceeds from competitive utility offerings over the same period. Mikkelsen and Partch found that total underwriting and issuer expenses average five and one-half percent of the proceeds from seasoned equity offerings over the 1972 to 1982 period. Smith found that total underwriting and issuer expenses for larger equity issues generally amount to four to five percent of the proceeds of the new issue.

The finance literature also contains numerous studies of the decline in price associated with sales of large blocks of stock to the public. These articles relate to the price impact of: (1) initial public offerings; (2) the sale of large blocks of stock from one investor to another; and (3) the issuance of seasoned equity issues to the general public. All of these studies generally support the notion that the announcement of the sale of large blocks of stock produces a decline in a company's share price. The decline in share price for initial public offerings is significantly larger than the decline in share price for seasoned equity offerings; and the decline in share price for public utilities is less than the decline in share price for non-public utilities. A comprehensive study of the magnitude of the decline in share price associated specifically with the sale of new equity by public utilities is reported in Pettway [19], who found the market pressure effect for a sample of 368 public utility equity sales to be in the range of two to three percent. This decline in price is a real cost to the utility, because the proceeds to the utility depend on the stock price on the day of issue.

In addition to the price decline associated with the announcement of a new equity issue, the finance literature recognizes that there is also a price decline associated with the actual issuance of equity securities. In particular, underwriters typically sell seasoned new equity securities to investors at a price lower than the closing market price on the day preceding the issue. The Rules of Fair Practice of the National Association of Securities Dealers require that underwriters not sell shares at a price above the offer price. Since the offer price represents a binding constraint to the underwriter, the underwriter tends to set the offer price slightly below the market price on the day of issue to compensate for the risk that the price received by the underwriter may go down, but can not increase. Smith provides evidence that the offer discount tends to be between 0.5 and 0.8 percent of the proceeds of an equity issue. I am not aware of any similar studies for debt issues.

In summary, the finance literature provides strong support for the conclusion that total underwriting and issuer expenses for public utility debt offerings represent approximately two percent of the amount of the proceeds, while total underwriting and issuer expenses for public utility equity offerings represent at least four to five percent of the amount of the proceeds. In

addition, the finance literature supports the conclusion that the cost associated with the decline in stock price at the announcement date represents approximately two to three percent as a result of a large public utility equity issue.

#### 4. TIME PATTERN OF FLOTATION COST RECOVERY

Although flotation costs are incurred only at the time a firm issues new securities, there is no reason why an issuing firm ought to recognize the expense only in the current period. In fact, if assets purchased with the proceeds of a security issue produce revenues over many years, a sound argument can be made in favor of recognizing flotation expenses over a reasonably lengthy period of time. Such recognition is certainly consistent with the generally accepted accounting principle that the time pattern of expenses match the time pattern of revenues, and it is also consistent with the normal treatment of debt flotation expenses in both regulated and unregulated industries.

In the context of a regulated firm, it should be noted that there are many possible time patterns for the recovery of flotation expenses. However, if it is felt that flotation expenses are most appropriately recovered over a period of years, then it should be recognized that investors must also be compensated for the passage of time. That is to say, the value of an investor's capital will be reduced if the expenses are merely distributed over time, without any allowance for the time value of money.

#### 5. ACCOUNTING FOR FLOTATION COST IN A REGULATORY SETTING

In a regulatory setting, a firm's revenue requirements are determined by the equation:

$$\text{Revenue Requirement} = \text{Total Expenses} + \text{Allowed Rate of Return} \times \text{Rate Base}$$

Thus, there are three ways in which an issuing firm can account for and recover its flotation expenses: (1) treat flotation expenses as a current expense and recover them immediately; (2) include flotation expenses in rate base and recover them over time; and (3) adjust the allowed rate of return upward and again recover flotation expenses over time. Before considering methods currently being used to recover flotation expenses in a regulatory setting, I shall briefly consider the advantages and disadvantages of these three basic recovery methods.

**Expenses.** Treating flotation costs as a current expense has several advantages. Because it allows for recovery at the time the expense occurs, it is not necessary to compute amortized balances over time and to debate which interest rate should be applied to these balances. A firm's stockholders are treated fairly, and so are the firm's customers, because they pay neither more nor less than the actual flotation expense. Since flotation costs are relatively small compared to the total revenue requirement, treatment as a current expense does not cause unusual rate hikes in the year of flotation, as would the introduction of a large generating plant in a state that does not allow Construction Work in Progress in rate base.

On the other hand, there are two major disadvantages of treating flotation costs as a current expense. First, since the asset purchased with the acquired funds will likely generate revenues for many years into the future, it seems unfair that current ratepayers should bear the full cost of issuing new securities, when future ratepayers share in the benefits. Second, this method requires



an estimate of the underpricing effect on each security issue. Given the difficulties involved in measuring the extent of underpricing, it may be more accurate to estimate the average underpricing allowance for many securities than to estimate the exact figure for one security.

**Rate Base.** In an article in *Public Utilities Fortnightly*, Bierman and Hass [5] recommend that flotation costs be treated as an intangible asset that is included in a firm's rate base along with the assets acquired with the stock proceeds. This approach has many advantages. For ratepayers, it provides a better match between benefits and expenses: the future ratepayers who benefit from the financing costs contribute the revenues to recover these costs. For investors, if the allowed rate of return is equal to the investors' required rate of return, it is also theoretically fair since they are compensated for the opportunity cost of their investment (including both the time value of money and the investment risk).

Despite the compelling advantages of this method of cost recovery, there are several disadvantages that probably explain why it has not been used in practice. First, a firm will only recover the proper amount for flotation expenses if the rate base is multiplied by the appropriate cost of capital. To the extent that a commission underestimates or overestimates the cost of capital, a firm will under-recover or over-recover its flotation expenses. Second, it may be both legally and psychologically difficult for commissioners to include an intangible asset in a firm's rate base. According to established legal doctrine, assets are to be included in rate base only if they are "used and useful" in the public service. It is unclear whether intangible assets such as flotation expenses meet this criterion.

**Rate of Return.** The prevailing practice among state regulators is to treat flotation expenses as an additional element of a firm's cost of capital or allowed rate of return. This method is similar to the second method above (treatment in rate base) in that some part of the initial flotation cost is amortized over time. However, it has a disadvantage not shared by the rate base method. If flotation cost is included in rate base, it is fairly easy to keep track of the flotation cost on each new equity issue and see how it is recovered over time. Using the rate of return method, it is not possible to track the flotation cost for specific issues because the flotation cost for a specific issue is never recorded. Thus, it is not clear to participants whether a current allowance is meant to recover (1) flotation costs actually incurred in a test period, (2) expected future flotation costs, or (3) past flotation costs. This confusion never arises in the treatment of debt flotation costs. Because the exact costs are recorded and explicitly amortized over time, participants recognize that current allowances for debt flotation costs are meant to recover some fraction of the flotation costs on all past debt issues.

## 6. EXISTING REGULATORY METHODS

Although most state commissions prefer to let a regulated firm recover flotation expenses through an adjustment to the allowed rate of return, there is considerable controversy about the magnitude of the required adjustment. The following are some of the most frequently asked questions: (1) Should an adjustment to the allowed return be made every year, or should the adjustment be made only in those years in which new equity is raised? (2) Should an adjusted rate of return be applied to the entire rate base, or should it be applied only to that portion of the rate base financed with paid-in capital (as opposed to retained earnings)? (3) What is the appropriate formula for adjusting the rate of return?

This section reviews several methods of allowing for flotation cost recovery. Because the regulatory methods of allowing for recovery of debt flotation costs are well known and widely accepted, I will begin my discussion of flotation cost recovery procedures by describing the widely-accepted procedure of allowing for debt flotation cost recovery.

### Debt Flotation Costs

Regulators uniformly recognize that companies incur flotation costs when they issue debt securities. They typically allow recovery of debt flotation costs by making an adjustment to both the cost of debt and the rate base (see Brigham [6]). Assume that: (1) a regulated company issues \$100 million in bonds that mature in 10 years; (2) the interest rate on these bonds is seven percent; and (3) flotation costs represent four percent of the amount of the proceeds. Then the cost of debt for regulatory purposes will generally be calculated as follows:

$$\begin{aligned}\text{Cost of Debt} &= \frac{\text{Interest expense} + \text{Amortization of flotation costs}}{\text{Principal value} - \text{Unamortized flotation costs}} \\ &= \frac{\$7,000,000 + \$400,000}{\$100,000,000 - \$4,000,000} \\ &= 7.71\%\end{aligned}$$

Thus, current regulatory practice requires that the cost of debt be adjusted upward by approximately 71 basis points, in this example, to allow for the recovery of debt flotation costs. This example does not include losses on reacquisition of debt. The flotation cost allowance would increase if losses on reacquisition of debt were included.

The logic behind the traditional method of allowing for recovery of debt flotation costs is simple. Although the company has issued \$100 million in bonds, it can only invest \$96 million in rate base because flotation costs have reduced the amount of funds received by \$4 million. If the company is not allowed to earn a 71 basis point higher rate of return on the \$96 million invested in rate base, it will not generate sufficient cash flow to pay the seven percent interest on the \$100 million in bonds it has issued. Thus, proper regulatory treatment is to increase the required rate of return on debt by 71 basis points.

### Equity Flotation Costs

The finance literature discusses several methods of recovering equity flotation costs. Because each method stems from a specific model, (*i.e.*, set of assumptions) of a firm and its cash flows, I will highlight the assumptions that distinguish one method from another.

**Arzac and Marcus.** Arzac and Marcus [2] study the proper flotation cost adjustment formula for a firm that makes continuous use of retained earnings and external equity financing and maintains a constant capital structure (debt/equity ratio). They assume at the outset that underwriting expenses and underpricing apply only to new equity obtained from external sources. They also assume that a firm has previously recovered all underwriting expenses, issuer expenses, and underpricing associated with previous issues of new equity.

To discuss and compare various equity flotation cost adjustment formulas, Arzac and Marcus make use of the following notation:

$k$	=	an investors' required return on equity
$r$	=	a utility's allowed return on equity base
$S$	=	value of equity in the absence of flotation costs
$S_f$	=	value of equity net of flotation costs
$K_t$	=	equity base at time $t$
$E_t$	=	total earnings in year $t$
$D_t$	=	total cash dividends at time $t$
$b$	=	$(E_t - D_t) \div E_t$ = retention rate, expressed as a fraction of earnings
$h$	=	new equity issues, expressed as a fraction of earnings
$m$	=	equity investment rate, expressed as a fraction of earnings, $m = b + h < 1$
$f$	=	flotation costs, expressed as a fraction of the value of an issue.

Because of flotation costs, Arzac and Marcus assume that a firm must issue a greater amount of external equity each year than it actually needs. In terms of the above notation, a firm issues  $hE_t \div (1-f)$  to obtain  $hE_t$  in external equity funding. Thus, each year a firm loses:

**EQUATION 1**

$$L = \frac{hE_t}{1-f} - hE_t = \frac{f}{1-f} \times hE_t$$

due to flotation expenses. The present value,  $V$ , of all future flotation expenses is:

**EQUATION 2**

$$V = \sum_{t=1}^{\infty} \frac{fhE_t}{(1-f)(1+k)^t} = \frac{fh}{1-f} \times \frac{rK_0}{k-mr}$$

To avoid diluting the value of the initial stockholder's equity, a regulatory authority needs to find the value of  $r$ , a firm's allowed return on equity base, that equates the value of equity net of flotation costs to the initial equity base ( $S_f = K_0$ ). Since the value of equity net of flotation costs equals the value of equity in the absence of flotation costs minus the present value of flotation costs, a regulatory authority needs to find that value of  $r$  that solves the following equation:

$$S_f = S - L.$$

This value is:

## EQUATION 3

$$r = \frac{k}{1 - \frac{fh}{1-f}}$$

To illustrate the Arzac-Marcus approach to adjusting the allowed return on equity for the effect of flotation costs, suppose that the cost of equity in the absence of flotation costs is 12 percent. Furthermore, assume that a firm obtains external equity financing each year equal to 10 percent of its earnings and that flotation expenses equal 5 percent of the value of each issue. Then, according to Arzac and Marcus, the allowed return on equity should be:

$$r = \frac{.12}{1 - \frac{(.05)(.1)}{.95}} = .1206 = 12.06\%$$

**Summary.** With respect to the three questions raised at the beginning of this section, it is evident that Arzac and Marcus believe the flotation cost adjustment should be applied each year, since continuous external equity financing is a fundamental assumption of their model. They also believe that the adjusted rate of return should be applied to the entire equity-financed portion of the rate base because their model is based on the assumption that the flotation cost adjustment mechanism will be applied to the entire equity-financed portion of the rate base. Finally, Arzac and Marcus recommend a flotation cost adjustment formula, Equation (3), that implicitly excludes recovery of financing costs associated with financing in previous periods and includes only an allowance for the fraction of equity financing obtained from external sources.

**Patterson.** The Arzac-Marcus flotation cost adjustment formula is significantly different from the conventional approach (found in many introductory textbooks) which recommends the adjustment equation:

## EQUATION 4

$$r = \frac{D_t}{P_{t-1}(1-f)} + g$$

where  $P_{t-1}$  is the stock price in the previous period and  $g$  is the expected dividend growth rate. Patterson [18] compares the Arzac-Marcus adjustment formula to the conventional approach and reaches the conclusion that the Arzac-Marcus formula effectively expenses issuance costs as they are incurred, while the conventional approach effectively amortizes them over an assumed infinite life of the equity issue. Thus, the conventional formula is similar to the formula for the recovery of debt flotation costs: it is not meant to compensate investors for the flotation costs of future issues, but instead is meant to compensate investors for the flotation costs of previous issues. Patterson argues that the conventional approach is more appropriate for rate making purposes because the plant purchased with external equity funds will yield benefits over many future periods.

**Illustration.** To illustrate the Patterson approach to flotation cost recovery, assume that a newly organized utility sells an initial issue of stock for \$100 per share, and that the utility plans to finance

all new investments with retained earnings. Assume also that: (1) the initial dividend per share is six dollars; (2) the expected long-run dividend growth rate is six percent; (3) the flotation cost is five percent of the amount of the proceeds; and (4) the payout ratio is 51.28 percent. Then, the investor's required rate of return on equity is  $[k = (D/P) + g = 6 \text{ percent} + 6 \text{ percent} = 12 \text{ percent}]$ ; and the flotation-cost-adjusted cost of equity is  $[6 \text{ percent} (1/.95) + 6 \text{ percent} = 12.316 \text{ percent}]$ .

The effects of the Patterson adjustment formula on the utility's rate base, dividends, earnings, and stock price are shown in Table 3. We see that the Patterson formula allows earnings and dividends to grow at the expected six percent rate. We also see that the present value of expected future dividends, \$100, is just sufficient to induce investors to part with their money. If the present value of expected future dividends were less than \$100, investors would not have been willing to invest \$100 in the firm. Furthermore, the present value of future dividends will only equal \$100 if the firm is allowed to earn the 12.316 percent flotation-cost-adjusted cost of equity on its entire rate base.

**Summary.** Patterson's opinions on the three issues raised in this section are in stark contrast to those of Arzac and Marcus. He believes that: (1) a flotation cost adjustment should be applied in every year, regardless of whether a firm issues any new equity in each year; (2) a flotation cost adjustment should be applied to the entire equity-financed portion of the rate base, including that portion financed by retained earnings; and (3) the rate of return adjustment formula should allow a firm to recover an appropriate fraction of all previous flotation expenses.

## 7. CONCLUSION

Having reviewed the literature and analyzed flotation cost issues, I conclude that:

**Definition of Flotation Cost:** A regulated firm should be allowed to recover both the total underwriting and issuance expenses associated with issuing securities and the cost of market pressure.

**Time Pattern of Flotation Cost Recovery.** Shareholders are indifferent between the alternatives of immediate recovery of flotation costs and recovery over time, as long as they are fairly compensated for the opportunity cost of their money. This opportunity cost must include both the time value of money and a risk premium for equity investments of this nature.

**Regulatory Recovery of Flotation Costs.** The Patterson approach to recovering flotation costs is the only rate-of-return-adjustment approach that meets the *Hope* case criterion that a regulated company's revenues must be sufficient to allow the company an opportunity to recover all prudently incurred expenses, including the cost of capital. The Patterson approach is also the only rate-of-return-adjustment approach that provides an incentive for investors to invest in the regulated company.

**Implementation of a Flotation Cost Adjustment.** As noted earlier, prevailing regulatory practice seems to be to allow the recovery of flotation costs through an adjustment to the required rate of return. My review of the literature on this subject indicates that there are at least two recommended methods of making this adjustment: the Patterson approach and the Arzac-Marcus approach. The Patterson approach assumes that a firm's flotation expenses on new equity

issues are treated in the same manner as flotation expenses on new bond issues, *i.e.*, they are amortized over future time periods. If this assumption is true (and I believe it is), then the flotation cost adjustment should be applied to a firm's entire equity base, including retained earnings. In practical terms, the Patterson approach produces an increase in a firm's cost of equity of approximately thirty basis points. The Arzac-Marcus approach assumes that flotation costs on new equity issues are recovered entirely in the year in which the securities are sold. Under the Arzac-Marcus assumption, a firm should not be allowed any adjustments for flotation costs associated with previous flotations. Instead, a firm should be allowed only an adjustment on future security sales as they occur. Under reasonable assumptions about the rate of new equity sales, this method produces an increase in the cost of equity of approximately six basis points. Since the Arzac-Marcus approach does not allow the company to recover the entire amount of its flotation cost, I recommend that this approach be rejected and the Patterson approach be accepted.

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**TABLE 1**  
**DIRECT COSTS AS A PERCENTAGE OF GROSS PROCEEDS**  
**FOR EQUITY (IPOS AND SEOS) AND STRAIGHT AND CONVERTIBLE BONDS**  
**OFFERED BY DOMESTIC OPERATING COMPANIES 1990—1994<sup>2</sup>**

**Equities**

Line No.	Proceeds (\$ in millions)	IPOs				SEOs			
		No. of Issues	Gross Spreads	Other Direct Expenses	Total Direct Costs	No. of Issues	Gross Spreads	Other Direct Expenses	Total Direct Costs
1	2-9.99	337	9.05%	7.91%	16.96%	167	7.72%	5.56%	13.28%
2	10-19.99	389	7.24%	4.39%	11.63%	310	6.23%	2.49%	8.72%
3	20-39.99	533	7.01%	2.69%	9.70%	425	5.60%	1.33%	6.93%
4	40-59.99	215	6.96%	1.76%	8.72%	261	5.05%	0.82%	5.87%
5	60-79.99	79	6.74%	1.46%	8.20%	143	4.57%	0.61%	5.18%
6	80-99.99	51	6.47%	1.44%	7.91%	71	4.25%	0.48%	4.73%
7	100-199.99	106	6.03%	1.03%	7.06%	152	3.85%	0.37%	4.22%
8	200-499.99	47	5.67%	0.86%	6.53%	55	3.26%	0.21%	3.47%
9	500 and up	10	5.21%	0.51%	5.72%	9	3.03%	0.12%	3.15%
<b>10</b>	<b>Total/Average</b>	<b>1,767</b>	<b>7.31%</b>	<b>3.69%</b>	<b>11.00%</b>	<b>1,593</b>	<b>5.44%</b>	<b>1.67%</b>	<b>7.11%</b>

**Bonds**

Line No.	Proceeds (\$ in millions)	Convertible Bonds				Straight Bonds			
		No. of Issues	Gross Spreads	Other Direct Expenses	Total Direct Costs	No. of Issues	Gross Spreads	Other Direct Expenses	Total Direct Costs
1	2-9.99	4	6.07%	2.68%	8.75%	32	2.07%	2.32%	4.39%
2	10-19.99	14	5.48%	3.18%	8.66%	78	1.36%	1.40%	2.76%
3	20-39.99	18	4.16%	1.95%	6.11%	89	1.54%	0.88%	2.42%
4	40-59.99	28	3.26%	1.04%	4.30%	90	0.72%	0.60%	1.32%
5	60-79.99	47	2.64%	0.59%	3.23%	92	1.76%	0.58%	2.34%
6	80-99.99	13	2.43%	0.61%	3.04%	112	1.55%	0.61%	2.16%
7	100-199.99	57	2.34%	0.42%	2.76%	409	1.77%	0.54%	2.31%
8	200-499.99	27	1.99%	0.19%	2.18%	170	1.79%	0.40%	2.19%
9	500 and up	3	2.00%	0.09%	2.09%	20	1.39%	0.25%	1.64%
<b>10</b>	<b>Total/Average</b>	<b>211</b>	<b>2.92%</b>	<b>0.87%</b>	<b>3.79%</b>	<b>1,092</b>	<b>1.62%</b>	<b>0.62%</b>	<b>2.24%</b>

[2] Inmoo Lee, Scott Lochhead, Jay Ritter, and Quanshui Zhao, "The Costs of Raising Capital," *Journal of Financial Research* Vol 19 No 1 (Spring 1996) pp. 59-74.

Notes:

Closed-end funds and unit offerings are excluded from the sample. Rights offerings for SEOs are also excluded. Bond offerings do not include securities backed by mortgages and issues by Federal agencies. Only firm commitment offerings and non-shelf-registered offerings are included.

Gross Spreads as a percentage of total proceeds, including management fee, underwriting fee, and selling concession.

Other Direct Expenses as a percentage of total proceeds, including management fee, underwriting fee, and selling concession.

Total Direct Costs as a percentage of total proceeds (total direct costs are the sum of gross spreads and other direct expenses.)

**TABLE 2**  
**DIRECT COSTS OF RAISING CAPITAL 1990—1994**  
**UTILITY VERSUS NON-UTILITY COMPANIES<sup>3</sup>**

<b>Equities</b>							
	<b>Non-Utilities</b>	<b>IPOs</b>			<b>SEOs</b>		
<b>Line No.</b>	<b>Proceeds (\$ in millions)</b>	<b>No. of Issues</b>	<b>Gross Spreads</b>	<b>Total Direct Costs</b>	<b>No. Of Issues</b>	<b>Gross Spreads</b>	<b>Total Direct Costs</b>
1	2-9.99	332	9.04%	16.97%	154	7.91%	13.76%
2	10-19.99	388	7.24%	11.64%	278	6.42%	9.01%
3	20-39.99	528	7.01%	9.70%	399	5.70%	7.07%
4	40-59.99	214	6.96%	8.71%	240	5.17%	6.02%
5	60-79.99	78	6.74%	8.21%	131	4.68%	5.31%
6	80-99.99	47	6.46%	7.88%	60	4.35%	4.84%
7	100-199.99	101	6.01%	7.01%	137	3.97%	4.36%
8	200-499.99	44	5.65%	6.49%	50	3.27%	3.48%
9	500 and up	10	5.21%	5.72%	8	3.12%	3.25%
<b>10</b>	<b>Total/Average</b>	1,742	7.31%	11.01%	1,457	5.57%	7.32%
<b>11</b>	<b>Utilities Only</b>						
12	2-9.99	5	9.40%	16.54%	13	5.41%	7.68%
13	10-19.99	1	7.00%	8.77%	32	4.59%	6.21%
14	20-39.99	5	7.00%	9.86%	26	4.17%	4.96%
15	40-59.99	1	6.98%	11.55%	21	3.69%	4.12%
16	60-79.99	1	6.50%	7.55%	12	3.39%	3.72%
17	80-99.99	4	6.57%	8.24%	11	3.68%	4.11%
18	100-199.99	5	6.45%	7.96%	15	2.83%	2.98%
19	200-499.99	3	5.88%	7.00%	5	3.19%	3.48%
20	500 and up	0			1	2.25%	2.31%
<b>21</b>	<b>Total/Average</b>	25	7.15%	10.14%	136	4.01%	4.92%

[3] Lee *et al*, *op. cit.*

**TABLE 2 (CONTINUED)**  
**DIRECT COSTS OF RAISING CAPITAL 1990—1994**  
**UTILITY VERSUS NON-UTILITY COMPANIES<sup>4</sup>**

<b>Bonds</b>							
	<b>Non- Utilities</b>	<b>Convertible Bonds</b>			<b>Straight Bonds</b>		
Line No.	Proceeds (\$ in millions)	No. of Issues	Gross Spreads	Total Direct Costs	No. of Issues	Gross Spreads	Total Direct Costs
1	2-9.99	4	6.07%	8.75%	29	2.07%	4.53%
2	10-19.99	12	5.54%	8.65%	47	1.70%	3.28%
3	20-39.99	16	4.20%	6.23%	63	1.59%	2.52%
4	40-59.99	28	3.26%	4.30%	76	0.73%	1.37%
5	60-79.99	47	2.64%	3.23%	84	1.84%	2.44%
6	80-99.99	12	2.54%	3.19%	104	1.61%	2.25%
7	100-199.99	55	2.34%	2.77%	381	1.83%	2.38%
8	200-499.99	26	1.97%	2.16%	154	1.87%	2.27%
9	500 and up	3	2.00%	2.09%	19	1.28%	1.53%
10	<b>Total/Average</b>	203	2.90%	3.75%	957	1.70%	2.34%
11	<b>Utilities Only</b>						
12	2-9.99	0			3	2.00%	3.28%
13	10-19.99	2	5.13%	8.72%	31	0.86%	1.35%
14	20-39.99	2	3.88%	5.18%	26	1.40%	2.06%
15	40-59.99	0			14	0.63%	1.10%
16	60-79.99	0			8	0.87%	1.13%
17	80-99.99	1	1.13%	1.34%	8	0.71%	0.98%
18	100-199.99	2	2.50%	2.74%	28	1.06%	1.42%
19	200-499.99	1	2.50%	2.65%	16	1.00%	1.40%
20	500 and up	0			1	3.50%	na <sup>5</sup>
21	<b>Total/Average</b>	8	3.33%	4.66%	135	1.04%	1.47%

Notes:

Total proceeds raised in the United States, excluding proceeds from the exercise of over allotment options.

Gross spreads as a percentage of total proceeds (including management fee, underwriting fee, and selling concession).

Other direct expenses as a percentage of total proceeds (including registration fee and printing, legal, and auditing costs).

[4] Lee *et al*, *op. cit.*

[5] Not available because of missing data on other direct expenses.

**TABLE 3**  
**ILLUSTRATION OF PATTERSON APPROACH TO FLOTATION COST RECOVERY**

LINE NO.	TIME PERIOD	RATE BASE	EARNINGS @ 12.32%	EARNINGS @ 12.00%	DIVIDENDS	AMORTIZATION INITIAL FC
1	0	95.00				
2	1	100.70	11.70	11.40	6.00	0.3000
3	2	106.74	12.40	12.08	6.36	0.3180
4	3	113.15	13.15	12.81	6.74	0.3371
5	4	119.94	13.93	13.58	7.15	0.3573
6	5	127.13	14.77	14.39	7.57	0.3787
7	6	134.76	15.66	15.26	8.03	0.4015
8	7	142.84	16.60	16.17	8.51	0.4256
9	8	151.42	17.59	17.14	9.02	0.4511
10	9	160.50	18.65	18.17	9.56	0.4782
11	10	170.13	19.77	19.26	10.14	0.5068
12	11	180.34	20.95	20.42	10.75	0.5373
13	12	191.16	22.21	21.64	11.39	0.5695
14	13	202.63	23.54	22.94	12.07	0.6037
15	14	214.79	24.96	24.32	12.80	0.6399
16	15	227.67	26.45	25.77	13.57	0.6783
17	16	241.33	28.04	27.32	14.38	0.7190
18	17	255.81	29.72	28.96	15.24	0.7621
19	18	271.16	31.51	30.70	16.16	0.8078
20	19	287.43	33.40	32.54	17.13	0.8563
21	20	304.68	35.40	34.49	18.15	0.9077
22	21	322.96	37.52	36.56	19.24	0.9621
23	22	342.34	39.77	38.76	20.40	1.0199
24	23	362.88	42.16	41.08	21.62	1.0811
25	24	384.65	44.69	43.55	22.92	1.1459
26	25	407.73	47.37	46.16	24.29	1.2147
27	26	432.19	50.21	48.93	25.75	1.2876
28	27	458.12	53.23	51.86	27.30	1.3648
29	28	485.61	56.42	54.97	28.93	1.4467
30	29	514.75	59.81	58.27	30.67	1.5335
31	30	545.63	63.40	61.77	32.51	1.6255
32	Present Value@12%		195.00	190.00	100.00	5.00

**EX ANTE RISK PREMIUM APPROACH**

My ex ante risk premium method is based on studies of the DCF expected return on proxy companies compared to the interest rate on Moody's A-rated utility bonds. Specifically, for each month in my study period, I calculate the risk premium using the equation,

$$RP_{\text{PROXY}} = DCF_{\text{PROXY}} - I_A$$

where:

$RP_{\text{PROXY}}$  = the required risk premium on an equity investment in the proxy group of companies,

$DCF_{\text{PROXY}}$  = average DCF estimated cost of equity on a portfolio of proxy companies; and

$I_A$  = the yield to maturity on an investment in A-rated utility bonds.

**Electric Company Ex Ante Risk Premium Analysis.** For my ex ante risk premium electric proxy group DCF analysis, I began with the twenty-four electric utilities comprising the Moody's electric utility group for the years 1999 through 2015. I used the Moody's group of electric utilities because they were a widely followed group of electric utilities, and using this constant group greatly simplified the data collection task required to estimate the ex ante risk premium over the months of my study. Simplifying the data collection task was desirable because the ex ante risk premium approach requires that the DCF model be estimated for every company in every month of the study period. Because many of the companies that were formerly included in the Moody's electric utility group have now been eliminated due to mergers and acquisitions, and because it is desirable to have a larger set of companies in the analysis than became available in the Moody's group, beginning in January 2016 I use the same proxy group of electric utilities and DCF model in my ex ante risk premium analysis as are used in my discounted cash flow analysis. The Ex Ante Risk Premium exhibit in my direct testimony displays the average DCF estimated cost of equity on an investment in the portfolio of electric utilities and the yield to maturity on A-rated utility bonds in each month of the study.

Previous studies have shown that the ex ante risk premium tends to vary inversely with the level of interest rates, that is, the risk premium tends to increase when interest rates decline, and decrease when interest rates go up. To test whether my studies also indicate that the ex ante risk premium varies inversely with the level of interest rates, I performed a regression analysis of the relationship between the ex ante risk premium and the yield to maturity on A-rated utility bonds, using the equation,

$$RP_{\text{PROXY}} = a + (b \times I_A) + e$$

where:

- $RP_{\text{PROXY}}$  = risk premium on proxy company group;  
 $I_A$  = yield to maturity on A-rated utility bonds;  
 $e$  = a random residual; and  
 $a, b$  = coefficients estimated by the regression procedure.

Regression analysis assumes that the statistical residuals from the regression equation are random. My examination of the residuals revealed that there is a significant probability that the residuals are serially correlated (non-zero serial correlation indicates that the residual in one time period tends to be correlated with the residual in the previous time period). Therefore, I adjusted my data to correct for the possibility of serial correlation in the residuals.

The common procedure for dealing with serial correlation in the residuals is to estimate the regression coefficients in two steps. First, a multiple regression analysis is used to estimate the serial correlation coefficient,  $r$ . Second, the estimated serial correlation coefficient is used to transform the original variables into new variables whose serial correlation is approximately zero. The regression coefficients are then re-estimated using the transformed variables as inputs in the regression equation. Based on my knowledge of the statistical relationship between the yield to maturity on A-rated utility bonds and the required risk premium, my estimate of the ex ante risk premium on an investment in my proxy electric company group as compared to an investment in A-rated utility bonds is given by the equation:

$$\begin{aligned} RP_{\text{PROXY}} &= 8.21 - .581 \times I_A \\ &= (14.937) \quad (-6.927) \text{ [1]} \end{aligned}$$

Using the forecast 4.4 percent yield to maturity on A-rated utility bonds, the regression equation produces an ex ante risk premium based on the electric proxy group equal to 5.64 percent ( $8.21 - .581 \times 4.4 = 5.64$ ).

To estimate the cost of equity using the ex ante risk premium method, one may add the estimated risk premium over the yield on A-rated utility bonds to the yield to maturity on A-rated utility bonds. The forecast yield on A-rated utility bonds is 4.43 percent. As noted above, my analyses produce an estimated risk premium over the yield on A-rated utility bonds equal to 5.64 percent. Adding an estimated risk premium of 5.64 percent to the 4.43 percent forecasted

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[1] The t-statistics are shown in parentheses.

yield to maturity on A-rated utility bonds produces a cost of equity estimate of 10.1 percent for the electric company proxy group using the ex ante risk premium method.



**EX ANTE RISK PREMIUM APPROACH: COMPARISON OF DCF EXPECTED RETURN  
ON AN INVESTMENT IN ELECTRIC UTILITIES TO THE INTEREST RATE ON  
MOODY'S A-RATED UTILITY BONDS**

In this analysis, I compute an electric utility equity risk premium by studying the relationship between the DCF estimated cost of equity for an electric utility proxy group to the interest rate on A-rated utility bonds. For each month in my September 1999 through May 2020 study period:

DCF	=	Average DCF-estimated cost of equity on a portfolio of proxy companies;
Bond Yield	=	Yield to maturity on an investment in A-rated utility bonds; and
Risk Premium	=	DCF cost of equity – bond yield.

A more detailed description of my *ex ante* risk premium method is contained in Appendix 4.

LINE	DATE	DCF	BOND YIELD	RISK PREMIUM
1	Sep-99	0.1157	0.0793	0.0364
2	Oct-99	0.1161	0.0806	0.0355
3	Nov-99	0.1192	0.0794	0.0398
4	Dec-99	0.1236	0.0814	0.0422
5	Jan-00	0.1221	0.0835	0.0386
6	Feb-00	0.1269	0.0825	0.0444
7	Mar-00	0.1313	0.0828	0.0485
8	Apr-00	0.1237	0.0829	0.0408
9	May-00	0.1227	0.0870	0.0357
10	Jun-00	0.1242	0.0836	0.0406
11	Jul-00	0.1247	0.0825	0.0422
12	Aug-00	0.1228	0.0813	0.0415
13	Sep-00	0.1164	0.0823	0.0341
14	Oct-00	0.1170	0.0814	0.0356
15	Nov-00	0.1191	0.0811	0.0380
16	Dec-00	0.1166	0.0784	0.0382
17	Jan-01	0.1194	0.0780	0.0414
18	Feb-01	0.1203	0.0774	0.0429
19	Mar-01	0.1207	0.0768	0.0439
20	Apr-01	0.1233	0.0794	0.0439
21	May-01	0.1279	0.0799	0.0480
22	Jun-01	0.1285	0.0785	0.0500
23	Jul-01	0.1295	0.0778	0.0517
24	Aug-01	0.1302	0.0759	0.0543
25	Sep-01	0.1321	0.0775	0.0546
26	Oct-01	0.1313	0.0763	0.0550
27	Nov-01	0.1296	0.0757	0.0539
28	Dec-01	0.1292	0.0783	0.0509
29	Jan-02	0.1274	0.0766	0.0508
30	Feb-02	0.1285	0.0754	0.0531
31	Mar-02	0.1248	0.0776	0.0472
32	Apr-02	0.1227	0.0757	0.0470
33	May-02	0.1236	0.0752	0.0484
34	Jun-02	0.1254	0.0741	0.0513

LINE	DATE	DCF	BOND YIELD	RISK PREMIUM
35	Jul-02	0.1337	0.0731	0.0606
36	Aug-02	0.1300	0.0717	0.0583
37	Sep-02	0.1272	0.0708	0.0564
38	Oct-02	0.1291	0.0723	0.0568
39	Nov-02	0.1242	0.0714	0.0528
40	Dec-02	0.1226	0.0707	0.0519
41	Jan-03	0.1195	0.0706	0.0489
42	Feb-03	0.1233	0.0693	0.0540
43	Mar-03	0.1212	0.0679	0.0533
44	Apr-03	0.1170	0.0664	0.0506
45	May-03	0.1095	0.0636	0.0459
46	Jun-03	0.1047	0.0621	0.0426
47	Jul-03	0.1072	0.0657	0.0415
48	Aug-03	0.1064	0.0678	0.0386
49	Sep-03	0.1029	0.0656	0.0373
50	Oct-03	0.1009	0.0643	0.0366
51	Nov-03	0.0985	0.0637	0.0348
52	Dec-03	0.0946	0.0627	0.0319
53	Jan-04	0.0921	0.0615	0.0306
54	Feb-04	0.0916	0.0615	0.0301
55	Mar-04	0.0912	0.0597	0.0315
56	Apr-04	0.0925	0.0635	0.0290
57	May-04	0.0962	0.0662	0.0300
58	Jun-04	0.0961	0.0646	0.0315
59	Jul-04	0.0953	0.0627	0.0326
60	Aug-04	0.0966	0.0614	0.0352
61	Sep-04	0.0951	0.0598	0.0353
62	Oct-04	0.0953	0.0594	0.0359
63	Nov-04	0.0918	0.0597	0.0321
64	Dec-04	0.0920	0.0592	0.0328
65	Jan-05	0.0925	0.0578	0.0347
66	Feb-05	0.0917	0.0561	0.0356
67	Mar-05	0.0918	0.0583	0.0335
68	Apr-05	0.0924	0.0564	0.0360
69	May-05	0.0910	0.0553	0.0356
70	Jun-05	0.0911	0.0540	0.0371
71	Jul-05	0.0899	0.0551	0.0348
72	Aug-05	0.0900	0.0550	0.0350
73	Sep-05	0.0923	0.0552	0.0371
74	Oct-05	0.0934	0.0579	0.0355
75	Nov-05	0.0981	0.0588	0.0393
76	Dec-05	0.0980	0.0580	0.0400
77	Jan-06	0.0980	0.0575	0.0405
78	Feb-06	0.1071	0.0582	0.0489
79	Mar-06	0.1055	0.0598	0.0457
80	Apr-06	0.1075	0.0629	0.0446

LINE	DATE	DCF	BOND YIELD	RISK PREMIUM
81	May-06	0.1087	0.0642	0.0445
82	Jun-06	0.1117	0.0640	0.0477
83	Jul-06	0.1110	0.0637	0.0473
84	Aug-06	0.1072	0.0620	0.0452
85	Sep-06	0.1111	0.0600	0.0511
86	Oct-06	0.1074	0.0598	0.0476
87	Nov-06	0.1078	0.0580	0.0498
88	Dec-06	0.1071	0.0581	0.0490
89	Jan-07	0.1096	0.0596	0.0500
90	Feb-07	0.1085	0.0590	0.0495
91	Mar-07	0.1094	0.0585	0.0509
92	Apr-07	0.1042	0.0597	0.0445
93	May-07	0.1068	0.0599	0.0469
94	Jun-07	0.1123	0.0630	0.0493
95	Jul-07	0.1130	0.0625	0.0505
96	Aug-07	0.1104	0.0624	0.0480
97	Sep-07	0.1078	0.0618	0.0460
98	Oct-07	0.1084	0.0611	0.0473
99	Nov-07	0.1116	0.0597	0.0519
100	Dec-07	0.1132	0.0616	0.0516
101	Jan-08	0.1193	0.0602	0.0591
102	Feb-08	0.1133	0.0621	0.0512
103	Mar-08	0.1170	0.0621	0.0549
104	Apr-08	0.1159	0.0629	0.0530
105	May-08	0.1162	0.0627	0.0535
106	Jun-08	0.1136	0.0638	0.0499
107	Jul-08	0.1172	0.0640	0.0532
108	Aug-08	0.1191	0.0637	0.0554
109	Sep-08	0.1185	0.0649	0.0536
110	Oct-08	0.1280	0.0756	0.0524
111	Nov-08	0.1312	0.0760	0.0552
112	Dec-08	0.1301	0.0654	0.0647
113	Jan-09	0.1241	0.0639	0.0602
114	Feb-09	0.1269	0.0630	0.0639
115	Mar-09	0.1286	0.0642	0.0644
116	Apr-09	0.1266	0.0648	0.0617
117	May-09	0.1242	0.0649	0.0593
118	Jun-09	0.1220	0.0620	0.0600
119	Jul-09	0.1174	0.0597	0.0577
120	Aug-09	0.1158	0.0571	0.0587
121	Sep-09	0.1152	0.0553	0.0599
122	Oct-09	0.1153	0.0555	0.0598
123	Nov-09	0.1196	0.0564	0.0633
124	Dec-09	0.1095	0.0579	0.0516
125	Jan-10	0.1112	0.0577	0.0535
126	Feb-10	0.1091	0.0587	0.0504

LINE	DATE	DCF	BOND YIELD	RISK PREMIUM
127	Mar-10	0.1076	0.0584	0.0492
128	Apr-10	0.1111	0.0582	0.0529
129	May-10	0.1093	0.0552	0.0541
130	Jun-10	0.1088	0.0546	0.0541
131	Jul-10	0.1078	0.0526	0.0552
132	Aug-10	0.1057	0.0501	0.0557
133	Sep-10	0.1059	0.0501	0.0558
134	Oct-10	0.1044	0.0510	0.0534
135	Nov-10	0.1051	0.0536	0.0514
136	Dec-10	0.1053	0.0557	0.0497
137	Jan-11	0.1044	0.0557	0.0487
138	Feb-11	0.1041	0.0568	0.0473
139	Mar-11	0.1044	0.0556	0.0488
140	Apr-11	0.1020	0.0555	0.0465
141	May-11	0.0994	0.0532	0.0462
142	Jun-11	0.1043	0.0526	0.0517
143	Jul-11	0.1019	0.0527	0.0492
144	Aug-11	0.1050	0.0469	0.0581
145	Sep-11	0.1016	0.0448	0.0568
146	Oct-11	0.1032	0.0452	0.0580
147	Nov-11	0.1014	0.0425	0.0589
148	Dec-11	0.1024	0.0435	0.0589
149	Jan-12	0.1016	0.0434	0.0582
150	Feb-12	0.0974	0.0436	0.0538
151	Mar-12	0.0971	0.0448	0.0523
152	Apr-12	0.0994	0.0440	0.0554
153	May-12	0.0981	0.0420	0.0561
154	Jun-12	0.0962	0.0408	0.0554
155	Jul-12	0.0963	0.0393	0.0570
156	Aug-12	0.0972	0.0400	0.0572
157	Sep-12	0.0968	0.0402	0.0566
158	Oct-12	0.0978	0.0391	0.0587
159	Nov-12	0.0935	0.0384	0.0551
160	Dec-12	0.0962	0.0400	0.0562
161	Jan-13	0.0968	0.0415	0.0553
162	Feb-13	0.0956	0.0418	0.0538
163	Mar-13	0.0976	0.0420	0.0556
164	Apr-13	0.0966	0.0400	0.0566
165	May-13	0.0970	0.0417	0.0553
166	Jun-13	0.0990	0.0453	0.0537
167	Jul-13	0.0978	0.0468	0.0510
168	Aug-13	0.0958	0.0473	0.0485
169	Sep-13	0.0950	0.0480	0.0470
170	Oct-13	0.0925	0.0470	0.0455
171	Nov-13	0.0931	0.0477	0.0454
172	Dec-13	0.0931	0.0481	0.0450

LINE	DATE	DCF	BOND YIELD	RISK PREMIUM
173	Jan-14	0.0922	0.0463	0.0459
174	Feb-14	0.0944	0.0453	0.0491
175	Mar-14	0.0983	0.0451	0.0532
176	Apr-14	0.0970	0.0441	0.0529
177	May-14	0.0983	0.0426	0.0557
178	Jun-14	0.0972	0.0429	0.0543
179	Jul-14	0.0966	0.0423	0.0543
180	Aug-14	0.0978	0.0413	0.0565
181	Sep-14	0.0962	0.0424	0.0538
182	Oct-14	0.1013	0.0406	0.0607
183	Nov-14	0.0995	0.0409	0.0586
184	Dec-14	0.0984	0.0395	0.0589
185	Jan-15	0.0972	0.0358	0.0614
186	Feb-15	0.0983	0.0367	0.0616
187	Mar-15	0.0985	0.0374	0.0611
188	Apr-15	0.1005	0.0375	0.0630
189	May-15	0.0983	0.0417	0.0566
190	Jun-15	0.0963	0.0439	0.0524
191	Jul-15	0.0956	0.0440	0.0516
192	Aug-15	0.0966	0.0425	0.0541
193	Sep-15	0.0941	0.0439	0.0502
194	Oct-15	0.0937	0.0429	0.0508
195	Nov-15	0.0938	0.0440	0.0498
196	Dec-15	0.0941	0.0435	0.0506
197	Jan-16	0.0981	0.0427	0.0554
198	Feb-16	0.0977	0.0411	0.0566
199	Mar-16	0.0974	0.0416	0.0558
200	Apr-16	0.0960	0.0400	0.0560
201	May-16	0.0943	0.0393	0.0550
202	Jun-16	0.0940	0.0378	0.0562
203	Jul-16	0.0930	0.0357	0.0573
204	Aug-16	0.0930	0.0359	0.0571
205	Sep-16	0.0932	0.0366	0.0566
206	Oct-16	0.0946	0.0377	0.0569
207	Nov-16	0.0933	0.0408	0.0525
208	Dec-16	0.0940	0.0427	0.0513
209	Jan-17	0.0934	0.0414	0.0520
210	Feb-17	0.0944	0.0418	0.0526
211	Mar-17	0.0942	0.0423	0.0519
212	Apr-17	0.0930	0.0412	0.0518
213	May-17	0.0970	0.0412	0.0558
214	Jun-17	0.0965	0.0394	0.0571
215	Jul-17	0.0956	0.0399	0.0557
216	Aug-17	0.0936	0.0386	0.0550
217	Sep-17	0.0960	0.0387	0.0573
218	Oct-17	0.0963	0.0391	0.0572

**EX POST RISK PREMIUM APPROACH**

**Source**

Stock price and yield information is obtained from Standard & Poor's Security Price publication. Standard & Poor's derives the stock dividend yield by dividing the aggregate cash dividends (based on the latest known annual rate) by the aggregate market value of the stocks in the group. The bond price information is obtained by calculating the present value of a bond due in thirty years with a \$4.00 coupon and the yield to maturity of each year's indicated Moody's A-rated utility bond yield. The values shown in the schedules are the January values of the respective indices.

**Calculation of Stock and Bond Returns**

Sample calculation of "Stock Return" column:

$$\text{Stock Return (2019)} = \left[ \frac{\text{Stock Price (2020)} - \text{Stock Price (2019)} + \text{Dividend (2019)}}{\text{Stock Price (2019)}} \right]$$

where Dividend (2019) = Stock Price (2019) x Stock Div. Yield (2019)

Sample calculation of "Bond Return" column:

$$\text{Bond Return (2019)} = \left[ \frac{\text{Bond Price (2020)} - \text{Bond Price (2019)} + \text{Interest (2019)}}{\text{Bond Price (2019)}} \right]$$

where Interest = \$4.00.

**EX POST RISK PREMIUM APPROACH: COMPARATIVE RETURNS ON S&P 500 STOCK INDEX  
AND MOODY'S A-RATED UTILITY BONDS 1937 — 2019**

LINE	YEAR	S&P 500 STOCK PRICE	STOCK DIVIDEND YIELD	STOCK RETURN	A-RATED BOND PRICE	BOND RETURN	RISK PREMIUM
1	2020	3,278.20	0.0211		\$113.41		
2	2019	2,607.39	0.0208	27.81%	\$94.20	24.64%	3.17%
3	2018	2,789.80	0.0198	-4.56%	\$102.46	-4.16%	-0.40%
4	2017	2,275.12	0.0209	24.71%	\$96.13	10.75%	13.97%
5	2016	1,918.60	0.0222	20.80%	\$95.48	4.87%	15.93%
6	2015	2,028.18	0.0208	-3.32%	\$107.65	-7.59%	4.26%
7	2014	1,822.36	0.0210	13.39%	\$89.89	24.20%	-10.81%
8	2013	1,481.11	0.0220	25.24%	\$97.45	-3.65%	28.89%
9	2012	1,300.58	0.0214	16.02%	\$94.36	7.52%	8.50%
10	2011	1,282.62	0.0185	3.25%	\$77.36	27.14%	-23.89%
11	2010	1,123.58	0.0203	16.18%	\$75.02	8.44%	7.74%
12	2009	865.58	0.0310	32.91%	\$68.43	15.48%	17.43%
13	2008	1,378.76	0.0206	-35.16%	\$72.25	0.24%	-35.40%
14	2007	1,424.16	0.0181	-1.38%	\$72.91	4.59%	-5.97%
15	2006	1,278.72	0.0183	13.20%	\$75.25	2.20%	11.01%
16	2005	1,181.41	0.0177	10.01%	\$74.91	5.80%	4.21%
17	2004	1,132.52	0.0162	5.94%	\$70.87	11.34%	-5.40%
18	2003	895.84	0.0180	28.22%	\$62.26	20.27%	7.95%
19	2002	1,140.21	0.0138	-20.05%	\$57.44	15.35%	-35.40%
20	2001	1,335.63	0.0116	-13.47%	\$56.40	8.93%	-22.40%
21	2000	1,425.59	0.0118	-5.13%	\$52.60	14.82%	-19.95%
22	1999	1,248.77	0.0130	15.46%	\$63.03	-10.20%	25.66%
23	1998	963.35	0.0162	31.25%	\$62.43	7.38%	23.87%
24	1997	766.22	0.0195	27.68%	\$56.62	17.32%	10.36%
25	1996	614.42	0.0231	27.02%	\$60.91	-0.48%	27.49%
26	1995	465.25	0.0287	34.93%	\$50.22	29.26%	5.68%
27	1994	472.99	0.0269	1.05%	\$60.01	-9.65%	10.71%
28	1993	435.23	0.0288	11.56%	\$53.13	20.48%	-8.93%
29	1992	416.08	0.0290	7.50%	\$49.56	15.27%	-7.77%
30	1991	325.49	0.0382	31.65%	\$44.84	19.44%	12.21%
31	1990	339.97	0.0341	-0.85%	\$45.60	7.11%	-7.96%
32	1989	285.41	0.0364	22.76%	\$43.06	15.18%	7.58%
33	1988	250.48	0.0366	17.61%	\$40.10	17.36%	0.25%
34	1987	264.51	0.0317	-2.13%	\$48.92	-9.84%	7.71%
35	1986	208.19	0.0390	30.95%	\$39.98	32.36%	-1.41%
36	1985	171.61	0.0451	25.83%	\$32.57	35.05%	-9.22%
37	1984	166.39	0.0427	7.41%	\$31.49	16.12%	-8.72%
38	1983	144.27	0.0479	20.12%	\$29.41	20.65%	-0.53%
39	1982	117.28	0.0595	28.96%	\$24.48	36.48%	-7.51%
40	1981	132.97	0.0480	-7.00%	\$29.37	-3.01%	-3.99%
41	1980	110.87	0.0541	25.34%	\$34.69	-3.81%	29.16%
42	1979	99.71	0.0533	16.52%	\$43.91	-11.89%	28.41%

LINE	YEAR	S&P 500 STOCK PRICE	STOCK DIVIDEND YIELD	STOCK RETURN	A-RATED BOND PRICE	BOND RETURN	RISK PREMIUM
43	1978	90.25	0.0532	15.80%	\$49.09	-2.40%	18.20%
44	1977	103.80	0.0399	-9.06%	\$50.95	4.20%	-13.27%
45	1976	96.86	0.0380	10.96%	\$43.91	25.13%	-14.17%
46	1975	72.56	0.0507	38.56%	\$41.76	14.75%	23.81%
47	1974	96.11	0.0364	-20.86%	\$52.54	-12.91%	-7.96%
48	1973	118.40	0.0269	-16.14%	\$58.51	-3.37%	-12.77%
49	1972	103.30	0.0296	17.58%	\$56.47	10.69%	6.89%
50	1971	93.49	0.0332	13.81%	\$53.93	12.13%	1.69%
51	1970	90.31	0.0356	7.08%	\$50.46	14.81%	-7.73%
52	1969	102.00	0.0306	-8.40%	\$62.43	-12.76%	4.36%
53	1968	95.04	0.0313	10.45%	\$66.97	-0.81%	11.26%
54	1967	84.45	0.0351	16.05%	\$78.69	-9.81%	25.86%
55	1966	93.32	0.0302	-6.48%	\$86.57	-4.48%	-2.00%
56	1965	86.12	0.0299	11.35%	\$91.40	-0.91%	12.26%
57	1964	76.45	0.0305	15.70%	\$92.01	3.68%	12.02%
58	1963	65.06	0.0331	20.82%	\$93.56	2.61%	18.20%
59	1962	69.07	0.0297	-2.84%	\$89.60	8.89%	-11.73%
60	1961	59.72	0.0328	18.94%	\$89.74	4.29%	14.64%
61	1960	58.03	0.0327	6.18%	\$84.36	11.13%	-4.95%
62	1959	55.62	0.0324	7.57%	\$91.55	-3.49%	11.06%
63	1958	41.12	0.0448	39.74%	\$101.22	-5.60%	45.35%
64	1957	45.43	0.0431	-5.18%	\$100.70	4.49%	-9.67%
65	1956	44.15	0.0424	7.14%	\$113.00	-7.35%	14.49%
66	1955	35.60	0.0438	28.40%	\$116.77	0.20%	28.20%
67	1954	25.46	0.0569	45.52%	\$112.79	7.07%	38.45%
68	1953	26.18	0.0545	2.70%	\$114.24	2.24%	0.46%
69	1952	24.19	0.0582	14.05%	\$113.41	4.26%	9.79%
70	1951	21.21	0.0634	20.39%	\$123.44	-4.89%	25.28%
71	1950	16.88	0.0665	32.30%	\$125.08	1.89%	30.41%
72	1949	15.36	0.0620	16.10%	\$119.82	7.72%	8.37%
73	1948	14.83	0.0571	9.28%	\$118.50	4.49%	4.79%
74	1947	15.21	0.0449	1.99%	\$126.02	-2.79%	4.79%
75	1946	18.02	0.0356	-12.03%	\$126.74	2.59%	-14.63%
76	1945	13.49	0.0460	38.18%	\$119.82	9.11%	29.07%
77	1944	11.85	0.0495	18.79%	\$119.82	3.34%	15.45%
78	1943	10.09	0.0554	22.98%	\$118.50	4.49%	18.49%
79	1942	8.93	0.0788	20.87%	\$117.63	4.14%	16.73%
80	1941	10.55	0.0638	-8.98%	\$116.34	4.55%	-13.52%
81	1940	12.30	0.0458	-9.65%	\$112.39	7.08%	-16.73%
82	1939	12.50	0.0349	1.89%	\$105.75	10.05%	-8.16%
83	1938	11.31	0.0784	18.36%	\$99.83	9.94%	8.42%
84	1937	17.59	0.0434	-31.36%	\$103.18	0.63%	-31.99%
85	Risk Premium			11.41%		6.76%	4.7%

Note: See Appendix 5 for an explanation of the derivation of stock and bond returns and the source of the data presented



**EX POST RISK PREMIUM APPROACH: COMPARATIVE RETURNS ON  
S&P UTILITY STOCK INDEX AND MOODY'S A-RATED  
UTILITY BONDS 1937 — 2019**

LINE	YEAR	S&P UTILITY STOCK PRICE	STOCK DIVIDEND YIELD	STOCK RETURN	A- RATED BOND PRICE	BOND RETURN	RISK PREMIUM
1	2020				\$113.41		
2	2019			25.79%	\$94.20	24.64%	1.15%
3	2018			3.67%	\$102.46	-4.16%	7.83%
4	2017			11.72%	\$96.13	10.75%	0.97%
5	2016			17.44%	\$95.48	4.87%	12.57%
6	2015			-3.90%	\$107.65	-7.59%	3.69%
7	2014			28.91%	\$89.89	24.20%	4.71%
8	2013			13.01%	\$97.45	-3.65%	16.66%
9	2012			2.09%	\$94.36	7.52%	-5.43%
10	2011			19.99%	\$77.36	27.14%	-7.15%
11	2010			7.04%	\$75.02	8.44%	-1.40%
12	2009			10.71%	\$68.43	15.48%	-4.77%
13	2008			-25.90%	\$72.25	0.24%	-26.14%
14	2007			16.56%	\$72.91	4.59%	11.96%
15	2006			20.76%	\$75.25	2.20%	18.56%
16	2005			16.05%	\$74.91	5.80%	10.25%
17	2004			22.84%	\$70.87	11.34%	11.50%
18	2003			23.48%	\$62.26	20.27%	3.21%
19	2002			-14.73%	\$57.44	15.35%	-30.08%
20	2001	307.70	0.0287	-17.90%	\$56.40	8.93%	-26.83%
21	2000	239.17	0.0413	32.78%	\$52.60	14.82%	17.96%
22	1999	253.52	0.0394	-1.72%	\$63.03	-10.20%	8.48%
23	1998	228.61	0.0457	15.47%	\$62.43	7.38%	8.09%
24	1997	201.14	0.0492	18.58%	\$56.62	17.32%	1.26%
25	1996	202.57	0.0454	3.83%	\$60.91	-0.48%	4.31%
26	1995	153.87	0.0584	37.49%	\$50.22	29.26%	8.23%
27	1994	168.70	0.0496	-3.83%	\$60.01	-9.65%	5.82%
28	1993	159.79	0.0537	10.95%	\$53.13	20.48%	-9.54%
29	1992	149.70	0.0572	12.46%	\$49.56	15.27%	-2.81%
30	1991	138.38	0.0607	14.25%	\$44.84	19.44%	-5.19%
31	1990	146.04	0.0558	0.33%	\$45.60	7.11%	-6.78%
32	1989	114.37	0.0699	34.68%	\$43.06	15.18%	19.51%
33	1988	106.13	0.0704	14.80%	\$40.10	17.36%	-2.55%
34	1987	120.09	0.0588	-5.74%	\$48.92	-9.84%	4.10%
35	1986	92.06	0.0742	37.87%	\$39.98	32.36%	5.51%
36	1985	75.83	0.0860	30.00%	\$32.57	35.05%	-5.04%
37	1984	68.50	0.0925	19.95%	\$31.49	16.12%	3.83%
38	1983	61.89	0.0948	20.16%	\$29.41	20.65%	-0.49%
39	1982	51.81	0.1074	30.20%	\$24.48	36.48%	-6.28%
40	1981	52.01	0.0978	9.40%	\$29.37	-3.01%	12.41%

LINE	YEAR	S&P UTILITY STOCK PRICE	STOCK DIVIDEND YIELD	STOCK RETURN	A- RATED BOND PRICE	BOND RETURN	RISK PREMIUM
41	1980	50.26	0.0953	13.01%	\$34.69	-3.81%	16.83%
42	1979	50.33	0.0893	8.79%	\$43.91	-11.89%	20.68%
43	1978	52.40	0.0791	3.96%	\$49.09	-2.40%	6.36%
44	1977	54.01	0.0714	4.16%	\$50.95	4.20%	-0.04%
45	1976	46.99	0.0776	22.70%	\$43.91	25.13%	-2.43%
46	1975	38.19	0.0920	32.24%	\$41.76	14.75%	17.49%
47	1974	48.60	0.0713	-14.29%	\$52.54	-12.91%	-1.38%
48	1973	60.01	0.0556	-13.45%	\$58.51	-3.37%	-10.08%
49	1972	60.19	0.0542	5.12%	\$56.47	10.69%	-5.57%
50	1971	63.43	0.0504	-0.07%	\$53.93	12.13%	-12.19%
51	1970	55.72	0.0561	19.45%	\$50.46	14.81%	4.64%
52	1969	68.65	0.0445	-14.38%	\$62.43	-12.76%	-1.62%
53	1968	68.02	0.0435	5.28%	\$66.97	-0.81%	6.08%
54	1967	70.63	0.0392	0.22%	\$78.69	-9.81%	10.03%
55	1966	74.50	0.0347	-1.72%	\$86.57	-4.48%	2.76%
56	1965	75.87	0.0315	1.34%	\$91.40	-0.91%	2.25%
57	1964	67.26	0.0331	16.11%	\$92.01	3.68%	12.43%
58	1963	63.35	0.0330	9.47%	\$93.56	2.61%	6.86%
59	1962	62.69	0.0320	4.25%	\$89.60	8.89%	-4.64%
60	1961	52.73	0.0358	22.47%	\$89.74	4.29%	18.18%
61	1960	44.50	0.0403	22.52%	\$84.36	11.13%	11.39%
62	1959	43.96	0.0377	5.00%	\$91.55	-3.49%	8.49%
63	1958	33.30	0.0487	36.88%	\$101.22	-5.60%	42.48%
64	1957	32.32	0.0487	7.90%	\$100.70	4.49%	3.41%
65	1956	31.55	0.0472	7.16%	\$113.00	-7.35%	14.51%
66	1955	29.89	0.0461	10.16%	\$116.77	0.20%	9.97%
67	1954	25.51	0.0520	22.37%	\$112.79	7.07%	15.30%
68	1953	24.41	0.0511	9.62%	\$114.24	2.24%	7.38%
69	1952	22.22	0.0550	15.36%	\$113.41	4.26%	11.10%
70	1951	20.01	0.0606	17.10%	\$123.44	-4.89%	21.99%
71	1950	20.20	0.0554	4.60%	\$125.08	1.89%	2.71%
72	1949	16.54	0.0570	27.83%	\$119.82	7.72%	20.10%
73	1948	16.53	0.0535	5.41%	\$118.50	4.49%	0.92%
74	1947	19.21	0.0354	-10.41%	\$126.02	-2.79%	-7.62%
75	1946	21.34	0.0298	-7.00%	\$126.74	2.59%	-9.59%
76	1945	13.91	0.0448	57.89%	\$119.82	9.11%	48.79%
77	1944	12.10	0.0569	20.65%	\$119.82	3.34%	17.31%
78	1943	9.22	0.0621	37.45%	\$118.50	4.49%	32.96%
79	1942	8.54	0.0940	17.36%	\$117.63	4.14%	13.22%
80	1941	13.25	0.0717	-28.38%	\$116.34	4.55%	-32.92%
81	1940	16.97	0.0540	-16.52%	\$112.39	7.08%	-23.60%
82	1939	16.05	0.0553	11.26%	\$105.75	10.05%	1.21%
83	1938	14.30	0.0730	19.54%	\$99.83	9.94%	9.59%

LINE	YEAR	S&P UTILITY STOCK PRICE	STOCK DIVIDEND YIELD	STOCK RETURN	A- RATED BOND PRICE	BOND RETURN	RISK PREMIUM
84	1937	24.34	0.0432	-36.93%	\$103.18	0.63%	-37.55%
85	Risk Premium			10.74%		6.76%	4.0%

EX POST RISK PREMIUM COST OF EQUITY	
Risk Premium S&P 500	4.7%
Risk Premium S&P Utilities	4.0%
Average Risk Premium	4.4%
Forecast Yield A-rated utility bond	4.4%
Flotation	0.2%
Risk Premium Cost of Equity	9.0%

Note: See Appendix 5 for an explanation of how stock and bond returns are derived and the source of the data presented. Standard & Poor's discontinued its S&P Utilities Index in December 2001. In this study, the stock returns beginning in 2002 are based on the total returns for the EEI Index of U.S. shareholder-owned electric utilities, as reported by EEI on its website.  
<http://www.eei.org/whatwedo/DataAnalysis/IndusFinanAnalysis/Pages/QtrlyFinancialUpdates.aspx>

**ESTIMATING BETA FROM A COMPARISON OF RISK PREMIA ON  
S&P 500 AND S&P UTILITIES 1937 THROUGH 2019**

YEAR	S&P UTILITIES STOCK RETURN	S&P 500 STOCK RETURN	10-YR. TREASURY BOND YIELD	UTILITIES RISK PREMIUM	MARKET RISK PREMIUM
2019	0.2579	0.2781	0.0214	0.2365	0.2566
2018	0.0367	-0.0456	0.0291	0.0076	-0.0747
2017	0.1172	0.2471	0.0233	0.0939	0.2238
2016	0.1744	0.2080	0.0184	0.1560	0.1896
2015	-0.0390	-0.0332	0.0214	-0.0604	-0.0546
2014	0.2891	0.1339	0.0254	0.2637	0.1085
2013	0.1301	0.2524	0.0235	0.1066	0.2289
2012	0.0209	0.1602	0.0180	0.0029	0.1422
2011	0.1999	0.0325	0.0278	0.1721	0.0047
2010	0.0704	0.1618	0.0322	0.0382	0.1296
2009	0.1071	0.3291	0.0326	0.0745	0.2965
2008	-0.2590	-0.3516	0.0367	-0.2957	-0.3883
2007	0.1656	-0.0138	0.0463	0.1193	-0.0601
2006	0.2076	0.1320	0.0479	0.1597	0.0841
2005	0.1605	0.1001	0.0429	0.1176	0.0572
2004	0.2284	0.0594	0.0427	0.1857	0.0167
2003	0.2348	0.2822	0.0401	0.1947	0.2421
2002	-0.1473	-0.2005	0.0461	-0.1934	-0.2466
2001	-0.1790	-0.1347	0.0502	-0.2292	-0.1849
2000	0.3278	-0.0513	0.0603	0.2675	-0.1116
1999	-0.0172	0.1546	0.0564	-0.0736	0.0982
1998	0.1547	0.3125	0.0526	0.1021	0.2599
1997	0.1858	0.2768	0.0635	0.1223	0.2133
1996	0.0383	0.2702	0.0644	-0.0261	0.2058
1995	0.3749	0.3493	0.0658	0.3091	0.2835
1994	-0.0383	0.0105	0.0708	-0.1091	-0.0603
1993	0.1095	0.1156	0.0587	0.0508	0.0569
1992	0.1246	0.0750	0.0701	0.0545	0.0049
1991	0.1425	0.3165	0.0786	0.0639	0.2379
1990	0.0033	-0.0085	0.0855	-0.0822	-0.0940
1989	0.3468	0.2276	0.0850	0.2618	0.1426
1988	0.1480	0.1761	0.0884	0.0596	0.0877
1987	-0.0574	-0.0213	0.0838	-0.1412	-0.1051
1986	0.3787	0.3095	0.0768	0.3019	0.2327
1985	0.3000	0.2583	0.1062	0.1938	0.1521
1984	0.1995	0.0741	0.1244	0.0751	-0.0503
1983	0.2016	0.2012	0.1110	0.0906	0.0902
1982	0.3020	0.2896	0.1300	0.1720	0.1596
1981	0.0940	-0.0700	0.1391	-0.0451	-0.2091
1980	0.1301	0.2534	0.1146	0.0155	0.1388
1979	0.0879	0.1652	0.0944	-0.0065	0.0708
1978	0.0396	0.1580	0.0841	-0.0445	0.0739

YEAR	S&P UTILITIES STOCK RETURN	S&P 500 STOCK RETURN	10-YR. TREASURY BOND YIELD	UTILITIES RISK PREMIUM	MARKET RISK PREMIUM
1977	0.0416	-0.0906	0.0742	-0.0326	-0.1648
1976	0.2270	0.1096	0.0761	0.1509	0.0335
1975	0.3224	0.3856	0.0799	0.2425	0.3057
1974	-0.1429	-0.2086	0.0756	-0.2185	-0.2842
1973	-0.1345	-0.1614	0.0684	-0.2029	-0.2298
1972	0.0512	0.1758	0.0621	-0.0109	0.1137
1971	-0.0007	0.1381	0.0616	-0.0623	0.0765
1970	0.1945	0.0708	0.0735	0.1210	-0.0027
1969	-0.1438	-0.0840	0.0667	-0.2105	-0.1507
1968	0.0528	0.1045	0.0565	-0.0037	0.0480
1967	0.0022	0.1605	0.0507	-0.0485	0.1098
1966	-0.0172	-0.0648	0.0492	-0.0664	-0.1140
1965	0.0134	0.1135	0.0428	-0.0294	0.0707
1964	0.1611	0.1570	0.0419	0.1192	0.1151
1963	0.0947	0.2082	0.0400	0.0547	0.1682
1962	0.0425	-0.0284	0.0395	0.0030	-0.0679
1961	0.2247	0.1894	0.0388	0.1859	0.1506
1960	0.2252	0.0618	0.0412	0.1840	0.0206
1959	0.0500	0.0757	0.0433	0.0067	0.0324
1958	0.3688	0.3974	0.0332	0.3356	0.3642
1957	0.0790	-0.0518	0.0365	0.0425	-0.0883
1956	0.0716	0.0714	0.0318	0.0398	0.0396
1955	0.1016	0.2840	0.0282	0.0734	0.2558
1954	0.2237	0.4552	0.0240	0.1997	0.4312
1953	0.0962	0.0270	0.0281	0.0681	-0.0011
1952	0.1536	0.1405	0.0248	0.1288	0.1157
1951	0.1710	0.2039	0.0241	0.1469	0.1798
1950	0.0460	0.3230	0.0205	0.0255	0.3025
1949	0.2783	0.1610	0.0193	0.2590	0.1417
1948	0.0541	0.0928	0.0215	0.0326	0.0713
1947	-0.1041	0.0199	0.0185	-0.1226	0.0014
1946	-0.0700	-0.1203	0.0174	-0.0874	-0.1377
1945	0.5789	0.3818	0.0173	0.5616	0.3645
1944	0.2065	0.1879	0.0209	0.1856	0.1670
1943	0.3745	0.2298	0.0207	0.3538	0.2091
1942	0.1736	0.2087	0.0211	0.1525	0.1876
1941	-0.2838	-0.0898	0.0199	-0.3037	-0.1097
1940	-0.1652	-0.0965	0.0220	-0.1872	-0.1185
1939	0.1126	0.0189	0.0235	0.0891	-0.0046
1938	0.1954	0.1836	0.0255	0.1699	0.1581
1937	-0.3693	-0.3136	0.0269	-0.3962	-0.3405
Risk Premium 1937 to 2020				0.0568	0.0635
RP Utilities/RP SP500				0.89	

**USING THE ARITHMETIC MEAN TO ESTIMATE  
THE COST OF EQUITY CAPITAL**

Consider an investment that in a given year generates a return of 30 percent with probability equal to 0.5 and a return of -10 percent with a probability equal to 0.5. For each one dollar invested, the possible outcomes of this investment at the end of year one are:

WEALTH AFTER ONE YEAR	PROBABILITY
\$1.30	0.50
\$0.90	0.50

At the end of year two, the possible outcomes are:

WEALTH AFTER TWO YEARS			PROBABILITY	WEALTH x PROBABILITY
(1.30) (1.30)	=	\$1.69	0.25	0.4225
(1.30) (.9)	=	\$1.17	0.25	0.2925
(.9) (1.30)	=	\$1.17	0.25	0.2925
(.9) (.9)	=	\$0.81	0.25	0.2025
Expected Wealth	=			\$1.21

The expected value of this investment at the end of year two is \$1.21. In a competitive capital market, the cost of equity is equal to the expected rate of return on an investment. In the above example, the cost of equity is that rate of return which will make the initial investment of one dollar grow to the expected value of \$1.21 at the end of two years. Thus, the cost of equity is the solution to the equation:

$$1(1+k)^2 = 1.21 \text{ or}$$

$$k = (1.21/1)^{.5} - 1 = 10\%.$$

The arithmetic mean of this investment is:

$$(30\%) (.5) + (-10\%) (.5) = 10\%.$$

Thus, the arithmetic mean is equal to the cost of equity capital.

The geometric mean of this investment is:

$$[(1.3) (.9)]^{.5} - 1 = .082 = 8.2\%.$$

Thus, the geometric mean is not equal to the cost of equity capital.

The lesson is obvious: for an investment with an uncertain outcome, the arithmetic mean is the best measure of the cost of equity capital.

**CALCULATION OF CAPITAL ASSET PRICING MODEL COST OF EQUITY  
USING AN HISTORICAL RISK PREMIUM**

LINE	COMPANY	VALUE LINE BETA	RISK- FREE RATE	MARKET RISK PREMIUM	BETA X RISK PREMIUM	CAPM COST OF EQUITY
1	ALLETE	0.85	2.84%	7.2%	6.1%	9.2%
2	Alliant Energy	0.80	2.84%	7.2%	5.8%	8.8%
3	Amer. Elec. Power	0.75	2.84%	7.2%	5.4%	8.5%
4	Ameren Corp.	0.80	2.84%	7.2%	5.8%	8.8%
5	CenterPoint Energy	1.15	2.84%	7.2%	8.3%	11.3%
6	CMS Energy Corp.	0.80	2.84%	7.2%	5.8%	8.8%
7	DTE Energy	0.90	2.84%	7.2%	6.5%	9.5%
8	Entergy Corp.	0.95	2.84%	7.2%	6.8%	9.9%
9	Eversgy	1.05	2.84%	7.2%	7.6%	10.6%
10	Fortis Inc.	0.80	2.84%	7.2%	5.8%	8.8%
11	MGE Energy	0.70	2.84%	7.2%	5.0%	8.1%
12	OGE Energy	1.05	2.84%	7.2%	7.6%	10.6%
13	Otter Tail Corp.	0.85	2.84%	7.2%	6.1%	9.2%
14	WEC Energy Group	0.80	2.84%	7.2%	5.8%	8.8%
15	AVANGRID, Inc.	0.80	2.84%	7.2%	5.8%	8.8%
16	Consol. Edison	0.75	2.84%	7.2%	5.4%	8.5%
17	Dominion Energy	0.80	2.84%	7.2%	5.8%	8.8%
18	Duke Energy	0.85	2.84%	7.2%	6.1%	9.2%
19	Eversource Energy	0.90	2.84%	7.2%	6.5%	9.5%
20	Exelon Corp.	0.90	2.84%	7.2%	6.5%	9.5%
21	FirstEnergy Corp.	0.85	2.84%	7.2%	6.1%	9.2%
22	NextEra Energy	0.85	2.84%	7.2%	6.1%	9.2%
23	PPL Corp.	1.05	2.84%	7.2%	7.6%	10.6%
24	Public Serv. Enterprise	0.90	2.84%	7.2%	6.5%	9.5%
25	Southern Co.	0.90	2.84%	7.2%	6.5%	9.5%
26	Avista Corp.	0.95	2.84%	7.2%	6.8%	9.9%
27	Black Hills	1.00	2.84%	7.2%	7.2%	10.3%
28	Edison Int'l	0.90	2.84%	7.2%	6.5%	9.5%
29	Hawaiian Elec.	0.80	2.84%	7.2%	5.8%	8.8%
30	IDACORP, Inc.	0.80	2.84%	7.2%	5.8%	8.8%
31	NorthWestern Corp.	0.90	2.84%	7.2%	6.5%	9.5%
32	Pinnacle West Capital	0.85	2.84%	7.2%	6.1%	9.2%
33	PNM Resources	0.90	2.84%	7.2%	6.5%	9.5%
34	Portland General	0.85	2.84%	7.2%	6.1%	9.2%
35	Sempra Energy	0.95	2.84%	7.2%	6.8%	9.9%
36	Xcel Energy Inc.	0.75	2.84%	7.2%	5.4%	8.5%
37	Cost of Equity 0.87 Beta	0.87	2.84%	7.2%	6.3%	9.3%
38	Cost of Equity 0.89 Beta	0.89	2.84%	7.2%	6.4%	9.5%
39	<b>Average Historical CAPM Cost of Equity</b>					<b>9.4%</b>

Notes: Historical Ibbotson® SBBI® risk premium including years 1926 through year end 2019 from 2020 SBBI Yearbook. Value Line beta for comparable companies from Value Line. Utility beta equal to 0.89 calculated per Schedule 6. Treasury bond yield forecast from data in Value Line Selection & Opinion, May 29, 2020, and Energy Information Administration, 2020, determined as follows. Value Line forecasts a yield on 10-year Treasury notes equal to 1.5 percent. The spread between the average yield on 10-year Treasury notes (0.67 percent) and 20-year Treasury bonds (1.12 percent) is 45 basis points. Adding 45 basis points to Value Line's 1.5 percent forecasted yield on 20-year Treasury notes produces a forecasted yield of 1.95 percent for 20-year Treasury bonds (see Value Line Investment Survey, Selection & Opinion, May 29, 2020). EIA forecasts a yield of 3.28 percent on 10-year Treasury notes. Adding the 45-basis point spread between 10-year Treasury notes and 20-year Treasury bonds to the EIA forecast of 3.28 percent for 10-year Treasury notes produces an EIA forecast for 20-year Treasury bonds equal to 3.73 percent. The average of the forecasts is 2.84 percent (1.95 percent using Value Line data and 3.73 percent using EIA data).

**CALCULATION OF CAPITAL ASSET PRICING MODEL COST OF EQUITY  
USING DCF ESTIMATE OF THE EXPECTED RATE OF RETURN  
ON THE MARKET PORTFOLIO**

LINE	COMPANY	VALUE LINE BETA	RISK- FREE RATE	DCF S&P 500	MARKET RISK PREMIUM	BETA X RISK PREMIUM	CAPM COST OF EQUITY
1	ALLETE	0.85	2.84%	11.5%	8.7%	7.36%	10.4%
2	Alliant Energy	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
3	Amer. Elec. Power	0.75	2.84%	11.5%	8.7%	6.50%	9.5%
4	Ameren Corp.	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
5	CenterPoint Energy	1.15	2.84%	11.5%	8.7%	9.96%	13.0%
6	CMS Energy Corp.	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
7	DTE Energy	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
8	Entergy Corp.	0.95	2.84%	11.5%	8.7%	8.23%	11.3%
9	Eversource Energy	1.05	2.84%	11.5%	8.7%	9.09%	12.1%
10	Fortis Inc.	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
11	MGE Energy	0.70	2.84%	11.5%	8.7%	6.06%	9.1%
12	OGE Energy	1.05	2.84%	11.5%	8.7%	9.09%	12.1%
13	Otter Tail Corp.	0.85	2.84%	11.5%	8.7%	7.36%	10.4%
14	WEC Energy Group	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
15	AVANGRID, Inc.	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
16	Consol. Edison	0.75	2.84%	11.5%	8.7%	6.50%	9.5%
17	Dominion Energy	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
18	Duke Energy	0.85	2.84%	11.5%	8.7%	7.36%	10.4%
19	Eversource Energy	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
20	Exelon Corp.	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
21	FirstEnergy Corp.	0.85	2.84%	11.5%	8.7%	7.36%	10.4%
22	NextEra Energy	0.85	2.84%	11.5%	8.7%	7.36%	10.4%
23	PPL Corp.	1.05	2.84%	11.5%	8.7%	9.09%	12.1%
24	Public Serv. Enterprise	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
25	Southern Co.	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
26	Avista Corp.	0.95	2.84%	11.5%	8.7%	8.23%	11.3%
27	Black Hills	1.00	2.84%	11.5%	8.7%	8.66%	11.7%
28	Edison Int'l	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
29	Hawaiian Elec.	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
30	IDACORP, Inc.	0.80	2.84%	11.5%	8.7%	6.93%	10.0%
31	NorthWestern Corp.	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
32	Pinnacle West Capital	0.85	2.84%	11.5%	8.7%	7.36%	10.4%
33	PNM Resources	0.90	2.84%	11.5%	8.7%	7.79%	10.8%
34	Portland General	0.85	2.84%	11.5%	8.7%	7.36%	10.4%
35	Sempra Energy	0.95	2.84%	11.5%	8.7%	8.23%	11.3%
36	Xcel Energy Inc.	0.75	2.84%	11.5%	8.7%	6.50%	9.5%
37	Cost of Equity 0.87 Beta	0.87	2.84%	11.5%	8.7%	7.57%	10.6%
38	Cost of Equity 0.89 Beta	0.89	2.84%	11.5%	8.7%	7.74%	10.8%
39	<b>Average DCF CAPM Cost of Equity</b>						<b>10.7%</b>

Notes: Value Line beta for comparable companies from Value Line. Utility beta equal to 0.89 calculated per Schedule 6. Treasury bond yield forecast from data in Value Line Selection & Opinion, May 29, 2020, and Energy Information Administration, 2020, determined as follows. Value Line forecasts a yield on 10-year Treasury notes equal to 1.5 percent. The spread between the average yield on 10-year Treasury notes (0.67 percent) and 20-year Treasury bonds (1.12 percent) is 45 basis points. Adding 45 basis points to Value Line's 1.5 percent forecasted yield on 20-year Treasury notes produces a forecasted yield of 1.95 percent for 20-year Treasury bonds (see Value Line Investment Survey, Selection & Opinion, May 29, 2020). EIA forecasts a yield of 3.28 percent on 10-year Treasury notes. Adding the 45-basis point spread between 10-year Treasury notes and 20-year Treasury bonds to the EIA forecast of 3.28 percent for 10-year Treasury notes produces an EIA forecast for 20-year Treasury bonds equal to 3.73 percent. The average of the forecasts is 2.84 percent (1.95 percent using Value Line data and 3.73 percent using EIA data).



(CONTINUED)  
SUMMARY OF DISCOUNTED CASH FLOW ANALYSIS  
FOR S&P 500 COMPANIES

	COMPANY	STOCK PRICE (P <sub>0</sub> )	D <sub>0</sub>	FORECAST OF FUTURE EARNINGS GROWTH	MODEL RESULT	MARKET CAP \$ (MILS)
1	3M	142.31	5.88	1.41%	5.7%	86,095
2	ABBOTT LABORATORIES	84.35	1.44	10.28%	12.2%	159,355
3	ABBVIE	81.00	4.72	11.50%	18.1%	160,708
4	ACCENTURE CLASS A	174.10	3.20	7.37%	9.4%	129,172
5	ACTIVISION BLIZZARD	62.88	0.41	22.96%	23.8%	56,846
6	ADV.AUTO PARTS	112.48	1.00	7.00%	8.0%	9,378
7	AES	12.97	0.57	7.10%	11.9%	8,624
8	AFLAC	34.65	1.12	1.88%	5.2%	24,969
9	AGILENT TECHS.	76.09	0.72	7.70%	8.7%	25,302
10	AIR PRDS.& CHEMS.	213.97	5.36	9.62%	12.4%	52,961
11	ALBEMARLE	65.10	1.54	15.00%	17.7%	7,245
12	ALLIANCE DATA SYSTEMS	46.29	0.84	5.60%	7.5%	2,099
13	ALLIANT ENERGY (XSC)	47.99	1.52	5.30%	8.7%	11,642
14	ALTRIA GROUP	38.00	3.36	3.18%	12.6%	70,191
15	AMCOR	8.57	0.46	2.57%	8.2%	14,878
16	AMER.ELEC.PWR.	81.23	2.80	5.85%	9.5%	38,532
17	AMEREN	72.52	1.98	5.90%	8.8%	17,364
18	AMERICAN EXPRESS	88.72	1.72	5.99%	8.1%	73,035
19	AMERICAN INTL.GP.	27.26	1.28	4.97%	10.0%	24,151
20	AMERICAN TOWER	228.67	4.32	16.89%	19.1%	102,023
21	AMERIPRISE FINL.	116.57	4.16	11.56%	15.6%	16,103
22	AMERISOURCEBERGEN	85.48	1.68	8.23%	10.4%	18,862
23	AMGEN	215.76	6.40	5.95%	9.1%	134,044
24	ANALOG DEVICES	100.81	2.48	6.95%	9.6%	42,210
25	ANTHEM	252.10	3.80	14.33%	16.1%	70,593
26	AON CLASS A	180.95	1.76	8.97%	10.0%	45,124
27	APPLE	276.36	3.28	11.47%	12.8%	1,383,649
28	APPLIED MATS.	49.77	0.88	19.10%	21.2%	52,129
29	ARTHUR J GALLAGHER	84.11	1.80	7.16%	9.5%	17,197
30	AT&T	30.52	2.08	2.42%	9.6%	210,829
31	ATMOS ENERGY	98.33	2.30	7.15%	9.7%	12,159
32	AUTOMATIC DATA PROC.	137.03	3.64	12.20%	15.2%	57,925
33	AVERY DENNISON	104.30	2.32	8.55%	11.0%	8,813
34	BALL	65.55	0.60	10.32%	11.3%	20,926
35	BANK OF AMERICA	23.13	0.72	5.12%	8.4%	198,758
36	BANK OF NEW YORK MELLON	34.60	1.24	2.48%	6.2%	30,835
37	BAXTER INTL.	84.50	0.98	9.67%	10.9%	44,482
38	BECTON DICKINSON	239.58	3.16	7.25%	8.7%	70,414
39	BEST BUY	70.09	2.20	7.90%	11.3%	20,997
40	BLACKROCK	457.87	14.52	2.39%	5.7%	78,479
41	BRISTOL MYERS SQUIBB	58.13	1.80	17.90%	21.6%	139,563
42	BROADCOM	247.93	13.00	12.35%	18.4%	111,414
43	CAMPBELL SOUP	49.38	1.40	2.75%	5.7%	14,535
44	CAPITAL ONE FINL.	60.98	1.60	8.00%	10.9%	27,992
45	CARDINAL HEALTH	48.97	1.94	4.73%	8.9%	15,461
46	CDW	99.61	1.52	9.10%	10.8%	15,545
47	CELANESE	78.35	2.48	4.60%	8.0%	10,180

	COMPANY	STOCK PRICE (P <sub>0</sub> )	D <sub>0</sub>	FORECAST OF FUTURE EARNINGS GROWTH	MODEL RESULT	MARKET CAP \$ (MILS)
48	CENTURYLINK	10.04	1.00	6.00%	17.0%	10,865
49	CERNER	66.27	0.72	14.90%	16.2%	20,632
50	CH ROBINSON WWD.	70.00	2.04	10.00%	13.2%	10,448
51	CHEVRON	82.59	5.16	5.50%	12.2%	173,629
52	CHURCH & DWIGHT CO.	67.60	0.96	7.90%	9.4%	17,741
53	CIGNA	179.02	0.04	12.59%	12.6%	69,468
54	CINTAS	214.34	2.55	9.70%	11.0%	25,027
55	CISCO SYSTEMS	40.62	1.44	6.18%	10.0%	191,861
56	CITIZENS FINANCIAL GROUP	22.10	1.56	5.72%	13.4%	9,245
57	CITRIX SYS.	138.19	1.40	6.40%	7.5%	16,967
58	CLOROX	190.03	4.24	5.26%	7.6%	25,721
59	CME GROUP	178.18	3.40	5.13%	7.2%	64,839
60	CMS ENERGY	57.40	1.63	7.29%	10.4%	15,756
61	COCA COLA	46.24	1.64	1.86%	5.5%	197,092
62	COLGATE-PALM.	68.34	1.76	4.25%	7.0%	60,360
63	COMCAST A	36.83	0.92	6.15%	8.8%	178,408
64	CONAGRA BRANDS	30.84	0.85	8.68%	11.7%	15,942
65	CONCHO RESOURCES	53.10	0.80	5.54%	7.1%	11,428
66	CONSOLIDATED EDISON	78.27	3.06	2.65%	6.7%	23,634
67	CONSTELLATION BRANDS 'A'	152.18	3.00	7.04%	9.2%	28,950
68	CORNING	21.01	0.88	4.80%	9.3%	16,421
69	CORTEVA	24.90	0.52	9.81%	12.1%	18,777
70	COSTCO WHOLESALE	301.79	2.80	6.48%	7.5%	134,625
71	COTY CL.A	5.37	0.50	7.60%	18.0%	2,503
72	CROWN CASTLE INTL.	150.02	4.80	21.00%	24.9%	63,496
73	CSX	62.73	1.04	5.35%	7.1%	52,327
74	CVS HEALTH	60.79	2.00	6.05%	9.6%	82,634
75	D R HORTON	44.68	0.70	9.90%	11.6%	19,049
76	DANAHER	149.46	0.72	10.69%	11.2%	112,556
77	DEERE	137.90	3.04	3.07%	5.4%	44,523
78	DENTSPLY SIRONA	41.00	0.40	9.82%	10.9%	9,136
79	DIAMONDBACK ENERGY	38.19	1.50	12.97%	17.5%	6,890
80	DOLLAR GENERAL	165.00	1.44	10.89%	11.9%	44,913
81	DOMINION ENERGY	76.17	3.76	4.89%	10.2%	66,014
82	DOMINO'S PIZZA	344.91	3.12	11.93%	12.9%	14,757
83	DOVER	87.77	1.96	7.20%	9.6%	13,105
84	DTE ENERGY	98.44	4.05	5.96%	10.4%	19,887
85	DUKE ENERGY	83.08	3.78	4.12%	8.9%	61,221
86	DUPONT DE NEMOURS	41.47	1.20	3.96%	7.0%	35,861
87	EASTMAN CHEMICAL	55.76	2.64	2.61%	7.6%	8,911
88	EATON	78.40	2.92	4.70%	8.7%	31,172
89	EBAY	36.20	0.64	9.78%	11.7%	30,011
90	ECOLAB	179.53	1.88	7.38%	8.5%	58,554
91	EDISON INTL.	56.52	2.55	3.00%	7.7%	21,263
92	ELI LILLY	144.16	2.96	12.53%	14.9%	146,461
93	EMERSON ELECTRIC	53.55	2.00	1.47%	5.3%	33,943
94	ENTERGY	98.06	3.72	5.70%	9.8%	19,534
95	EVERGY	57.87	2.02	3.90%	7.6%	13,403
96	EVERSOURCE ENERGY	80.89	2.27	5.73%	8.7%	26,714
97	EXPEDITOR INTL.OF WASH.	68.21	1.04	4.43%	6.0%	12,106
98	EXXON MOBIL	42.61	3.48	10.95%	20.3%	191,834

	COMPANY	STOCK PRICE (P <sub>0</sub> )	D <sub>0</sub>	FORECAST OF FUTURE EARNINGS GROWTH	MODEL RESULT	MARKET CAP \$ (MILS)
99	FIDELITY NAT.INFO.SVS.	126.28	1.40	12.66%	13.9%	85,316
100	FLOWSERVE	27.22	0.80	6.36%	9.5%	3,256
101	FMC	84.45	1.76	9.71%	12.0%	12,048
102	FORTIVE	57.68	0.28	5.76%	6.3%	19,908
103	GARMIN	80.19	2.44	4.87%	8.1%	16,021
104	GENERAL DYNAMICS	135.34	4.40	4.80%	8.2%	39,298
105	GENERAL MILLS	57.14	1.96	5.92%	9.6%	36,932
106	GILEAD SCIENCES	76.94	2.72	1.84%	5.5%	92,686
107	GLOBAL PAYMENTS	157.00	0.78	16.32%	16.9%	53,980
108	GLOBE LIFE	74.47	0.75	6.60%	7.7%	7,727
109	GOLDMAN SACHS GP.	175.78	5.00	5.37%	8.4%	62,395
110	H&R BLOCK	15.71	1.04	10.00%	17.5%	3,210
111	HASBRO	67.26	2.72	10.55%	15.1%	9,435
112	HERSHEY	135.07	3.09	6.85%	9.3%	19,341
113	HEWLETT PACKARD ENTER.	9.93	0.48	4.91%	10.1%	13,244
114	HNTGTN.INGALLS INDS.	185.92	4.12	3.81%	6.1%	7,087
115	HOME DEPOT	207.94	6.00	7.25%	10.4%	256,179
116	HONEYWELL INTL.	135.78	3.60	3.15%	5.9%	95,472
117	HORMEL FOODS	46.83	0.93	4.20%	6.3%	25,808
118	HP	16.04	0.70	7.56%	12.3%	24,735
119	HUMANA	340.53	2.50	12.28%	13.1%	51,718
120	HUNT JB TRANSPORT SVS.	97.61	1.08	5.55%	6.7%	11,074
121	HUNTINGTON BCSH.	8.92	0.60	4.90%	12.1%	8,327
122	IDEX	142.74	2.00	11.50%	13.1%	11,617
123	IHS MARKIT	63.25	0.68	11.35%	12.6%	27,206
124	ILLINOIS TOOL WORKS	154.17	4.28	3.01%	5.9%	52,129
125	INTEL	56.04	1.32	9.07%	11.7%	267,165
126	INTERCONTINENTAL EX.	86.70	1.20	8.99%	10.5%	51,138
127	INTERNATIONAL BUS.MCHS.	116.54	6.52	3.92%	9.9%	107,772
128	INTUIT	254.02	2.12	6.82%	7.7%	75,751
129	IRON MOUNTAIN	25.12	2.47	8.00%	19.0%	6,875
130	JACOBS ENGR.	79.57	0.76	10.40%	11.5%	9,941
131	JOHNSON & JOHNSON	138.66	4.04	4.80%	7.9%	389,077
132	JOHNSON CONTROLS INTL.	29.52	1.04	16.29%	20.4%	21,379
133	JP MORGAN CHASE & CO.	95.39	3.60	4.99%	9.0%	278,240
134	KANSAS CITY SOUTHERN	132.39	1.60	10.24%	11.6%	14,133
135	KELLOGG	62.64	2.28	1.78%	5.5%	21,410
136	KIMBERLY-CLARK	133.86	4.28	5.48%	8.9%	46,604
137	KLA	150.25	3.40	12.07%	14.6%	27,586
138	KROGER	32.21	0.64	6.23%	8.4%	25,394
139	L3HARRIS TECHNOLOGIES	183.35	3.40	13.23%	15.3%	38,680
140	LAM RESEARCH	249.29	4.60	13.76%	15.9%	39,364
141	LAMB WESTON HOLDINGS	59.27	0.92	3.40%	5.0%	8,218
142	LEIDOS HOLDINGS	94.89	1.36	10.34%	11.9%	14,050
143	LINCOLN NATIONAL	32.62	1.60	9.88%	15.4%	6,877
144	LINDE	179.78	3.85	10.83%	13.2%	102,931
145	LOCKHEED MARTIN	358.34	9.60	8.78%	11.7%	101,661
146	LOWE'S COMPANIES	99.02	2.20	16.30%	18.9%	88,321
147	MARATHON PETROLEUM	30.36	2.32	1.89%	9.9%	23,943
148	MARKETAXESS HOLDINGS	401.77	2.40	16.25%	16.9%	18,118
149	MARSH & MCLENNAN	94.52	1.82	5.21%	7.3%	52,626

	COMPANY	STOCK PRICE (P <sub>0</sub> )	D <sub>0</sub>	FORECAST OF FUTURE EARNINGS GROWTH	MODEL RESULT	MARKET CAP \$ (MILS)
150	MASCO	39.18	0.54	9.00%	10.5%	12,112
151	MASTERCARD	266.62	1.60	14.21%	14.9%	296,721
152	MAXIM INTEGRATED PRDS.	52.23	1.92	5.22%	9.1%	15,192
153	MCDONALDS	172.55	5.00	3.36%	6.4%	136,889
154	MCKESSON	136.49	1.64	8.16%	9.5%	23,689
155	MEDTRONIC	92.00	2.16	7.46%	10.0%	131,444
156	MERCK & COMPANY	77.07	2.44	6.00%	9.4%	194,078
157	MICROCHIP TECH.	80.64	1.47	8.90%	10.9%	22,399
158	MICROSOFT	166.60	2.04	15.22%	16.6%	1,407,941
159	MONDELEZ INTERNATIONAL CL.A	50.50	1.14	5.89%	8.3%	71,016
160	MOODY'S	232.48	2.24	7.70%	8.7%	48,051
161	MOSAIC	11.69	0.20	7.00%	8.8%	4,442
162	MOTOROLA SOLUTIONS	142.29	2.56	10.32%	12.3%	23,570
163	MSCI	302.87	2.72	10.60%	11.6%	28,549
164	NASDAQ	102.71	1.96	7.47%	9.5%	18,821
165	NETAPP	41.89	1.92	5.96%	10.9%	10,170
166	NEWS 'A'	10.12	0.20	7.17%	9.3%	4,452
167	NEWS 'B'	10.12	0.20	7.17%	9.3%	4,452
168	NEXTERA ENERGY	233.40	5.60	8.01%	10.6%	113,939
169	NIKE 'B'	84.72	0.98	11.73%	13.0%	115,260
170	NISOURCE	24.26	0.84	5.25%	8.9%	8,835
171	NORFOLK SOUTHERN	160.94	3.76	6.29%	8.8%	44,488
172	NORTHERN TRUST	76.52	2.80	2.42%	6.2%	15,554
173	NORTHROP GRUMMAN	319.19	5.28	10.51%	12.3%	53,412
174	NUCOR	38.05	1.61	3.94%	8.4%	12,250
175	NVIDIA	276.05	0.64	13.70%	14.0%	220,662
176	OLD DOMINION FGT.LINES	138.41	0.61	7.33%	7.8%	18,342
177	OMNICOM GROUP	55.81	2.60	1.40%	6.2%	11,237
178	ONEOK	33.55	3.74	0.24%	11.9%	15,112
179	ORACLE	49.55	0.96	9.61%	11.7%	166,825
180	OTIS WORLDWIDE	47.15	0.80	4.30%	6.1%	23,031
181	PACKAGING CORP.OF AM.	90.13	3.16	5.00%	8.7%	8,862
182	PARKER-HANNIFIN	148.66	3.52	3.43%	5.9%	21,587
183	PAYCHEX	65.56	2.48	3.87%	7.9%	24,324
184	PENTAIR	33.30	0.76	5.10%	7.5%	5,951
185	PEPSICO	127.50	4.09	4.64%	8.0%	182,123
186	PERKINELMER	83.56	0.28	10.80%	11.2%	10,331
187	PERRIGO	49.75	0.90	10.00%	12.0%	7,508
188	PHILIP MORRIS INTL.	72.53	4.68	4.03%	10.9%	109,731
189	PINNACLE WEST CAP.	76.83	3.13	4.86%	9.2%	8,186
190	PIONEER NTRL.RES.	83.49	2.20	16.40%	19.5%	15,238
191	PNC FINL.SVS.GP.	103.54	4.60	1.84%	6.4%	44,293
192	PPG INDUSTRIES	90.09	2.04	5.83%	8.2%	22,646
193	PRINCIPAL FINL.GP.	34.35	2.24	6.03%	13.1%	9,892
194	PROCTER & GAMBLE	113.44	3.16	7.53%	10.6%	280,441
195	PRUDENTIAL FINL.	57.03	4.40	9.00%	17.7%	22,341
196	PUB.SER.ENTER.GP.	47.01	1.96	3.70%	8.1%	24,649
197	QUANTA SERVICES	33.07	0.20	8.75%	9.4%	4,617
198	QUEST DIAGNOSTICS	102.41	2.24	4.32%	6.6%	15,240
199	RALPH LAUREN CL.A	77.78	2.75	1.70%	5.3%	3,489
200	REGIONS FINL.NEW	10.28	0.62	8.16%	14.8%	9,645

	COMPANY	STOCK PRICE (P <sub>0</sub> )	D <sub>0</sub>	FORECAST OF FUTURE EARNINGS GROWTH	MODEL RESULT	MARKET CAP \$ (MILS)
201	REPUBLIC SVS.'A'	79.76	1.62	5.68%	7.8%	26,009
202	RESMED	151.57	1.56	21.10%	22.4%	23,402
203	ROCKWELL AUTOMATION	175.54	4.08	3.10%	5.5%	23,864
204	ROPER TECHNOLOGIES	330.70	2.05	5.50%	6.2%	38,405
205	ROSS STORES	87.72	1.14	7.38%	8.8%	32,301
206	S&P GLOBAL	271.55	2.68	8.30%	9.4%	75,643
207	SEAGATE TECH.	48.13	2.60	9.13%	15.1%	13,306
208	SEALED AIR	27.45	0.64	3.95%	6.4%	4,675
209	SEMPRA EN.	118.86	4.18	4.20%	7.9%	35,876
210	SHERWIN-WILLIAMS	497.53	5.36	7.85%	9.0%	51,268
211	SKYWORKS SOLUTIONS	96.52	1.76	11.25%	13.3%	19,583
212	SMITH (AO)	40.38	0.96	8.00%	10.6%	5,736
213	SNAP-ON	121.65	4.32	10.00%	14.0%	7,268
214	SOUTHERN	55.22	2.56	4.35%	9.3%	57,956
215	STANLEY BLACK & DECKER	110.26	2.76	8.24%	11.0%	19,594
216	STARBUCKS	70.64	1.64	4.24%	6.7%	90,847
217	STRYKER	173.08	2.30	5.57%	7.0%	71,690
218	SYSKO	49.56	1.80	7.40%	11.4%	26,691
219	TARGET	106.51	2.64	6.77%	9.4%	59,805
220	TE CONNECTIVITY	70.76	1.92	9.90%	12.9%	25,844
221	TECHNIPFMC	8.42	0.52	7.25%	14.0%	3,358
222	TELEFLEX	318.33	1.36	11.45%	11.9%	16,354
223	TEXAS INSTRUMENTS	108.97	3.60	6.73%	10.3%	107,820
224	THERMO FISHER SCIENTIFIC	311.93	0.88	9.99%	10.3%	134,737
225	TIFFANY & CO	124.34	2.32	8.12%	10.2%	15,251
226	TRACTOR SUPPLY	94.43	1.40	10.23%	11.9%	12,464
227	TYSON FOODS 'A'	58.21	1.68	9.40%	12.6%	17,850
228	UNION PACIFIC	148.76	3.88	10.20%	13.1%	112,663
229	UNITED PARCEL SER.'B'	94.64	4.04	5.60%	10.2%	68,426
230	UNITEDHEALTH GROUP	266.47	4.32	12.80%	14.6%	273,124
231	UNUM GROUP	16.01	1.14	5.37%	13.1%	2,976
232	US BANCORP	35.73	1.68	1.99%	6.9%	49,798
233	V F	57.71	1.92	6.00%	9.6%	21,768
234	VALERO ENERGY	55.63	3.92	6.00%	13.7%	27,454
235	VERISK ANALYTICS CL.A	150.52	1.08	8.79%	9.6%	25,887
236	VERIZON COMMUNICATIONS	54.94	2.46	1.90%	6.5%	224,528
237	VISA 'A'	171.88	1.20	11.52%	12.3%	327,064
238	VULCAN MATERIALS	103.63	1.36	10.41%	11.9%	13,438
239	WABTEC	53.22	0.48	6.35%	7.3%	11,004
240	WALGREENS BOOTS ALLIANCE	43.49	1.83	2.01%	6.4%	35,212
241	WALMART	121.34	2.16	5.50%	7.4%	355,488
242	WEC ENERGY GROUP	88.76	2.53	5.90%	9.0%	27,537
243	WELLS FARGO & CO	29.73	2.04	5.71%	13.2%	100,532
244	WESTERN UNION	19.71	0.90	7.79%	12.8%	7,861
245	WILLIAMS	16.68	1.60	1.98%	12.1%	23,924
246	WILLIS TOWERS WATSON	180.88	2.72	6.50%	8.1%	26,086
247	WW GRAINGER	267.24	5.76	9.50%	11.9%	15,830
248	XCEL ENERGY	60.51	1.72	6.00%	9.0%	31,642
249	XILINX	82.25	1.52	7.45%	9.4%	21,768
250	XYLEM	66.88	1.04	11.31%	13.1%	11,169
251	YUM! BRANDS	78.57	1.88	4.59%	7.1%	26,514

	COMPANY	STOCK PRICE (P <sub>0</sub> )	D <sub>0</sub>	FORECAST OF FUTURE EARNINGS GROWTH	MODEL RESULT	MARKET CAP \$ (MILS)
252	ZIMMER BIOMET HDG.	111.18	0.96	5.55%	6.5%	26,181
253	ZOETIS A	122.98	0.80	6.46%	7.2%	63,329
254	Market-weighted Average				11.5%	

Notes: In applying the DCF model to the S&P 500, I include in the DCF analysis only those companies in the S&P 500 group which pay a dividend, have an available positive analyst's long-term growth estimate.

- D<sub>0</sub> = Current dividend per Refinitiv.  
P<sub>0</sub> = Average of the monthly high and low stock prices during the three months ending May 2020 per Refinitiv.  
g = I/B/E/S forecast of future earnings growth May 2020 per Refinitiv.  
k = Cost of equity using the quarterly version of the DCF model shown below:

$$k = \left[ \frac{d_0(1+g)^{\frac{1}{4}}}{P_0} + (1+g)^{\frac{1}{4}} \right]^4 - 1$$

COMPARABLE EARNINGS VALUE LINE ELECTRIC UTILITIES

	COMPANY	AVERAGE FORECAST ROE 2020 TO 2023-2025	ADJUSTMENT FACTOR	FORECASTED RETURN ON AVERAGE EQUITY
1	ALLETE	7.3%	1.0228	7.5%
2	Alliant Energy	10.3%	1.0150	10.5%
3	Amer. Elec. Power	10.5%	1.0305	10.8%
4	Ameren Corp.	9.7%	1.0393	10.0%
5	AVANGRID Inc.	4.8%	1.0067	4.9%
6	Avista Corp.	7.2%	1.0203	7.3%
7	Black Hills	8.8%	1.0246	9.1%
8	CenterPoint Energy	11.8%	1.0407	12.3%
9	CMS Energy Corp.	13.5%	1.0417	14.1%
10	Consol. Edison	7.8%	1.0245	8.0%
11	Dominion Energy	11.8%	1.0164	12.0%
12	DTE Energy	10.3%	1.0311	10.7%
13	Duke Energy	8.0%	1.0214	8.2%
14	Edison Int'l	10.3%	1.0347	10.7%
15	Entergy Corp.	10.3%	1.0265	10.6%
16	Eversource Energy	7.5%	1.0097	7.6%
17	Exelon Corp.	9.2%	1.0320	9.5%
18	FirstEnergy Corp.	8.3%	1.0211	8.5%
19	Fortis Inc.	16.2%	1.0532	17.0%
20	Hawaiian Elec.	6.5%	1.0197	6.6%
21	IDACORP Inc.	9.0%	1.0226	9.2%
22	MGE Energy	9.0%	1.0163	9.1%
23	NextEra Energy	9.5%	1.0300	9.8%
24	NorthWestern Corp.	11.3%	1.0295	11.7%
25	OGE Energy	8.5%	1.0179	8.7%
26	Otter Tail Corp.	12.0%	1.0015	12.0%
27	Pinnacle West Capital	10.5%	1.0227	10.7%
28	PNM Resources	10.0%	1.0233	10.2%
29	Portland General	8.5%	1.0464	8.9%
30	PPL Corp.	8.7%	1.0155	8.8%
31	Public Serv. Enterprise	13.0%	1.0250	13.3%
32	Sempra Energy	10.8%	0.9943	10.8%
33	Southern Co.	10.2%	1.0529	10.7%
34	WEC Energy Group	12.0%	1.0192	12.2%
35	Xcel Energy Inc.	11.8%	1.0174	12.0%
36	Average	10.3%	1.0306	10.6%
37				10.1%

Data from Value Line reports	
West Value Line	24-Apr-20
East Value Line	15-May-20
Central Value Line	12-Jun-20

Note: The adjustment factor is computed using the formula:  $2 \times (1 + 5\text{-year change in equity}) \div (2 + 5\text{-year change in equity})$ . The adjustment factor is required to convert the Value Line ROE data, which are based on year-end equity, to a rate of return on equity based on average equity for the year.

**AVERAGE MARKET VALUE CAPITAL STRUCTURE  
VALUE LINE ELECTRIC UTILITIES 2015 – 2019**

	YEAR	%LONG- TERM DEBT	%MARKET EQUITY
1	2015	37%	63%
2	2016	35%	65%
3	2017	37%	63%
4	2018	35%	65%
5	2019	40%	60%
6	Average 2015 - 2019	37%	63%

Data from Value Line Investment Analyzer. Data at each year end from Investment Analyzer at May of following year (that is, 2016 as reported at May 2017, for example).